

# Expanding Nuclear Physics Horizons with the Gamma Factory

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The Gamma Factory (GF) is an ambitious proposal, currently explored within the CERN Physics Beyond Colliders program, for a source of photons with energies up to  $\approx 400$  MeV and photon fluxes (up to  $\approx 10^{17}$  photons  $s^{-1}$ ) exceeding those of the currently available gamma sources by orders of magnitude. The high-energy (secondary) photons are produced via resonant scattering of the primary laser photons by highly relativistic partially-stripped ions circulating in the accelerator. The secondary photons are emitted in a narrow cone and the energy of the beam can be monochromatized, down to  $10^{-3}$ – $10^{-6}$  level, via collimation, at the expense of the photon flux. This paper surveys the new opportunities that may be afforded by the GF in nuclear physics and related fields.

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## 1. Introduction

The Gamma Factory (GF) is a novel research tool proposed in ref. [1] and subsequently developed at CERN as part of its Physics Beyond Colliders studies.<sup>[2]</sup> The main aim of the GF is the generation of high-intensity gamma-ray beams of tunable energy and relatively small energy spread. At the same time, the GF facility offers unique scientific opportunities by far not limited to the various uses of the produced gamma rays (the secondary beam), but also includes spectroscopy of stored relativistic ions, including radioactive ions, with the (primary, energy boosted) laser photons that are used to produce the gamma rays, as well as the production and use of various tertiary beams.

As a unique and unprecedented research tool, the GF opens new possibilities across several fields of physics, from atomic physics (with the opportunities surveyed in ref. [3]) to nuclear physics and related fields (the subject of the present paper), to elementary-particle physics and searches for physics beyond the standard model (SM). While the GF today is still a proposal, some of its key components such as the production and storage of partially stripped ions (PSI), for instance hydrogen- and helium-like Pb and phosphorus-like Xe,<sup>[4–6]</sup> have been already demonstrated experimentally in the Super Proton Synchrotron (SPS) and the Large Hadron Collider (LHC) at CERN. Moreover, the proof-of-principle experiment,<sup>[7]</sup> further discussed in Section 13, will demonstrate the full GF concept at SPS. The design of the experiments is complete, awaiting approval of the SPS Committee.

### 1.1. The Gamma Factory

The principle of the GF is illustrated in **Figure 1**. Highly charged partially-stripped ions circulate in a storage ring at ultrarelativistic speeds with a Lorentz factor  $\gamma = (1 - \beta^2)^{-1/2}$ , with  $\beta = v/c \approx 1$  being the ion speed normalized by the speed of light. The electrons bound to these ions interact with a (primary) laser beam and undergo transitions between the atomic shells. The resonance fluorescence photons, as seen in the laboratory frame, are emitted in a narrow cone with opening angle of  $\approx 1/\gamma$ , and form the secondary beam. The photon energy is boosted by a factor of  $\approx 4\gamma^2$  with respect to the original laser photons used for the electronic excitation. The anticipated secondary beam parameters are listed in **Table 1**. In many respects, the GF will be a qualitative leap compared to the existing gamma sources, as well as sources currently under construction. These are briefly discussed in Appendix A.

Successful excitation of an atomic shell relies on a resonance condition involving both the relativistic factor  $\gamma$  of the PSI as well as the primary (optical) laser frequency  $\omega$ . Thus, the tunability of the secondary beam energy is achieved by simultaneously tuning  $\gamma$  and adjusting the wavelength or the incident angle  $\theta_i$  of the

primary laser beam to maintain the resonance with an atomic transition in the PSI ( $\hbar\omega'$ )

$$\hbar\omega' = \hbar\omega\gamma(1 + \beta \cos \theta_i) \quad (1)$$

The ion beam energy variation is a routine procedure in a storage ring. Indeed, at the LHC, the ions are injected with an initial relativistic factor of around  $\gamma = 220$ , and are subsequently accelerated up to  $\gamma = 2900$ . Tunable-laser technologies are also well developed.

The secondary gamma-ray beam will have a strong correlation between the emission angle  $\theta$  (see **Figure 1**) and the gamma-ray energy  $E$  given by the expression

$$E(\theta) = \frac{E_{\max}}{2\gamma^2(1 - \beta \cos \theta)} \quad (2)$$

where  $E_{\max} = (1 + \beta)\gamma\hbar\omega'$ . For small angles this can be approximated as

$$E(\theta) \approx \frac{E_{\max}}{1 + \gamma^2\theta^2} \approx \frac{4\gamma^2\hbar\omega}{1 + \gamma^2\theta^2} \quad (3)$$

A small fraction of photons are emitted with large angles,  $\theta \approx 1$ , and in this case the emitted photon energy is comparable to the incident laser photon energy. For instance

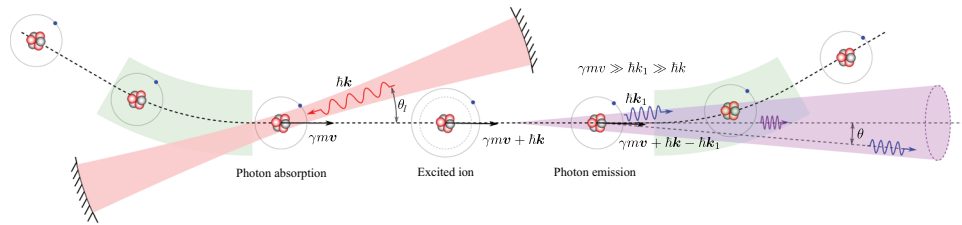
$$E\left(\frac{\pi}{2}\right) = \frac{E_{\max}}{2\gamma^2} \approx 2\hbar\omega \quad (4)$$

For a given emission angle, the residual photon energy spread is mainly determined by the angular spread of the PSI beam and its angular size as seen from the observation point (the location of the target or detector). A typical normalized transverse emittance of the ion beam in the LHC is  $\epsilon_n = \gamma\sigma_x\sigma_{x'} \approx 1$  mm-mrad. The transverse beam size in the LHC can be varied from  $\approx 1$  mm down to  $\approx 10$   $\mu\text{m}$  (in the collider interaction points). With a mm-wide ion beam,  $\sigma_x \approx 1$  mm and for  $\gamma \approx 10^3$ , this corresponds to angular spread on the order of a microradian  $\sigma_{x'} = \epsilon_n/\gamma\sigma_x \approx 10^{-6}$ . Therefore, the uncorrelated energy spread of the secondary gamma-photon beam will be on the order of  $\delta\theta/\theta \approx \sigma_{x'}\gamma \approx 10^{-3}$  (see **Figure 2**). However, for the visible angular size of the mm-wide source of photons to drop below 1  $\mu\text{rad}$ , the distance to the observation point should be more than 1 km.

Laser cooling can potentially dramatically reduce the ion-beam emittance and energy spread. The transverse-only laser cooling<sup>[8]</sup> can be applied to reduce the transverse beam size and angular spread by one order of magnitude at which point the energy spread in the ion beam will become important, since the typical relative energy spread in the LHC ion beam is on the order of  $10^{-4}$ . To improve the energy-angle correlation in the resulting gamma-photon beam to better than  $10^{-4}$ , both transverse and longitudinal laser cooling should be applied.<sup>[8–10]</sup> Deep laser cooling will be limited by the intrabeam scattering and other collective effects.

In summary, an optimal trade-off between the gamma beam intensity and its spectral resolution will have to be made for each of the usage cases of the GF beams, including case-by-case choice of the number of ions per bunch, interaction-point collision

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**Figure 1.** The Gamma Factory concept. Laser photons with momentum  $\hbar k$  (the primary photon beam) impinge onto ultrarelativistic ions (relativistic factor  $\gamma$ , mass  $m$ , velocity  $v$ ) circulating in a storage ring. Resonantly scattered photons, as seen in the laboratory frame, are emitted in a narrow cone with an opening angle  $\approx 1/\gamma$  in the direction of the motion of the ions. The energy of these secondary photons is boosted by a factor of up to  $4\gamma^2$  with respect to the energy of the initial photons.

optics, beam emittance, and the distance of the gamma beam target to its production point.

Beside their energy and emission pattern, the secondary photons are characterized by their polarization. The polarization depends not only on the emission angle  $\theta$ , but also on the polarization state (e.g., magnetic sublevel population) of the incident PSI and the polarization of incident laser photons. A proper choice of these parameters results in emission of secondary gamma rays with high degrees of circular or linear, and generally, arbitrary polarization. A detailed analysis of the polarization of scattered photons, as performed using the density-matrix approach, is presented in ref. [12].

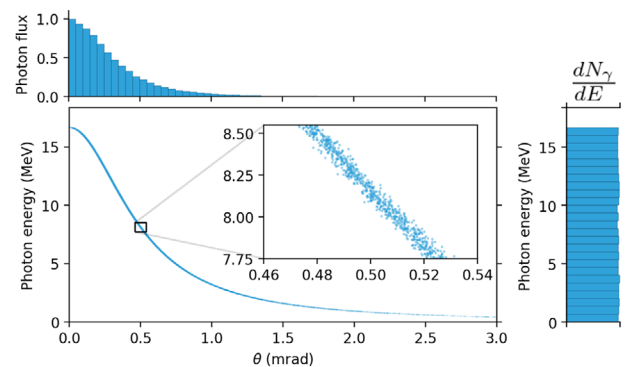
## 1.2. The Goals and Main Results of This Paper

Realization of the GF project will result in a new facility based on the significant progress achieved in accelerator physics, laser technology, detectors, control devices, computer control, and data-analysis techniques. The state-of-the-art modern instrumentation and measurement techniques will enable the next step in our understanding of deep problems in nuclear, atomic, and hadron physics.

**Table 1.** Representative parameters of the Gamma Factory at CERN with currently available ion beams.  $q$  denotes the charge state of the ions. The numbers are presented for Pb ions. Note that the current optimization for the LHC is for the collider mode. A dedicated optimization for the GF may lead to improvements.

Parameter	Value	Note
Ion $\gamma$ factor	10 – 2900	a)
Ion species	Pb <sup>q+</sup> as an example	
Transverse beam radius	16 $\mu\text{m}$	
Number of ions in a bunch	$10^8$	b)
Number of bunches in the ring	592 – 1232	
Effective repetition rate	10 MHz	c)
Ion energy spread	$10^{-4}$	
RMS bunch length	7.9 cm	
Normalized emittance	1.6 $\mu\text{m}$	
Circumference of the LHC	26.7 km	

a) The lowest  $\gamma$  factors are for the SPS. At the LHC, they are  $\approx 200$ ; b) A larger number can be expected for lighter PSI,<sup>[13]</sup> for example,  $3 \cdot 10^9$  for He-like Ca; c) 20 MHz planned after the LHC injector upgrade



**Figure 2.** Correlation between the energy and angle of emitted photon in one particular case of the Gamma Factory based on hydrogen-like calcium ion beam in the LHC. The top histogram shows the corresponding photon flux density (photons per unit area per unit time) into a small solid angle. The right histogram shows the flat energy spectrum. The ion beam parameters in this example are:  $\gamma = 2048$ ,  $\sigma_x = 0.44$  mm,  $\sigma_{x'} = 2.2$   $\mu\text{rad}$  (normalized emittance  $\epsilon_n = \gamma\sigma_x\sigma_{x'} = 2$  mm·mrad).<sup>[11]</sup>

Historically, new tools have led to new discoveries. Therefore, as we survey the science opportunities offered by the GF, we attempt to identify novel, potentially breakthrough directions. Here are some of these:

- Physics opportunities with primary (Section 2) and secondary (Section 4) beams with previously unattainable parameters;
- Spectroscopy of nuclear gamma transitions on par with laser spectroscopy of atoms (Section 2);
- Investigation of the physics of exotic nuclei and of the mechanism of their stability along the road to the drip lines (Section 6);
- Direct measurements of astrophysical S-factors at relevant energies (Section 4.4.3);
- Resolving narrow resonances in the photofission cross section of actinides via state-selective high-resolution spectroscopy (Section 4.5);
- Pionic (Section 4.8) and Delta-resonance (Section 4.10) physics on a qualitatively and quantitatively new level of precision;
- Precision measurement of parity violation (PV) in hadronic and nuclear systems at previously inaccessible levels (Section 4.11);
- Investigation of exotic radioactive nuclei in conjunction with the CERN Isotope mass Separator On-Line (ISOLDE) facility (Section 4) and/or a dedicated storage ring (Section 6);

- Production of copious amounts of isotopes and nuclear isomers for medicine, dark matter search, and gamma lasers via photonuclear reactions (Section 8);
- Gamma polarimetry at the  $< 10^{-6}$  rad level (Section 10.1);
- Production of and physics opportunities with high-intensity, monoenergetic, and small-emittance tertiary beams (neutrons, muons, neutrinos, etc.; Section 12).

In this paper, we outline a possible nuclear physics program for the GF, successively addressing the opportunities afforded by using the primary photon beams (starting with spectroscopy of stored ions with primary photons in Section 2), the secondary photon beams (starting with a discussion of fixed-target experiments in Section 4), followed with a discussion of production and use of tertiary beams of various particles in Section 12.

## 2. Nuclear Spectroscopy in the Ion Beam

Laser spectroscopy of atomic transitions is well established in ion storage rings, see, for example, refs.<sup>[14,15]</sup> Precision spectroscopy of nuclear transitions may also be possible with the GF.

With the initial laser-photon energy of up to 10 eV and the relativistic factor at the LHC of up to  $\gamma \approx 3000$ , in their reference frame, the circulating ions “see” the photon energies up to 60 keV, high enough to excite low-lying nuclear states. This opens up possibilities of nuclear spectroscopy or even nuclear quantum optics already with the primary GF beam. For this purpose, it is not necessary to use PSI and the experiments can be performed with bare ions. The prospects of combining relativistically accelerated nuclei as a target with presently available coherent light sources for first nuclear quantum optics experiments were originally discussed in ref. [16]. At that time, a combination of X-ray free electron lasers and more moderate target acceleration was envisaged. This in turn posed severe challenges due to the geographical distance between the required large-scale facilities, with table-top laser or accelerator alternatives still lacking in performance.<sup>[17,18]</sup> The GF envisaged at CERN is in a unique position of achieving high photon energies even with (table-top) lasers operating in the visible and ultraviolet (UV) ranges, thus opening new possibilities for nuclear quantum optics experiments.

In this section, we give examples of low-lying nuclear transitions that can be driven by the primary laser light of the GF, discuss the opportunities related to nuclear isomers and possible couplings between the nuclear and atomic degrees of freedom, and put forward further prospects for using nuclear transitions for laser cooling or obtaining even higher gamma-ray energies at the GF.

One needs to point out that direct spectroscopy of nuclear transitions at the GF would require overcoming a number of specific challenges, including ensuring the availability of ion sources with stable or radioactive isotopes capable of producing beams of sufficient intensity, operation of the full accelerator chain with radioactive species, as well as low excitation rates and long decay times of the narrow excited states. None of these appear as a priori “show stoppers,” but would need to be carefully addressed on a case-by-case basis.

### 2.1. Low-Energy Nuclear Transitions

Examples of low-energy gamma transitions starting from a stable or long-lived nuclear ground state are listed in **Table 2**. Typically, the low-lying nuclear spectrum can be described by collective rotations and vibrations of the nuclear surface,<sup>[19]</sup> and such excited states frequently connect to the ground state via electric-dipole-forbidden transitions.<sup>[20]</sup> Direct spectroscopy on these transitions can provide detailed information, for example, on the relative role of different transition multipoles (e.g.,  $M1$  and  $E2$  mixing), or provide accurate transition probabilities. In the context of nuclear quantum optics, many of these transitions were theoretically investigated for coherent driving with X-ray free electron laser sources.<sup>[16,20,21]</sup>

We note that some of the transitions to the ground state listed in Table 2 have not been directly observed, indicating their strong degree of suppression. For instance, due to its low energy, the radiative decay channel of the 8 eV first excited state in  $^{229}\text{Th}$  has not been observed so far, despite many experimental attempts of direct photoexcitation.<sup>[22]</sup> This peculiar “isomeric” transition is discussed in more detail in the context of the GF in the next section. In addition, the 13.034 and 51.697 keV excited states in  $^{235}\text{U}$  have only been observed to connect to the 76 eV long-lived first excited state.<sup>[23]</sup> This is attributed to selection rules for the  $K$ -quantum number, that is, the nuclear spin projection on the symmetry axis. In Table 2 we therefore list instead the available experimental data on the two transitions to the isomeric state. Detailed investigations of strongly suppressed transitions at the GF, for instance the ones connecting the 13.034 and 51.697 keV levels of  $^{235}\text{U}$  to the ground state, would contribute to a better understanding of nuclear structure and the interplay between nuclear collective and single-particle degrees of freedom.

In addition to transitions connecting the nuclear ground state with a low-lying excited state, one can envisage the use of nuclei in metastable states as PSI in the ion beam. Such nuclear metastable states are also known as isomers and can store large amounts of energy over long period of time. Their existence is typically attributed to large differences in spin, shape or  $K$  quantum number, between the isomer and the lower-lying levels.<sup>[24,25]</sup> In an advantageous configuration of the nuclear excited levels, once the excitation occurs from the isomeric state to an upper gateway level, the subsequent nuclear decay may proceed directly to a state below the isomer, thus reaching the ground state in a fast cascade. Such a process is called isomer depletion, since it allows for the depopulation of the isomeric state and thus a controlled release of the energy stored in the metastable state. A typical example is the case of the 2.4 MeV  $^{93m}\text{Mo}$  isomer, for which we present the relevant partial level scheme in **Figure 3**. An excitation scheme involving such a  $\Lambda$ -like three-level system (of the states  $I$ ,  $G$ , and  $F$  in the Figure 3 example), known as Raman-type excitation in atomic and molecular physics, is advantageous since the excitation and decay photons have different energies and can therefore be more easily distinguished in experiments. In the context of isomers, an additional fascinating potential application is related to the controlled release of nuclear energy on demand that would allow the design of a clean nuclear energy storage solution without involving fission or fusion.<sup>[24]</sup> A list of nuclear isomer parameters

**Table 2.** Examples of low-energy nuclear transitions, sorted by energy, with the lower state being a stable or long-lived ground (or isomeric) state with half-life  $T_{1/2}^g$  and nuclear spin  $I_g$ . The excited state energy  $E_e$  and the dominant multipolarity  $\lambda L$  are given together with the excited state spin  $I_e$ .  $T_{1/2}^{\text{rad}}$  corresponds to the calculated radiative half-life of the excited state.  $\alpha(K/L)$  is the internal conversion coefficient of the transition corresponding to the  $K/L$ -shell electrons. The  $\alpha(K/L)$  values are calculated or measured for neutral atoms. Nuclear parameters were taken from the ENSDF database<sup>[32]</sup> unless otherwise specified.

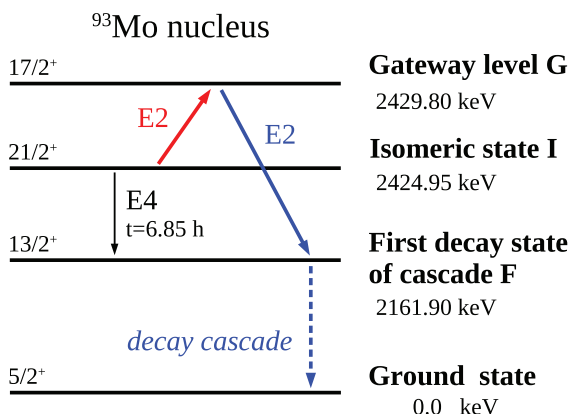
Isotope	$T_{1/2}^g$	$E_e$ [keV]	$I_g$	$I_e$	$\lambda L$	$T_{1/2}^{\text{rad}}$ [s]	$\alpha(K)$	$\alpha(L)$
<sup>229</sup> Th	7880 y	0.008 <sup>a)</sup>	5/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	5.19 × 10 <sup>3</sup>	–	–
<sup>235</sup> U	7 × 10 <sup>8</sup> y	0.076	7/2 <sup>–</sup>	1/2 <sup>+</sup>	E3	7.03 × 10 <sup>23b)</sup>	–	–
<sup>201</sup> Hg	stable	1.565	3/2 <sup>–</sup>	1/2 <sup>–</sup>	M1	3.76 × 10 <sup>–3</sup>	–	–
<sup>205</sup> Pb	1.7 × 10 <sup>7</sup> y	2.329	5/2 <sup>–</sup>	1/2 <sup>–</sup>	E2	9.07 × 10 <sup>2</sup>	–	–
<sup>181</sup> Ta	stable	6.238	7/2 <sup>+</sup>	9/2 <sup>–</sup>	E1	4.34 × 10 <sup>–4</sup>	–	–
<sup>239</sup> Pu	2.4 × 10 <sup>4</sup> y	7.861	1/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	2.04 × 10 <sup>–7</sup>	–	–
<sup>169</sup> Tm	stable	8.410	1/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	1.07 × 10 <sup>–6</sup>	–	–
<sup>83</sup> Kr	stable	9.406	9/2 <sup>+</sup>	7/2 <sup>+</sup>	M1	2.80 × 10 <sup>–6</sup>	–	14
<sup>187</sup> Os	stable	9.756	1/2 <sup>–</sup>	3/2 <sup>–</sup>	M1	9.01 × 10 <sup>–7</sup>	–	–
<sup>137</sup> La	6 × 10 <sup>4</sup> y	10.560	7/2 <sup>+</sup>	5/2 <sup>+</sup>	M1	1.04 × 10 <sup>–5</sup>	–	93.2
<sup>45</sup> Sc	stable	12.400	7/2 <sup>–</sup>	3/2 <sup>+</sup>	(M2)	1.96 × 10 <sup>2</sup>	362	54
<sup>235</sup> U	– <sup>c)</sup>	13.034	1/2 <sup>+</sup> <sup>d)</sup>	3/2 <sup>+</sup>	M1	2.43 × 10 <sup>–7e)</sup>	–	–
<sup>73</sup> Ge	stable	13.284	9/2 <sup>+</sup>	5/2 <sup>+</sup>	E2	3.1 × 10 <sup>–3</sup>	299	666
<sup>57</sup> Fe	stable	14.413	1/2 <sup>–</sup>	3/2 <sup>–</sup>	M1	9.32 × 10 <sup>–7</sup>	7.35	0.78
<sup>151</sup> Eu	≥ 1.7 × 10 <sup>18</sup> y	21.541	5/2 <sup>+</sup>	7/2 <sup>+</sup>	M1	2.62 × 10 <sup>–7</sup>	–	21.7
<sup>149</sup> Sm	stable	22.507	7/2 <sup>–</sup>	5/2 <sup>–</sup>	M1	2.24 × 10 <sup>–7</sup>	–	22.2 <sup>f)</sup>
<sup>119</sup> Sn	stable	23.871	1/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	1.07 × 10 <sup>–7</sup>	–	4.1
<sup>161</sup> Dy	stable	25.651	5/2 <sup>+</sup>	5/2 <sup>–</sup>	E1	9.59 × 10 <sup>–8</sup>	–	1.79 <sup>f)</sup>
<sup>201</sup> Hg	stable	26.272	3/2 <sup>–</sup>	5/2 <sup>–</sup>	M1	4.61 × 10 <sup>–8</sup>	–	55.9 <sup>f)</sup>
<sup>129</sup> I	1.6 × 10 <sup>7</sup> y	27.793	7/2 <sup>+</sup>	5/2 <sup>+</sup>	M1	1.02 × 10 <sup>–7</sup>	–	4.06
<sup>229</sup> Th	7880 y	29.190	5/2 <sup>+</sup>	5/2 <sup>+</sup>	M1	3.26 × 10 <sup>–8g)</sup>	–	168 <sup>f)</sup>
<sup>40</sup> K	1.2 × 10 <sup>9</sup> y	29.830	4 <sup>–</sup>	3 <sup>–</sup>	M1	5.47 × 10 <sup>–9</sup>	0.26 <sup>f)</sup>	0.023 <sup>f)</sup>
<sup>201</sup> Hg	stable	32.145	3/2 <sup>–</sup>	3/2 <sup>–</sup>	M1	5.04 × 10 <sup>–9h)</sup>	–	30.8 <sup>f)</sup>
<sup>237</sup> Np	2.1 × 10 <sup>6</sup> y	33.196	5/2 <sup>+</sup>	7/2 <sup>+</sup>	M1	9.92 × 10 <sup>–9</sup>	–	131 <sup>f)</sup>
<sup>125</sup> Te	stable	35.492	1/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	2.15 × 10 <sup>–8</sup>	11.69	1.602
<sup>189</sup> Os	stable	36.200	3/2 <sup>–</sup>	1/2 <sup>–</sup>	M1	1.09 × 10 <sup>–8</sup>	–	15.6
<sup>121</sup> Sb	stable	37.129	5/2 <sup>+</sup>	7/2 <sup>+</sup>	M1	4.06 × 10 <sup>–8</sup>	9.36	1.227
<sup>129</sup> Xe	stable	39.578	1/2 <sup>+</sup>	3/2 <sup>+</sup>	M1	1.25 × 10 <sup>–8</sup>	10.27	1.41
<sup>233</sup> U	1.6 × 10 <sup>5</sup> y	40.351	5/2 <sup>+</sup>	7/2 <sup>+</sup>	M1 <sup>i)</sup>	1.03 × 10 <sup>–7</sup>	–	374 <sup>f)</sup>
<sup>243</sup> Am	7364 y	42.20	5/2 <sup>–</sup>	7/2 <sup>–</sup>	M1	6.43 × 10 <sup>–9</sup>	–	110
<sup>229</sup> Th	7880 y	42.435	5/2 <sup>+</sup>	7/2 <sup>+</sup>	M1	2.59 × 10 <sup>–8</sup>	–	99.3 <sup>f)</sup>
<sup>240</sup> Pu	6561 y	42.824	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.55 × 10 <sup>–7</sup>	–	658
<sup>246</sup> Cm	4706 y	42.852	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.31 × 10 <sup>–7</sup>	–	770 <sup>f)</sup>
<sup>248</sup> Cm	3.5 × 10 <sup>5</sup> y	43.400	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.22 × 10 <sup>–7</sup>	–	724 <sup>f)</sup>
<sup>234</sup> U	2.5 × 10 <sup>5</sup> y	43.498	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.80 × 10 <sup>–7</sup>	–	520
<sup>244</sup> Pu	8.1 × 10 <sup>7</sup> y	44.2	0 <sup>+</sup>	2 <sup>+</sup>	(E2)	1.23 × 10 <sup>–7</sup>	–	560
<sup>242</sup> Pu	3.7 × 10 <sup>5</sup> y	44.54	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.20 × 10 <sup>–7</sup>	–	543 <sup>f)</sup>
<sup>238</sup> U	4.5 × 10 <sup>9</sup> y	44.916	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.26 × 10 <sup>–7</sup>	–	444
<sup>236</sup> U	2.3 × 10 <sup>7</sup> y	45.242	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.38 × 10 <sup>–7</sup>	–	429
<sup>235</sup> U	7 × 10 <sup>8</sup> y	46.103	7/2 <sup>–</sup>	9/2 <sup>–</sup>	M1	7.15 × 10 <sup>–10</sup>	–	40
<sup>183</sup> W	≥ 6.7 × 10 <sup>20</sup> y	46.484	1/2 <sup>–</sup>	3/2 <sup>–</sup>	M1	1.73 × 10 <sup>–9</sup>	–	6.46 <sup>f)</sup>
<sup>232</sup> Th	1.4 × 10 <sup>10</sup> y	49.369	0 <sup>+</sup>	2 <sup>+</sup>	E2	1.15 × 10 <sup>–7</sup>	–	244
<sup>81</sup> Kr	2.3 × 10 <sup>5</sup> y	49.57	7/2 <sup>+</sup>	9/2 <sup>+</sup>	M1	9.41 × 10 <sup>–9</sup>	1.117 <sup>f)</sup>	0.169 <sup>f)</sup>
<sup>235</sup> U	– <sup>c)</sup>	51.697	1/2 <sup>+</sup> <sup>d)</sup>	5/2 <sup>+</sup>	E2	8.34 × 10 <sup>–8e)</sup>	–	226
<sup>230</sup> Th	7.5 × 10 <sup>4</sup> y	53.227	0 <sup>+</sup>	2 <sup>+</sup>	E2	8.08 × 10 <sup>–8</sup>	–	166.8

(Continued)

Table 2. Continued.

Isotope	$T_{1/2}^g$	$E_e$ [keV]	$I_g$	$I_e$	$\lambda L$	$T_{1/2}^{\text{rad}}$ [s]	$\alpha(K)$	$\alpha(L)$
$^{157}\text{Gd}$	stable	54.536	$3/2^-$	$5/2^-$	$M1$	$1.74 \times 10^{-9}$	$9.50^{\text{j}}$	2
$^{239}\text{Pu}$	$2.4 \times 10^4$ y	57.275	$1/2^+$	$5/2^+$	$E2$	$3.58 \times 10^{-8}$	–	161.1
$^{237}\text{Np}$	$2.1 \times 10^6$ y	59.540	$5/2^+$	$5/2^-$	$E1$	$1.86 \times 10^{-7\text{h}}$	–	$0.376^{\text{f}}$
$^{155}\text{Gd}$	stable	60.010	$3/2^-$	$5/2^-$	$M1$	$2.04 \times 10^{-9}$	7.25	1.48

<sup>a)</sup> transition energy from, refs. [26, 27] and radiative transition rate deduced using theoretical predictions in ref. [28]; <sup>b)</sup> using theoretical predictions from ref. [29]; <sup>c)</sup> the isomeric state at 0.076 keV is considered as the ground state for this transition. In PSI the IC channel of the isomeric decay is closed and the radiative half-life would be much longer than the ground-state  $\alpha$  decay half-life; <sup>d)</sup> isomeric state spin; <sup>e)</sup> Radiative decay rate is given for the transition to the isomeric state at 0.076 keV; <sup>f)</sup> theoretical values derived using the *Brlcc* database<sup>[30]</sup> based on ref. [31] with corresponding mixing-ratio data from the ENSDF database;<sup>[32]</sup> <sup>g)</sup> using theoretical predictions from ref. [33]; <sup>h)</sup> calculated for the direct decay to the ground state only; <sup>i)</sup> this transition has  $M1 + E2$  multipolarity with a large mixing ratio  $\delta \approx 0.93$ .  $M1$  is the dominant radiative channel by a small margin; <sup>j)</sup> for He- or H-like ions, the ionization potential increases closing the IC channel and  $\alpha(K) = 0$ .



**Figure 3.** Partial level scheme of  $^{93}_{42}\text{Mo}$ . The isomeric state (I) can be excited to the gateway level (G) which subsequently decays back to I or to a level F, initiating a cascade via different intermediate states (dashed line) to the ground state. The direct  $I \rightarrow F$  decay is a strongly hindered  $E4$  transition, while  $I \rightarrow G$  and  $G \rightarrow F$  are prompt  $E2$  transitions.

useful for potential isomer depletion as well as other applications such as medical applications or gamma-ray lasers are presented in Tables 7–10. An idea on how to use the GF for spectroscopy of isomers and possible depleting levels above them is sketched in Section 2.4.1.

## 2.2. The Lowest-Lying Nuclear Isomer $^{229\text{m}}\text{Th}$

Considerable interest in both theory and experiment has been paid in the past years to the lowest-known nuclear excited state, lying at only  $\approx 8$  eV above the ground state of  $^{229}\text{Th}$ .<sup>[26,27]</sup>  $^{229}\text{Th}$  belongs to the light actinide nuclear mass region known for the presence of enhanced collectivity and shape-dynamic properties.<sup>[34]</sup> The single-particle states of the odd neutron determine the  $^{229}\text{Th}$  ground state with  $K^\pi = 5/2^+$  and the isomeric state with  $K^\pi = 3/2^+$  based on the  $5/2^+[633]$  and  $3/2^+[631]$  single-particle orbitals. Here  $K$  refers again to the projection of the total nuclear angular momentum on the body-fixed principal symmetry axis of the system,  $\pi$  is parity, and we use the usual Nilsson notation  $K^\pi[Nn_z\Lambda]$  with  $N$ ,  $n_z$ , and  $\Lambda$  being the asymptotic Nilsson quantum numbers.<sup>[35]</sup>

Because the isomeric transition energy is accessible with vacuum-ultraviolet lasers,  $^{229\text{m}}\text{Th}$  is the best candidate for a nu-

clear clock, that is, a clock based on a nuclear rather than an electronic transition.<sup>[36–38]</sup> At the GF, the low-energy isomeric transition can be in principle accessed with a primary infrared laser beam nearly counter propagating with the ion beam or an optical laser beam directed at an obtuse angle to the ion beam. In addition, one can also make use of the higher levels of  $^{229}\text{Th}$  to populate the isomer. Indeed, in a recent nuclear resonant scattering (NRS) experiment performed on a solid-state thorium-oxide target at the synchrotron-radiation source at SPring-8 in Japan, the  $^{229\text{m}}\text{Th}$  isomer was excited indirectly via population of a higher-lying excited state.<sup>[39]</sup> Resonant X-rays were driving the transition between the ground state  $5/2^+[633]$  and the second excited state  $5/2^+[631]$  at 29.19 keV (see also Table 2). This excited state decays with a branching ratio of  $\approx 0.9$  to the isomeric state  $3/2^+[631]$ . This is another example of Raman-type excitation in a nuclear  $\Lambda$  three-level system similar to the isomer-depletion process discussed in Section 2.1, however, now with the aim of populating instead of depleting the long-lived state.

The NRS experiment provided valuable information about the properties of the second excited state of  $^{229}\text{Th}$ , whose excitation energy of about 29.2 keV has been determined with sub-eV accuracy. In addition, it also opened a new route for the determination of the  $^{229\text{m}}\text{Th}$  energy,<sup>[39,40]</sup> though so far less precisely than the best prior measurements.<sup>[26,27]</sup> However, one of the drawbacks for NRS experiments is the use of solid-state targets, in which the predominant nuclear decay is via internal conversion, quenching the isomeric state in microseconds.<sup>[38]</sup> This is where the unique capabilities of the storage-ring experiments can come into play. For example, one could employ a  $^{229}\text{Th}$ -ion beam in a dedicated storage ring, see Section 6. At the LHC, it may be possible to work with  $^{229}\text{Th}^{q+}$  ions with charge states  $q = 84\text{--}90$ , for which the internal conversion channel is closed, since only  $2p_{3/2}$  orbitals and higher have ionization potentials smaller than 29 keV. With  $^{229}\text{Th}$  ions in various charge states, one can also investigate the nuclear hyperfine mixing effect, which is expected to significantly shorten the isomer lifetime in particular charge states, with considerable differences between odd- and even-charge states.<sup>[41]</sup>

At the GF, one can drive the 29 keV transition in the relativistic Th ions, allowing for precision studies of excited state properties. We may then envisage coherent nuclear driving with two narrowband UV primary beams that can excite simultaneously the two  $M1$  transitions  $5/2^+[633] \rightarrow 5/2^+[631]$  and  $3/2^+[631] \rightarrow 5/2^+[631]$ , both at  $\approx 29$  keV. Varying the frequency of the second laser beam driving the  $3/2^+[631] \rightarrow 5/2^+[631]$  transition, would

provide an independent route to determine the energy of the isomeric nuclear state  $^{229m}\text{Th}$  with  $10^{-2}$  eV or perhaps even better accuracy. In addition, the two secondary X-ray beams would open, for the first time, the possibility to exploit quantum-optics schemes as known from atomic or molecular  $\Lambda$ -systems directly with nuclear transitions.

In particular we can, in principle, envisage so-called  $\pi$ -pulses which swap the population between the lower and the upper state for each of the transitions, or stimulated Raman adiabatic passage (STIRAP)<sup>[42,43]</sup> between the ground state and the isomeric state. The latter would have the advantage that the population is coherently and efficiently transferred from the ground state  $5/2^+[633]$  to the isomeric state  $3/2^+[631]$  independently of the branching ratio of the excited state. While already proposed for nuclear coherent population transfer,<sup>[17]</sup> the lack of suitable X-ray and gamma-ray facilities has prevented STIRAP from being observed for nuclear transitions so far. This could change with the advent of the GF. Laser phase fluctuations are known to reduce the performance of STIRAP<sup>[44]</sup> as adiabaticity is disturbed during phase jumps. Nearly transform-limited pulses are best suited for experimental implementation of STIRAP.<sup>[42,44]</sup> Such coherence properties of the driving beams should be available from the primary UV lasers.

Finally, we mention that, in principle, direct excitation of the low-energy isomeric state in  $^{229}\text{Th}$  should be possible also with the approach of driving  $\approx\text{eV}$  M1 transitions using microwaves with Lorentz boost of photon energies, as discussed in Section 14.5.

### 2.3. Interaction of Nuclear and Atomic Degrees of Freedom

The GF can be used to drive nuclear or atomic transitions in the ion beam with energies of up to  $\approx 60$  keV. In this region, the coupling of the nuclear and atomic degrees of freedom can be rather strong. Thus, the GF could become a powerful tool to explore the interplay between nuclear excitation or decay and electronic transitions. In the following, we outline the relevant processes and experimental prospects.

We address separately weak-interaction and electromagnetic-interaction processes involving atomic electrons; for hyperfine interaction effects we refer to the review on the atomic physics opportunities at the GF.<sup>[3]</sup> In the first category fall the electron-capture (EC) and bound  $\beta$  decay channels. EC cannot occur in bare ions because of the absence of  $K$ -shell electrons. Furthermore, it was shown that for the cases of  $^{140}\text{Pr}$  and  $^{142}\text{Pm}$ , the nuclear lifetime of the one-electron  $\text{Pr}^{58+}$  ( $\text{Pm}^{60+}$ ) ion is shorter than the ones of the corresponding two- or many-electron cases.<sup>[45,46]</sup> This could be explained by conservation of the total angular momentum, since only particular spin orientations of the nucleus and of the captured electron can contribute to the allowed EC decay.<sup>[47]</sup> This selection rule leads to the acceleration of the allowed Gamow–Teller  $1^+ \rightarrow 0^+$  decay in one-electron  $\text{Pr}^{58+}$  and  $\text{Pm}^{60+}$  ions, while it stalls  $1^+ \rightarrow 2^+$  decays in one-electron  $^{122}\text{I}$  ions.<sup>[48]</sup> Bound  $\beta$  decay, on the other hand, can only occur if vacancies in the atomic shell are available for the  $\beta^-$  particle to occupy. The process and corresponding nuclear lifetime are sensitive to the electronic environment. For example, for bare  $^{163}\text{Dy}$  and  $^{187}\text{Re}$  ions, the empty  $K$  shells enable  $\beta^-$  decay into these

atomic orbits with half-lives of  $48 \pm 3$  d and  $32.9 \pm 2.0$  y, respectively, while in the corresponding neutral atoms the nuclei are stable ( $^{163}\text{Dy}$ ) or live  $10^9$  times longer ( $^{187}\text{Re}$ ).<sup>[49–51]</sup> The study of such processes, however, does not require the primary GF photon beam to drive any nuclear transition, but rather  $\beta$ -unstable ions in the storage ring and control of the electronic states.

Studies of weak decays of highly-charged ions are routinely conducted at GSI in Darmstadt.<sup>[52,53]</sup> However, there are numerous cases of forbidden decays of interest to astrophysics, for which such measurements are not presently feasible at GSI due to insufficient production rates.<sup>[54]</sup> To give just one example,  $^{56}\text{Ni}$  is among the most abundant products in supernova explosions. The half-life of a neutral atom is  $6.075(10)$  d<sup>[55]</sup> and the main decay branch is the Gamow–Teller  $0^+ \rightarrow 1^+$  transition to the 1720.19 keV state in  $^{56}\text{Co}$ . In fully-ionized  $^{56}\text{Ni}^{28+}$  nuclei, the EC decay channel is disabled. Experiments indicate a weak  $\beta^+$  decay branch<sup>[56]</sup> rendering  $^{56}\text{Ni}$  a possible cosmo-chronometer, in contradiction to shell-model predictions.<sup>[57]</sup> The ISOL production method employed at ISOLDE can be superior in providing high-intensity beams of some elements.<sup>[58]</sup> Furthermore, the production yields will be significantly improved within the EPIC project (Exploiting the Potential of ISOLDE at CERN),<sup>[59]</sup> which will facilitate conducting such experiments at the GF.

We now turn to the electromagnetic coupling between atomic and nuclear transitions for decay channels such as internal conversion, bound internal conversion or electronic bridge,<sup>[60]</sup> which are suitable case studies that can take full advantage of the GF. Internal conversion is typically the stronger decay channel of low-lying excited nuclear states, in particular for excitation energies below 60 keV. This in turn means that the lifetimes of such excited states strongly depend on the electronic configuration of the ion, both in terms of available electrons and spin couplings.<sup>[61]</sup> In a pioneering study by Phillips and coworkers, the internal conversion rates for the 14-keV Mössbauer level in  $^{57}\text{Fe}$  were studied in F-like to H-like ions produced as secondary beams in Coulomb excitation. For H-like ions, effects due to conservation of the total spin  $F$  were revealed.<sup>[62]</sup> The investigation of nuclear decays in highly ionized  $^{125}\text{Te}^{44+}$  up to  $^{125}\text{Te}^{48+}$  ions led to the discovery of a new decay mode, bound internal conversion.<sup>[63]</sup>

Studies of the influence of the electron shell on isomer lifetimes are particularly noteworthy since they might provide valuable information about energies and symmetry properties of nuclear states.<sup>[64,65]</sup> Experimental information is presently limited to only a few cases.<sup>[66–71]</sup> In addition, a strong incentive comes from the field of astrophysics, since nucleosynthesis in stellar plasmas proceeds at high temperatures and, therefore, at a high degree of ionization.<sup>[51,72,73]</sup>

With the unique capabilities of the GF, we can design, for the first time, scenarios in which both the nuclear excited states and electronic excited states are populated by the primary laser beam Lorentz-boosted in the reference frame of the accelerated ions. An additional degree of freedom for the experiment is the charge state of the ions. In order to investigate the effects of the atomic shell on nuclear decay lifetimes, PSI with few remaining electrons would be of interest. Nuclear transitions below 60 keV such as those listed in Table 2 could be driven by one laser beam, while a second laser beam could be used to control the electronic shell. For convenience, we provide also the  $K$ -shell and  $L$ -shell internal conversion coefficients, that is, the ratios between the internal

conversion (for the respective electronic shell) and the radiative decay rates, for the transitions listed in Table 2.

Due to low excitation energies and the rather high ionization potentials of the *K*- and *L*-shell electrons, for many of these transitions the respective internal conversion channels are closed; these are indicated with “-” in the last two columns of Table 2. Note that the tabulated internal conversion coefficients are given for neutral atoms and their values are for orientation only. Once a specific charge state is envisaged, dedicated theoretical calculations can provide the correct value of internal conversion rates. There are two possible reasons for differences with the neutral-atom case. First, due to an increase of ionization potentials in PSI, the internal conversion channel may be completely closed. Second, for open shells, spin-coupling effects may change the internal conversion rates as observed in ref. [62].

We also note that although the special cases of the low-lying  $^{229m}\text{Th}$  and  $^{235m}\text{U}$  isomers are well-known for having large internal conversion coefficients for the outer-shell electrons, the corresponding low-charge states are not accessible at the GF which will operate with beams of partially stripped but nevertheless highly charged ions. For example, the internal conversion coefficient for the 8 eV isomeric transition in  $^{229m}\text{Th}$  is  $\approx 10^9$  for the neutral atom,<sup>[64]</sup> but the channel is closed already for  $\text{Th}^+$  ions. From Table 2 we identify interesting cases with large internal conversion coefficients for the *K*- and *L*-shell electrons, which are appealing candidates for future studies at the GF. Focusing on internal conversion coefficients larger than 100, we identify as promising candidates the transitions in  $^{45}\text{Sc}$ ,  $^{73}\text{Ge}$ ,  $^{237}\text{Np}$  (the 33 keV transition),  $^{243}\text{Am}$ , together with almost all listed transitions in Th and U isotopes, and with all listed transitions in Pu and Cm isotopes. For these nuclei, studies at the GF of the dependence of the nuclear excited-state lifetime on the charge state and spin coupling of the electrons would be very interesting.

A different and promising prospect coupling the atomic and nuclear degrees of freedom at the GF involves the so-called electronic bridge process. Thereby the interaction of a nucleus with a photon is mediated by atomic electrons. In the electronic bridge process, the nuclear decay is accompanied by virtual excitation of an electron into a higher bound orbital. The electron then de-excites by photoemission. The process is third-order in quantum electrodynamics (QED), but can nevertheless be the dominant channel for the decay of a nuclear isomer. Electronic bridge processes involving nuclear excitation at the expense of the initially excited electronic shell are sometimes called “inverse electronic bridge,”<sup>[74]</sup> however, many works use the same term for both excitation and decay channels. The electronic bridge may dominate, for example, in low-energy transitions where the hyperfine interaction between the electron and the nucleus is less suppressed by selection rules than the direct gamma-decay, since the photon coupling scales as a lower power of the photon energy. In this case the electrons can act as an effective “bridge” for the interaction, particularly if the resonance condition is met.<sup>[75]</sup>

The electronic bridge has been studied for several nuclear transitions including the 76 eV  $^{235m}\text{U}$  isomer,<sup>[29,74,76,77]</sup> the 8 eV  $^{229m}\text{Th}$  isomer,<sup>[78–85]</sup> and the 3.05 keV nuclear transition starting from the 6<sup>-</sup> 464 keV isomer of  $^{84}\text{Rb}$ .<sup>[86]</sup> Laser-induced electronic bridge has been proposed to determine the excitation energy of the  $^{229}\text{Th}$  isomer in various charge states.<sup>[87–90]</sup> However, to date, the electronic bridge process has not been experimentally observed.<sup>[91]</sup>

The GF provides a new opportunity to explore the electronic bridge process, particularly as a means of driving nuclear excitation. Not only are there many suitable transitions (see Table 2), but one can also tune the charge state of the PSI to optimize the resonance condition for the electronic excitation. As a concrete example we may consider the 2.329 keV nuclear excited state in  $^{205}\text{Pb}$ , which in neutral atoms is an isomer with 24  $\mu\text{s}$  half-life.<sup>[32]</sup> Understanding the decay properties of this state is important for nuclear astrophysics, where a much faster EC-decay is expected to  $^{205}\text{Tl}$  than the 17 My decay of the  $^{205}\text{Pb}$  ground state.<sup>[92,93]</sup> This process affects the very end of s-process nucleosynthesis in the Tl-Bi region.<sup>[94]</sup> Furthermore, since  $^{205}\text{Pb}$  is the only short-lived cosmic radioactivity produced exclusively in the s-process, the evidence for which was found in meteorites, it turns out to be important for constraining cosmochemical simulations.<sup>[95]</sup>

Once the outer N-, O-, and P-shell electrons are stripped off, the internal conversion channel is closed and the decay can only proceed via an *E2* radiative decay, leading to a half-life of  $\approx 3$  h. In PSI, the *M1* electronic fine-structure transition  $2p_{1/2}-2p_{3/2}$  has approximately the same energy as the nuclear transition. Therefore, in suitably chosen PSI, electronic bridge decay paths will open where the  $2p_{1/2}-2p_{3/2}$  transition mediates the nuclear transition. For example, in N-like Pb, the electronic bridge rate will exceed the radiative rate by several orders of magnitude, reducing the lifetime to minutes or seconds, depending on how well the resonance condition is met. This electronic bridge process may be directly observed in the GF by comparing excitation rates in different PSI where the resonant electronic transition is available (such as N-like) against those for which it is not (such as He-like).

## 2.4. Further Experimental Prospects Involving Nuclear Transitions in the Ion Beam

In addition to the aspects discussed so far, several proposals on how to use low-energy nuclear transitions for isomer spectroscopy, laser cooling or production of even higher gamma-ray energies in the secondary beams have been put forward. We shortly address these ideas here.

### 2.4.1. Spectroscopy of Isomers

The fact that the stored ions can be accelerated and decelerated in the storage ring opens the possibility to perform spectroscopy of appropriately long-lived isomeric states using two subsequent photoinduced transitions in a scenario reminiscent of pump-probe spectroscopy. A primary laser with a fixed photon energy is first used. The ion relativistic factor  $\gamma$  is adjusted to excite nuclear transitions which populate a long-lived isomeric state. This could be either a direct transition or excitation of the long-lived isomeric state via intermediate states.

After a sufficient amount of isomeric ions are stored, one can change the relativistic factor of the ions to a different value  $\gamma'$ . At this energy, with the same primary laser, transitions depleting the isomeric state would be driven, and secondary photons detected. This provides a method for performing high-resolution spectroscopy of isomeric states and possible gateway levels around it in a broad range of frequencies, effectively driving ( $\gamma, \gamma'$ ) reactions as the ones discussed in Section 8.2 in the context of



isomer production for medical applications. A limitation is that, with primary-beam photon energies of up to  $\approx 10$  eV, the energy of the laser-driven gamma transitions needs to be below 60 keV. One candidate with an adequate level scheme below this energy is  $^{229\text{m}}\text{Th}$ , for which transitions from the 29 keV level connect to both the isomeric and ground states. With the development of short-wave laser and mirror technologies and/or the advent of the LHC high-energy upgrade, the limitation of 60 keV as maximum photon energy will be overcome, significantly enlarging the set of potential candidates.

We note that detailed studies of isomeric nuclear states are important in the astrophysical context. For example, as discussed, in refs. [96, 97], the properties of long-lived isomers play an important role in setting the abundances of elements produced in astrophysical nuclear reactions.

#### 2.4.2. Laser Cooling with Nuclear Transitions

Cooling via scattering of laser photons near-resonant to gamma transitions in bare nuclei was suggested in ref. [98], where the authors show that reasonable damping times (of less than an hour) can be achieved for several bare ions at the LHC. While laser cooling of PSI using electron transitions is generally much more efficient, laser cooling of bare nuclei may be advantageous for colliding-beam applications to avoid beam losses due to mutual stripping of the colliding PSI beams.<sup>[98]</sup> Candidate transitions for laser cooling can be selected from those listed in Table 2 or from the original proposal in ref. [98].

#### 2.4.3. Production of Higher-Energy Gamma Rays

In principle, the GF concept can be extended to produce photons with much higher energies than 400 MeV that can be generated by scattering conventional laser photons on relativistic PSI. This could be achieved by replacing the optical laser source, which excites the electronic shells of the primary beam, with an X-ray laser source driving nuclear transitions of the relativistic ions. Suitable nuclear resonances include the so-called giant dipole resonances (GDR) which are discussed in Section 4.3. We can envisage an efficient excitation up to nuclear energies of  $\approx 15$  MeV, where the dipole response for stable medium to heavy nuclei exhausts almost 100% of the Thomas–Reiche–Kuhn (TRK) sum rule. Much higher energies would lead to particle loss and reduced radiative decay of the nuclear excitation. In turn, 15 MeV corresponds to  $\approx 2.6$  keV photon energy for the primary beam and  $\approx 87$  GeV photon energy for the secondary beam considering  $\gamma = 2900$ .

X-ray free electron sources such as the LCLS,<sup>[99]</sup> SACLA,<sup>[100]</sup> or the European XFEL<sup>[101]</sup> can easily cover the region of interest of a few keV. In addition, since the GDR is broad, the limited temporal coherence of the X-ray source should not play an important role. The difficulty when envisaging such a setup is that the GF and the X-ray facilities would need to be co-located, which is an obvious limiting factor. This has been so far a major impediment for other proposed combinations of relativistic acceleration and coherent X-ray sources in nuclear quantum optics.<sup>[16–18]</sup> However, this impediment might be solved by using table-top plasma-driven sources.<sup>[102]</sup>

Further opportunities for producing higher-energy gamma rays may be afforded by scattering off relativistic beams of the

secondary photons produced by the GF itself. This is discussed in Section 7.2.

### 3. *P*- and *CP*-Violating Compton Scattering of Primary Photons from Stored Ions

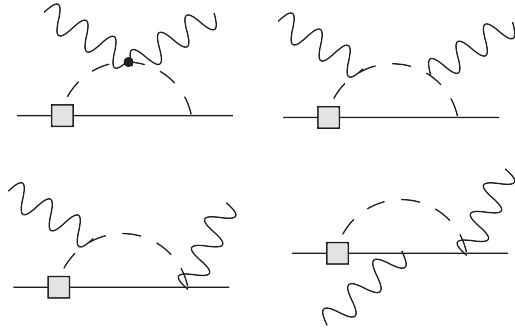
Searching for exotic signatures of violation of symmetry under spatial inversion *P* and time reversal *T* in Compton scattering,  $\gamma(\vec{q}) + N(\vec{p}) \rightarrow \gamma(\vec{q}') + N(\vec{p}')$ , is a natural task for the GF. A clear distinction of the GF (where photons are scattered from stored ion beams) from existing gamma sources based on laser-light backscattering from an electron beam is the possibility to probe specifically hadronic *P*-violating, *T*-conserving (PVTC), and *P*- and *T*-violating (PVTV) interactions.<sup>[103]</sup> The experiment will consist in counting the number of the generated secondary photons as a function of the circular polarization of the primary light.

We start this discussion with the case of the proton beam at the LHC. For the laser-photon energy of  $\approx 10$  eV and the relativistic factor  $\gamma_p \approx 7000$  (approximately double that of the ion beam), the photon energy in the photon-proton c.m. frame of  $\approx 140$  keV can be reached. The theory of Compton scattering on a nucleon at low energies with PVTC was laid out in refs. [104, 105], and the PVTV case was considered in ref. [106]. Long-wavelength photons only interact with the bulk properties of the nucleon: its charge, mass, magnetic moment, and, in the case of a PVTV process, the electric dipole moment (EDM). Additionally, polarizabilities parametrize the response of the internal structure of the nucleon (which also depends on PVTC and PVTV interactions) to a quasistatic electromagnetic field. Peculiar for PVTC and PVTV Compton processes, the effect of polarizabilities dominates over the respective ground-state contribution, the opposite to the case of Compton scattering without symmetry violation.<sup>[106]</sup> This opens up a possibility to search for a new class of PVTV interactions other than those generating the EDM. Disregarding the effects of the nucleon spin for this discussion, the PVTC and PVTV signatures in the Compton scattering process with circularly polarized incoming laser photons are given by the  $\vec{S}_\gamma \cdot (\vec{q} + \vec{q}')$  and  $\vec{S}_\gamma \cdot (\vec{q} - \vec{q}')$  terms, respectively, where  $\vec{S}_\gamma = i\vec{\epsilon}_\lambda(\vec{q}) \times \vec{\epsilon}_{\lambda'}^*(\vec{q}')$  is the photon spin defined in terms of the initial and final photon polarization vectors  $\vec{\epsilon}_\lambda(\vec{q})$  and  $\vec{\epsilon}_{\lambda'}^*$ , respectively. The presence of such PVTC and PVTV terms leads to a single-spin asymmetry<sup>[106]</sup>

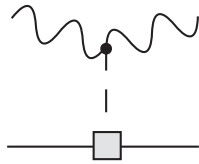
$$A_\gamma \equiv \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = A_\gamma^{\text{PVTC}} \cos^4 \frac{\theta}{2} + A_\gamma^{\text{PVTV}} \sin^4 \frac{\theta}{2} \quad (5)$$

where  $\sigma^\pm$  stands for the differential Compton cross section with left/right circular polarization of the incident photon. Asymmetries  $A_\gamma^{\text{PVTC}}$  and  $A_\gamma^{\text{PVTV}}$  encode the respective polarizabilities. Importantly, both PVTC and PVTV signals arise in the same observable, and the only difference is in its angular dependence. This feature follows from the fact that the *P*-even, *T*-odd vector  $\vec{S}_\gamma$  projects onto either the *P*-odd, *T*-odd combination  $(\vec{q} + \vec{q}')$ , or the *P*-odd, *T*-even combination  $(\vec{q} - \vec{q}')$ , so that the single-spin asymmetry is purely PVTC in the forward direction, purely PVTV in the backward direction, and a mixture of the two in between.

The size of the asymmetry  $A_\gamma$  in Equation (5) depends on the model used to generate  $A_\gamma^{\text{PVTC}}$  and  $A_\gamma^{\text{PVTV}}$ . For the nucleon case,



**Figure 4.** Representative Feynman diagrams responsible for generating PVTC polarizabilities. The square denotes the PVTC pion–nucleon coupling  $h_{\pi}^1$ , while the dotted vertex denotes the two-photon coupling to the pion.



**Figure 5.** The  $\pi^0$ -pole contribution to the PVTV polarizabilities. The square denotes the PVTV pion–nucleon coupling  $\bar{g}_0$ .

the relevant mechanism is due to parity-violating couplings of lightest mesons, most notably the pions.

The diagrams of **Figure 4** yield<sup>[104,105]</sup>

$$A_{\gamma}^{\text{PVTC}} \approx 3 \times 10^{-8} \left( \frac{h_{\pi}^1}{5 \times 10^{-7}} \right) \left( \frac{\omega}{100 \text{ MeV}} \right)^3 \quad (6)$$

where  $\omega$  stands for the c.m. photon energy. A recent measurement of the PV asymmetry in  $\bar{n} + p \rightarrow d + \gamma$  by the NPDGamma collaboration<sup>[107]</sup> obtained

$$h_{\pi}^1 = (2.6 \pm 1.2 \pm 0.2) \times 10^{-7} \quad (7)$$

with the first and second uncertainties being statistical and systematic, respectively. This, together with the maximum energy of 140 keV in this GF setting, makes the PVTC asymmetry on a proton beam too small to be observed.

Similarly, the PVTV pion-nucleon coupling  $\bar{g}_0$  generates PVTV polarizabilities, for example, via  $\pi^0$  exchange as shown in **Figure 5**. This mechanism leads to an estimate<sup>[106]</sup>

$$A_{\gamma}^{\text{PVTV}} \approx \bar{g}_0 \left( \frac{\omega}{m_{\pi}} \right)^2 \quad (8)$$

The natural size of  $\bar{g}_0$  is constrained by the neutron EDM,<sup>[108]</sup>  $\bar{g}_0 \lesssim 10^{-11}$ , so the PVTV asymmetry is also too small to be observed.

To access the PVTC and PVTV signatures via laser backscattering at the GF, we therefore turn our attention to systems in which i) the characteristic energy scale is (ideally) comparable to the c.m. photon energy available, that is, 60 keV for the ion beam, and ii) the natural size of symmetry violation is enhanced by the presence of parity doublets, nearly degenerate pairs of states of opposite parity.<sup>[109]</sup> We denote the average excitation energy of the

parity doublet by  $E_{\text{pd}} \approx E_1 \approx E_2$  and the energy splitting within the parity doublet by  $\Delta E = E_2 - E_1$ . If the typical nuclear energy scale  $E_N \approx 10 \text{ MeV}$  is much larger than this splitting, an enhancement factor  $R \approx E_N / \Delta E \gg 1$  arises, and the expectation for the size of the symmetry-violating asymmetries in the “polarizability regime”  $\omega \leq E_{\text{pd}}$  is

$$A_{\gamma}^{\text{PVTC}} \sim 10^{-8} R \left( \frac{\omega}{E_{\text{pd}}} \right)^3 \quad (9)$$

$$A_{\gamma}^{\text{PVTV}} \lesssim 10^{-11} R \left( \frac{\omega}{E_{\text{pd}}} \right)^2 \quad (10)$$

We list a few known examples of parity doublets in light nuclei in **Table 3**. Given that the photon energy in the center-of-momentum of the laser photon and the stored beam is constrained to be below 60 keV, while the typical nuclear excitations reside at a few MeV, we can still operate in the polarizability regime. The enhancement due to the small energy splitting within a doublet comes in linearly, whereas energy suppression appears quadratically or cubically. Because of this, one should aim at the smallest energy denominator in Equations (9) and (10) making <sup>18,19</sup>F and <sup>21</sup>Ne promising candidates.

Until now, these nuclei were only used for looking for PVTC signals. If a small PVTV component is present additionally to the parity mixing (PV is a prerequisite for PVTV effects), a backward-peaked component will arise. Note that due to a quadratic energy suppression rather than cubic for PVTC, the PVTV signal will have an additional enhancement with respect to the PVTC case, adding to the motivation for looking for such tiny asymmetries.

The longitudinal polarization of the relativistic ions (those that have non-zero spin) will allow to address the spin-dependent PVTC and PVTV polarizabilities. Following ref. [104] for the PVTC case worked out for the polarized proton, we expect the PV longitudinal single-spin asymmetry

$$A_{\text{lon spin}}^{\text{PVTC}} \approx 10^{-8} R \left( \frac{\omega}{E_{\text{pd}}} \right)^2 \quad (11)$$

The lower power of energy in this estimate suggests that if using a polarized ion beam is a viable option the PVTC effects Compton scattering might be easier to access than the photon asymmetry. In contrast, the contribution of PVTV spin polarizabilities to this observable is suppressed by an extra power of the photon energy, and involving the ion spin does not offer better sensitivity to PVTV.

The figure of merit (FOM) is defined as<sup>[110]</sup>

$$\text{FOM} = \text{Rate} \times A^2 \quad (12)$$

and corresponds to the inverse time necessary for an observation of the asymmetry. Above, the rate is proportional to the cross section and fluxes of the colliding particles, and  $A$  denotes the asymmetry. The cross section for low-energy Compton scattering (Thomson scattering) is

$$\sigma = \frac{8\pi}{3} \left( \frac{Z^2 \alpha \hbar}{Mc} \right)^2 \quad (13)$$

**Table 3.** Parameters of the low-lying parity doublets in isotopes of fluorine and neon, from the ENSDF database.<sup>[32]</sup>

Isotope	$T_{1/2}$	$E_1$ [keV]	$I_1^P$	$E_2$ [keV]	$I_2^P$	$\Delta E$ [keV]	$R$	$10^8 A_\gamma^{\text{PVTTC}}$	FOM [ $s^{-1}$ ]
$^{18}\text{F}$ ( $1^+$ )	109.77(5) min	1042	$0^+$	1081	$0^-$	39	256	0.05	$2.5 \times 10^{-8}$
$^{19}\text{F}$ ( $\frac{1}{2}^+$ )	stable	0	$\frac{1}{2}^+$	110	$\frac{1}{2}^-$	110	91	15	$2 \times 10^{-3}$
$^{20}\text{Ne}$ ( $0^+$ )	stable	11255	$1^-$	11258	$1^+$	3.2	3125	$5 \times 10^{-4}$	$2.5 \times 10^{-22}$
$^{21}\text{Ne}$ ( $\frac{3}{2}^+$ )	stable	2789	$\frac{1}{2}^+$	2795	$\frac{1}{2}^-$	5.7	1754	0.02	$4 \times 10^{-9}$

Here  $Z$  and  $M$  are the charge and mass of the ion. The cross section is  $\sigma \approx 3 \mu\text{b}$  for the case of  $^{19}\text{F}$ . The event rate is obtained as a product of the laser photon rate of  $N_\gamma \approx 10^{25} \text{ s}^{-1}$ , number of ions per bunch  $N_{I/b} \approx 10^{10}$  (see Table 1), and the ratio of the process cross section  $\sigma$  to the cross section of the laser beam  $S \approx (20 \mu\text{m})^2$

$$\text{Rate} = N_{I/b} \times N_\gamma \times \frac{\sigma}{S} \approx 10^{11} \text{ s}^{-1} \quad (14)$$

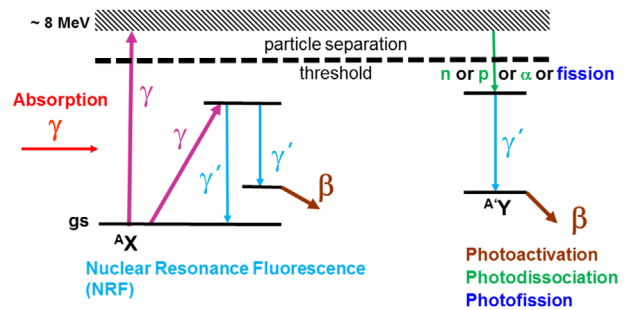
Here we assume that the time structure of the laser pulses is matched to that of the ion bunches. Numerical estimates of the FOM for the four ions under consideration are summarized in Table 3. These results indicate that a promising candidate nucleus is  $^{19}\text{F}$ , for which a 10% measurement of the asymmetry can be achieved with a day of statistics accumulation.

A final note in this section concerns the background not associated with symmetry-violating effects. Final-state interaction (FSI) due to electromagnetic rescattering will generate a non-zero phase of the Compton amplitude if even a tiny linear polarization component  $P$  is present, leading to a false asymmetry due to a correlation  $\vec{S}_\gamma \cdot [\vec{q} \times \vec{q}']$ . In ref. [106] this background was estimated as  $A_\gamma^{\text{FSI}} \approx \alpha \frac{\omega^2}{M_N^2} P \sin^2 \theta \cos 2\phi$ . The maximal degree of misalignment of circular polarization of laser photons can reasonably be assumed to be  $P \leq 10^{-6}$ , and for  $\omega \leq 60 \text{ keV}$  the false asymmetry should be small. The modulation with the azimuthal angle  $\phi$  can be used to further suppress this undesired background: when integrated over the full  $2\pi$  range, this non-symmetry-violating background drops out of the asymmetry. The above estimate relies on the assumption that the photon energy lies below the inelastic threshold. For  $\omega \leq 60 \text{ keV}$  this requirement suggests that a fully stripped ion beam has to be used to avoid that atomic excitations and interferences thereof mimic the PVTTC or PVTV signatures. An additional PVTV-type correlation may be generated by FSI on top of a PVTTC signature. We expect this effect at the level  $10^{-5}$  of PVTTC or smaller.

The experiment at the GF will entail measuring the flux of secondary photons depending on the circular polarization of the laser photons. The detector will have to be  $2\pi$ -symmetric in order to eliminate the  $\cos 2\phi$ -modulated electromagnetic background.

#### 4. Nuclear Physics with GF Secondary-Photon Beam on Fixed Targets

This section addresses the opportunities provided by the GF secondary beam for nuclear spectroscopy and hadron physics in the energy range from a few to hundreds of MeV. A wide variety of targets can be used in conjunction with the GF secondary beam,



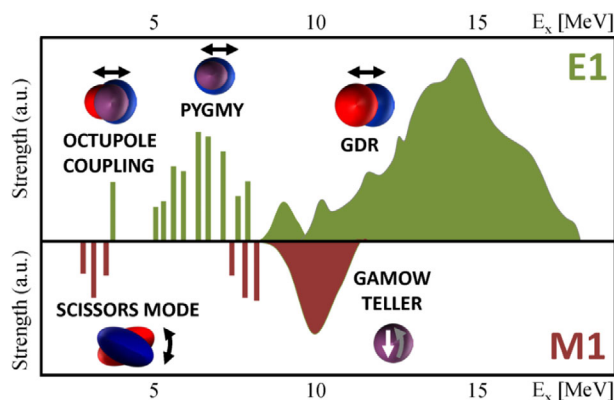
**Figure 6.** Possible photonuclear reactions following the absorption of a photon provided by the GF: excitation below the particle separation threshold will allow for nuclear spectroscopy via nuclear resonance fluorescence (NRF), potentially followed by  $\beta$  decay (photoactivation). Excitation into the continuum above the particle-separation threshold will be followed by photodissociation (i.e., emission of neutrons, protons, or  $\alpha$  particles) or by photofission.

benefiting from the vast experience and infrastructure at CERN. Apart from stable or long-lived nuclear species, unique opportunities to use rare radioactive elements may be opened by the close physical proximity to the ISOLDE,<sup>[111]</sup> one of the world's leading sources of radioactive nuclides. Further opportunities may be rendered possible by a dedicated storage ring for rare isotopes discussed in Section 6.

Perhaps the most obvious application of the GF is nuclear spectroscopy, which will benefit from the narrow spectral bandwidth achievable with collimated GF photons, their energy tunability, and high intensities. **Figure 6** displays a schematic overview of possible photonuclear reaction pathways following the absorption of an impinging photon. Nuclear spectroscopy experiments have been performed since the advent of betatron particle accelerators and Schiff's seminal paper from 1946,<sup>[112]</sup> proposing to use electron bremsstrahlung (converted from energetic electron beams) to detect nuclear resonance fluorescence (NRF) off bound excited nuclear states. NRF is discussed in Section 4.1 on gamma spectroscopy of narrow resonances at the GF.

As indicated in Figure 6, in parallel to NRF, deexcitation of an intermediate level may proceed not directly toward the ground state of the excited nucleus, but via  $\beta$  decay to a daughter nucleus (photoactivation). Alternatively, an excitation into the continuum above the particle-separation threshold will lead to subsequent deexcitation via particle emission (neutrons, protons,  $\alpha$  particles), hence to photodissociation, addressed in more detail in Section 4.4 or to photofission, discussed in Section 4.5.

In **Figure 7**, possible strong (electric and magnetic) dipole excitations in heavy, deformed nuclei are schematically shown as a function of their excitation energy. We concentrate on dipole



**Figure 7.** Illustration of the photoresponse of deformed atomic nuclei as a function of the photon energy, divided into phenomena involving electric ( $E1$ ) and magnetic ( $M1$ ) excitations. Figure by A. Zilges.

excitations since at the few MeV energies of interest, the gamma-ray wavelength is much larger than the nuclear size. On the magnetic dipole ( $M1$ ) side, at lower energies, the orbital magnetic dipole excitation corresponds in a simplistic geometric, macroscopic picture to a scissors-like vibration of the deformed proton and neutron fluids against each other.<sup>[113]</sup> Therefore this  $M1$  mode is referred to as the ‘scissors mode’, the magnetic analogue of the GDR. We further discuss the importance of these transitions in the context of the GF in Section 4.1. At higher energies of  $\approx 10$  MeV, Gamow–Teller (GT) transitions<sup>[114]</sup> appearing as  $M1$  excitation strength are related to the common weak-interaction processes of spin–isospin-type ( $\sigma\tau$ , i.e., a product of the spin and isospin operators) in atomic nuclei. These are of interest not only in nuclear physics, but also in astrophysics; they play an important role in supernovae explosions and nucleosynthesis.<sup>[115–117]</sup>

On the electric dipole ( $E1$ ) side of Figure 7, the GDR represents a collective excitation mode where protons and neutrons vibrate against each other along or perpendicular to the symmetry axis of the nucleus. The double-humped structure of the GDR in deformed nuclei appears typically at energies of around  $77 \cdot A^{-1/3}$  MeV ( $A$  is the mass number), which corresponds to about 14 MeV in rare earth nuclei. This isovector GDR was initially found as a spectral feature corresponding to the excitation of the nuclear ground state, but soon Brink and Axel concluded that giant resonances could be associated with any nuclear state, independent of the microscopic structure of this state.<sup>[118,119]</sup> This led to intense studies of GDR properties of excited states, the so-called GDR in hot nuclei.<sup>[120]</sup> Further prospects of GF studies of the GDR and potential multiphoton excitation are presented in Section 4.3.

In addition, enhanced electric dipole excitations are expected at lower excitation energies. Several experimental studies using electromagnetic probes have found an enhancement of electric dipole strength between about 5 and 10 MeV. This phenomenon is denoted as pygmy dipole resonance (PDR) and has been intensively studied in recent years.<sup>[121–128]</sup> In a simplified geometrical picture, the PDR is described as neutron skin oscillating against a  $N = Z$  core. The PDR phenomenon is discussed in more detail in Section 4.2.

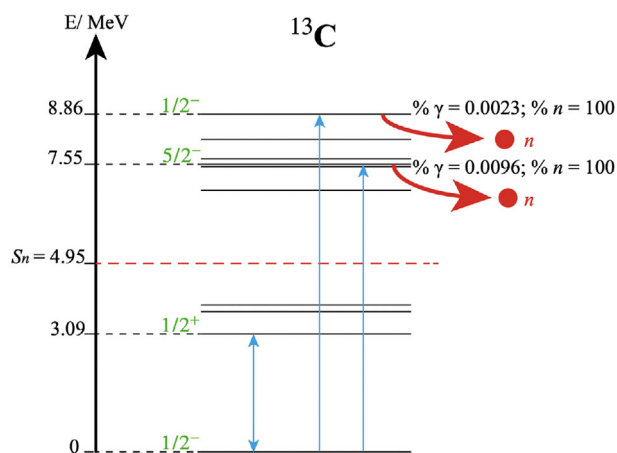
Moving toward even higher secondary-beam energies, and toward hadron physics, the second part of the section goes beyond traditional gamma spectroscopy to address Compton and photo-induced processes on light nuclei in Section 4.7, pion photoproduction in Section 4.8, and the Delta-resonance region and continuum effects in Section 4.10. The section concludes with prospects of more exotic processes at the GF involving parity-violation in Section 4.11.

#### 4.1. Narrow Resonances

Narrow resonances in a wide energy range up to the particle-separation threshold are the subject of NRF. Resonance fluorescence in general refers to the resonant excitation of an upper state by absorption of electromagnetic radiation and decay of the excited level by emission of radiation. Via NRF, nuclear states are excited in photon-scattering experiments and their deexcitation through electromagnetic transitions is studied via gamma-ray spectroscopy.<sup>[113,129]</sup> From these experiments, photoabsorption cross sections and the related photon strength functions<sup>[130,131]</sup> are deduced, which are important for the description of photonuclear reactions and the inverse radiative-capture reactions.

In NRF experiments, the nucleus is excited by the absorption of a real photon. As these photons only carry a small angular momentum, excitation favors transitions where the change of the nuclear angular momentum is small. The strongest transitions are typically of dipole character ( $E1$  or  $M1$ ). The excited states may subsequently decay either directly or via intermediate lower-lying states back to the ground state. The latter transitions are typically weak and difficult to resolve from the background when using energetically continuous (broadband) bremsstrahlung. Therefore, for example, the determination of the total transition width  $\Gamma$  is not always possible with bremsstrahlung beams. An alternative way to perform NRF experiments uses quasi-monochromatic photon beams as provided by existing or upcoming Compton-backscattering facilities<sup>[132,133]</sup> and in the future by the GF.

In general, for all nuclear shapes where the centers of mass and charge do not coincide, one expects an electric dipole moment leading to enhanced electric dipole transitions. Examples are deformed shapes due to octupole deformations or any kind of cluster configurations. Rotations on top of the octupole vibrations coupled to the quadrupole deformed core lead to the so-called octupole vibrational bands. In spherical nuclei close to magic proton or neutron shells the lowest-lying excitations are quadrupole and octupole vibrations of the nuclear shape. A coupling of these two single-‘phonon’ excitations leads to a two-phonon quintuplet with spins  $J^\pi = 1^- - 5^-$ . The  $1^-$  member of this multiplet can, in principle, be excited via an electric dipole transition from the ground state in NRF experiments. The energies of all these dipole excitations ( $E1$  and  $M1$ ) lie in the same range of roughly 2–4 MeV, see also Figure 7. This emphasizes the crucial necessity for parity assignments for the interpretation of observed excitations. NRF is by far the most sensitive tool to detect such dipole excitations and to (model independently) determine their characteristics: excitation energies, spins, parities, decay energies, level widths, lifetimes, decay branchings, multipole mixing ratios, and absolute transition strengths.



**Figure 8.** Nuclear energy levels below 8.86 MeV in  $^{13}\text{C}$ . Energies,  $J^P$  and decay modes<sup>[55]</sup> are given for the levels discussed in this work. The arrows show excitation to be induced by the secondary GF photons. For the lowest-energy gamma resonance, the double-sided arrow indicates that the only decay channel is via photon emission.

There are many specific examples of transitions that can be studied at the GF taking advantage of its monochromaticity, tunability and unsurpassed photon flux. An interesting case is the one of  $^{13}\text{C}$ , which exhibits many accessible resonances displayed in the partial level scheme in **Figure 8**. The case of  $^{13}\text{C}$  will be discussed in the context of polarimetry with narrow resonances in Section 10.1. The interesting neutron emission channels at 7.55 and 8.86 MeV can be selectively excited by the GF and used in turn to generate tertiary monoenergetic fast neutron beams. This topic is the subject of Section 12.5.

Another interesting case is the longest lived ( $\tau_{1/2} \gtrsim 1.2 \cdot 10^{15}$  y) isomer  $^{180m}\text{Ta}$  lying 77 keV above a short-lived ground state (see also Table 9). This isomer has been extensively studied in order to understand its decay mechanisms via photoexcitation to a gateway level above the isomer,<sup>[134]</sup> following the scheme presented in Section 2.1. Previous experiments<sup>[135]</sup> using broadband bremsstrahlung radiation could neither identify the gateway levels nor could they provide information about the involved transition probabilities. The high flux and excellent monochromaticity of the GF secondary beam could finally shed light on this matter.

Finally, we note that scattering of linearly polarized photons on unpolarized or spin-zero nuclei is an effective method to determine the parity of excited nuclear states, see, for example, ref. [136]. The advantage of the GF for such studies is the ability to resolve relatively narrow resonances combined with high statistical sensitivity and tunability of the photon energy.

#### 4.2. Pygmy Dipole Resonances

The dipole response for stable (medium to heavy) nuclei with a moderate neutron excess is almost entirely concentrated in the giant dipole resonance (GDR) that exhausts almost 100% of the TRK sum rule (which is proportional to the energy-weighted sum rule).<sup>[137,138]</sup> For this collective excitation, the nuclear ( $N - Z$ ) asymmetry and the corresponding symmetry energy provide the restoring force for the oscillation between the excess neutrons

against the ( $N = Z$ ) nuclear core.<sup>[139]</sup> Thus only a minor part of the  $E1$  strength is expected at lower excitation energies.

The electric dipole strength distribution at low energies (below  $\approx 5$  MeV) is dominated by multi-phonon excitations originating from the coupling between  $J^\pi = 2^+$  quadrupole and  $J^\pi = 3^-$  octupole vibrations of the nuclear shape, being the lowest single-phonon excitations in even-even nuclei near closed neutron or proton shells. The two-phonon excitations  $2^+ \otimes 3^-$ , called quadrupole–octupole coupling, lead to a multiplet consisting of five states with spins and parities  $J^\pi = 1^-, \dots, 5^-$ . In photon-scattering experiments, the  $1^-$  member of the  $2^+ \otimes 3^-$  multiplet can be excited selectively by an  $E1$  transition from the ground state. Its subsequent decay is predominantly back to the ground state via an  $E1$  transition.<sup>[140]</sup>

At energies between 5 MeV and a few hundred keV above the neutron-separation threshold, an enhancement of dipole strength was observed in many semi-magical and magical nuclei.<sup>[121]</sup> It was found that the  $E1$  dipole strength at energies below the GDR range is of the order of 1% of the TRK sum for stable nuclei, and up to about 5% for the exotic nuclei studied so far.<sup>[123]</sup> Owing to its relatively low strength, this low-lying  $E1$  transition is often denoted as the pygmy dipole resonance (PDR). The first PDR observation was made by Bartholomew in 1961 who found enhanced gamma-ray emission after neutron capture.<sup>[141]</sup> The PDR name was coined in 1969, when its impact on calculations of neutron-capture cross sections was reported.<sup>[142]</sup> In 1971, Mohanet et al. proposed a description of the PDR in a three-fluid hydrodynamical model.<sup>[143]</sup> One interpretation is an oscillation of excess neutrons (the neutron skin) against the  $N = Z$  core. The PDR is of great interest because it provides information on the neutron skin and on the nuclear symmetry energy as a crucial ingredient to the nuclear matter equation-of-state.<sup>[144]</sup> On theoretical grounds, employing the relativistic quasiparticle random phase approximation (RQRPA) approach, a one-to-one correlation was found between the pygmy dipole strength and parameters describing the density dependence of the nuclear symmetry energy, and in turn with the thicknesses of the neutron skin.<sup>[145]</sup>

As discussed in ref. [139], the determination of the neutron radius of a heavy nucleus, that is, its neutron distribution, is a fundamental problem related to the equation-of-state of nuclear matter with far-reaching consequences in areas as diverse as atomic PV,<sup>[146,147]</sup> nuclear structure,<sup>[148–152]</sup> heavy-ion collisions,<sup>[153–157]</sup> and neutron-star structure.<sup>[158–162]</sup> Hence, the far-reaching impact of understanding the  $E1$  strength distribution of the PDR motivated still ongoing extensive experimental and theoretical studies in a wide mass range.<sup>[121,123–126,128,163–168]</sup> In a recent work at GSI,<sup>[166]</sup> PDR were studied in a chain of chromium isotopes, see **Table 4**.

As photon scattering is a key experimental technique to study the  $E1$  dipole strength in nuclei, and in particular the PDR, an intense and high-quality (i.e., monoenergetic) photon beam as envisaged for the GF would turn out highly beneficial for this active research field.

#### 4.3. GDR and Multiphoton Excitation

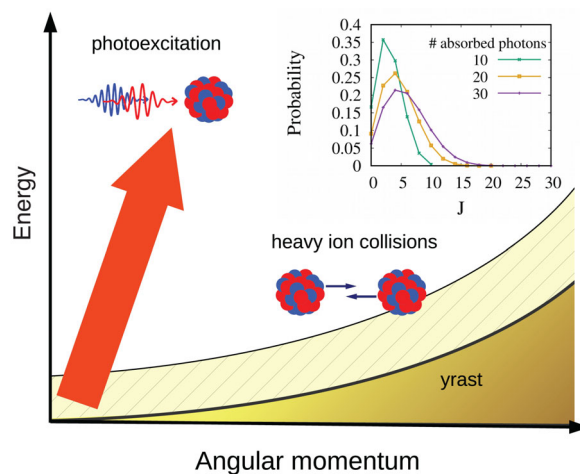
The high photon flux in the GF secondary beam can be used at photon energies of 10–20 MeV to excite the GDR in

**Table 4.** Examples of isotope chains. Isotopes in the table have half-lives longer than 1 h.<sup>[55]</sup>

${}^Z X$	Isotopes A: abundance and/or $T_{1/2}$
${}_{24}\text{Cr}$	48: 21.6 h, 50: 4.34% $\geq 1.3 \times 10^{18}$ y, 51: 27.7 d, 52: 83.8%, 53: 9.50%, 54: 2.36%
${}_{50}\text{Sn}$	110: 4.11 h, 112: 0.97% $\leq 1.3 \times 10^{21}$ y, 113: 115 d, 114: 0.66%, 115: 0.34%, 116: 14.5%, 117: 7.68%, 118: 24.2%, 119: 8.59%, 120: 32.6%, 121: 27.0 h, 122: 4.63%, 123: 129 d, 124: 5.79% $\geq 1.2 \times 10^{21}$ y, 125: 9.64 d, 126: $2.30 \times 10^5$ y, 127: 2.10 h
${}_{62}\text{Sm}$	142: 72.5 m, 144: 3.07%, 145: 340 d, 146: $10.3 \times 10^7$ y, 147: 15.0% $1.06 \times 10^{11}$ y, 148: $11.2\% 7 \times 10^{15}$ y, 149: 13.8%, 150: 7.38%, 151: 90 y, 152: 26.8%, 153: 46.3 h, 154: 22.8%, 156: 9.4 h
${}_{66}\text{Dy}$	152: 2.38 h, 153: 6.4 h, 154: $3.0 \times 10^6$ y, 155: 9.9 h, 156: 0.056%, 157: 8.14 h, 158: 0.095%, 159: 144 d, 160: 2.33%, 161: 18.9%, 162: 25.5%, 163: 24.9%, 164: 28.3%, 165: 2.33 h, 166: 81.6 h
${}_{70}\text{Yb}$	164: 75.8 m, 166: 56.7 h, 168: 0.123%, 169: 32.0 d, 170: 2.98%, 171: 14.1%, 172: 21.7%, 173: 16.1%, 174: 32.0%, 175: 4.18 d, 176: 13.0%, 177: 1.91 h, 178: 74 m

medium-mass and heavy nuclei. In a shell-model picture the GDR is a superposition of particle–hole excitations out of the ground state and is not an eigenstate of the nuclear Hamiltonian. These particle–hole excitations actually do not all have the same energy, leading to a spreading of the GDR often referred to as Landau damping.<sup>[169,170]</sup> The residual two-body interaction mixes the particle–hole excitations with each other and with other shell-model configurations and, thus, spreads the GDR over the eigenstates of the nuclear Hamiltonian. This leads to a Lorentzian distribution of the dipole strength with a so-called “spreading” width  $\Gamma^\downarrow$  of around 5 MeV.<sup>[171,172]</sup> Ground-state deformation in axially-symmetric deformed nuclei leads to a splitting of the GDR Lorentzian into two components. The GDR spectrum, with its strength, centroid, and Lorentzian parametrizations thus offer information on the nuclear shape,<sup>[173]</sup> and in addition, on the nuclear size, the nuclear symmetry energy (important for the study of neutron-star structure) and the viscosity of the neutron and proton fluids.<sup>[174]</sup> In a time-dependent picture, the spreading of the GDR over nuclear eigenstates can be viewed as statistical equilibration<sup>[175]</sup> with a characteristic time scale  $\hbar/\Gamma^\downarrow$ .

According to the Brink–Axel hypothesis, the GDR is a mode of excitation not only of the nuclear ground state, but of any excited state as well.<sup>[118,119]</sup> GDRs built on excited states are termed “hot GDRs” and have so far been produced in heavy-ion collisions leading to fusion or incomplete fusion.<sup>[120]</sup> As a result of the collision, a compound nucleus is formed, that is, a highly excited nucleus in which the excitation energy is distributed over several or many particle-hole excitations.<sup>[175]</sup> Heavy-ion collisions involve large angular momenta, leading to high angular momentum states in the compound nucleus. Completely new prospects would be opened by the possibility to reach the same excitation energies by multi-photon absorption. Absorption of a dipole photon transfers one unit of angular momentum. The total angular momentum in a multiple dipole absorption process typically increases with the square root of the number of absorbed photons.<sup>[176]</sup> Multiple dipole absorption would therefore lead to excitation of the compound nucleus at high energy and at comparatively low angular momentum, far above the yrast line, as



**Figure 9.** Qualitative illustration of two regimes of nuclear excitation. The yrast line defines the minimum energy of a nuclear state with a certain angular momentum. Heavy-ion collisions preferentially excite states close to the yrast line (region depicted by hatched area). Multiple absorption of multi-MeV dipole photons involves small transfer of angular momentum and could lead to compound states several hundred MeV above yrast (red arrow). The inset shows the angular-momentum distributions for  $N_0 = 10, 20$  and 30 absorbed dipole photons starting from an initial state with  $J = 0$ . Adapted with permission.<sup>[176]</sup> Copyright 2014, American Physical Society.

illustrated in **Figure 9**. The spectral region of high excitation energy and small angular momentum is so far mostly unexplored. Little is known experimentally in that region about state densities, the widths of the GDRs, decay properties of highly excited states, and, specifically, about the nuclear equilibration process.

The identification of  $\hbar/\Gamma^\downarrow$  with the equilibration time becomes questionable at high excitation energy well above particle threshold. For example, hot GDRs<sup>[120]</sup> are characterized by high neutron-evaporation rates and have correspondingly short lifetimes.<sup>[177]</sup> Neutron evaporation may happen prior to complete equilibration. The increase of the GDR width due to neutron evaporation then does not correspond to a shorter equilibration time. Such increase is considered to be one of the possible reasons for the damping of the hot GDR.<sup>[120,177,178]</sup> Sokolov and Zelevinsky confirmed the interpretation of ref. [177] and attributed the disappearance of the collective GDR strength observed experimentally to the complex interplay between internal and external dynamics with decay into the continuum.<sup>[179]</sup> A different explanation postulating an increase of the spreading width with temperature was also put forward.<sup>[180]</sup>

Due to its large width, the GDR can in many cases be investigated with broadband gamma sources. In the following we identify special cases for which the high photon flux and/or monochromaticity of the GF may be of advantage.

First, the high photon flux would be beneficial for the study of GDR excitations in exotic nuclei far from the valley of stability. Due to their short lifetime, such targets are bound to produce small excitation yields and are hard to access experimentally. A notable exception is the PDR and GDR measurement of the neutron-rich unstable  ${}^{68}\text{Ni}$  nucleus.<sup>[181]</sup> Nuclear gamma spectroscopy on the GDR at the GF could bring new insights into the shapes and properties of exotic nuclei.

Second, the GF will enable photofission studies of fission isomers in actinides. A nuclear reaction such as (d,p) or fragmentation would produce highly deformed excited states in the second minimum of the fission barrier. Photoabsorption would excite the GDR built upon these states. The high photon flux and in particular the monochromaticity of the GF would allow for photofission studies of these strongly deformed actinides with a much better sensitivity than so far available to the fission barrier landscape. This is the subject of Section 4.5.

Finally, one may consider the possibility of multiple absorption of dipole photons, where for instance a second absorbed photon excites a GDR built upon the GDR reached by the first photon. As shown in ref. [182], a comparison of single and multiple GDRs could probe statistical aspects of the resonance width, exhibiting either a Lorentzian or Gaussian shape. For the focused laser pulses envisaged at the Nuclear Pillar of the Extreme Light Infrastructure in Bucharest,<sup>[183]</sup> with pulse durations of tens of zeptoseconds ( $1 \text{ zs} = 10^{-21} \text{ s}$ ), theoretical studies based upon the Brink–Axel hypothesis predict multi-photon absorption of up to approximately hundred photons. This would lead to excitation energies in the range of several 100 MeV, to multiple neutron evaporation and to the formation of neutron-deficient nuclei far from the valley of stability.<sup>[176,184–186]</sup> In comparison, focusing of the secondary beam does not appear to be feasible at the GF and the envisaged pulse durations are many orders of magnitude longer. Thus, even the probability of two-photon excitation remains small at the GF.

#### 4.4. Photonuclear Response above Particle Threshold

The excitation-energy region around the particle-separation threshold is, on the one hand, of interest from a theoretical perspective because the coupling of bound quantum states to the continuum of unbound states requires an extended formalism, which is particularly intricate for exotic nuclei near the drip-lines where all structures are weakly bound.<sup>[187]</sup> On the other hand, this energy region covers the Gamow-window of thermally driven reactions of nucleons with heavy nuclei. Its understanding is a prerequisite for modeling nuclear-reaction cascades in hot cosmic objects and thus for understanding nucleosynthesis. Below the threshold, all excited resonances decay predominantly by gamma-ray emission, with rare cases of  $E0$  transitions involving internal conversion or electron–positron pair production.

In this regime, the knowledge of the nuclear level densities and the gamma-ray strength function is of crucial importance as an ingredient, for example, to model nuclear-reaction-network calculations of nucleosynthesis. From an experimental perspective, the so-called “Oslo method” was established as a reliable tool to derive these properties from measured gamma-ray energy spectra. The Oslo method comprises a set of analysis techniques designed to extract the nuclear level density and average gamma-decay strength function from a set of excitation-energy tagged gamma-ray spectra. The method was first introduced in ref. [188] and since then continuously further developed.<sup>[189]</sup> Recently a new software implementation of the method was provided.<sup>[190]</sup>

Above the threshold, the particle-decay channel opens up. Either no gamma rays can be observed at all or their intensity cannot be used as a measure of the total electromagnetic excita-

tion strength of the resonance due to the unknown particle-decay branching ratio. An intense narrow-energy-band photon beam will open up new horizons for investigation of nuclear photo-response at and above the separation threshold.<sup>[191]</sup>

##### 4.4.1. Neutron-Capture Cross Sections of S-Process Branching Nuclei

Cosmic nucleosynthesis of heavy elements above the so-called iron peak mainly proceeds via neutron-capture processes; the r process (r: rapid neutron capture) is connected to scenarios of high neutron densities well above  $10^{20} \text{ cm}^{-3}$  and temperatures on the order of  $2\text{--}3 \times 10^9 \text{ K}$  as occurring in explosive scenarios such as, for example, supernovae or neutron-star mergers.<sup>[72,192]</sup> In contrast, average neutron densities during s-process nucleosynthesis (s: slow neutron capture) are rather small ( $\approx 10^8 \text{ cm}^{-3}$ ), that is, the neutron capture rate  $\lambda_n$  is normally well below the  $\beta$ -decay rate  $\lambda_\beta$  and the reaction path is close to the valley of  $\beta$  stability.<sup>[193–195]</sup> However, when the s-process reactions occur at peak neutron densities, reaction path branchings occur at unstable isotopes with half-lives as low as several days. The half-lives at these branching points are normally known with high accuracy, at least under laboratory conditions. One relies on theory for the extrapolation to stellar temperatures;<sup>[196]</sup> the neutron-capture cross sections are accessible to direct experiments only in special cases. Besides the limited availability of sufficient amounts of target material, intrinsic activity of the target hinders experimental access especially in the case of branching points involving isotopes with short half-lives. Moreover, the predictions in the Hauser–Feshbach statistical model yield different results depending on the underlying parameter sets. Additionally, studies of branching points involving long-lived isotopes (e.g.,  $^{147}\text{Pm}$ ,  $^{151}\text{Sm}$ ,  $^{155}\text{Eu}$ ) showed that the recommended values of neutron-capture cross sections in the Hauser–Feshbach statistical model<sup>[197]</sup> differ by up to 50% from the experimentally determined values.<sup>[198]</sup> Therefore, further and precise experimental constraints on the theoretical predictions of these crucial values are needed. The inverse ( $\gamma, n$ ) reaction could be used at the GF to determine optimized model-input parameters for improved predictions.

##### 4.4.2. ( $\gamma, p$ ), ( $\gamma, \alpha$ ) Cross Sections for P-Process Nucleosynthesis

In the framework of cosmic nucleosynthesis, ‘p-nuclei’ are certain proton-rich, naturally occurring isotopes of some elements which cannot be produced in either slow (s-process) or rapid (r-process) neutron-capture processes. In the seminal paper by Burbidge, Burbidge, Fowler, and Hoyle ( $B^2FH$ ),<sup>[199]</sup> accompanied by,<sup>[200]</sup> the s- and r-processes for the production of intermediate and heavy nuclei beyond iron were introduced. It was immediately realized by the authors of both papers that a number of proton-rich isotopes can never be synthesized through sequences of only neutron captures and  $\beta^-$  decays. This required the postulation of a third process. It was termed p-process, because it was thought to proceed via proton captures at high temperature, however, later findings shed doubts on the feasibility to use proton captures for producing all of the nuclides missing from the s- and r-process mechanisms. In the literature, “p-process” is

sometimes used as a general term denoting whatever production mechanism(s) is/are found to be responsible for the p-nuclides. Historically, there were 35 p-nuclides identified, with  $^{74}\text{Se}$  being the lightest and  $^{196}\text{Hg}$  the heaviest.<sup>[201]</sup> Compared to the bulk of natural isotopes, p-nuclei generally show abundances which are 1-2 orders of magnitude lower. Photodisintegration rates, like  $(\gamma, n)$ ,  $(\gamma, p)$ , and  $(\gamma, \alpha)$  play a crucial role in the nucleosynthesis of these nuclei. As the p-reaction network calculations comprise several hundred isotopes and the corresponding reaction rates, theoretical predictions of these rates, normally obtained in the framework of the Hauser–Feshbach statistical model theory,<sup>[202]</sup> are necessary for the modeling. The reliability of these calculations should be tested experimentally for selected isotopes.

While the  $(\gamma, n)$  cross sections in the energy regime of the GDR around 15 MeV were measured extensively already several decades ago (see, for example, ref. [203]), many efforts using continuous bremsstrahlung spectra have been made<sup>[204–206]</sup> to determine the reaction rates without any assumptions on the shape of the dependence of the cross section on energy in the astrophysically relevant energy region just above the reaction threshold. Also laser Compton backscattering to produce monoenergetic photon beams was used to determine reaction rates by an absolute cross section measurement.<sup>[207]</sup> In contrast, experimental knowledge about the  $(\gamma, p)$  and  $(\gamma, \alpha)$  reactions in the corresponding astrophysical Gamow energy window is much more scarce. In fact, the experimental data are based on the observation of the time reversal  $(p, \gamma)$  and  $(\alpha, \gamma)$  cross sections, respectively<sup>[208–211]</sup> for the neutron-deficient nuclei with mass numbers around 100. Therefore, being able to measure these rates directly would represent a significant progress. It should be noted that deeper insight into the p-process nucleosynthesis would not emerge from the measurement of only a few selected reactions, but via the development of a comprehensive database. This necessitates rather short individual measurement times for studying the stable p nuclei despite their typically low natural abundances.<sup>[212]</sup> This will only become possible using intense  $\gamma$  beams as will be provided by the VEGA facility at ELI-NP and, ultimately, by the GF.

However, the majority of nuclides in the p-process network calculations are radioactive. Here, the access to stored secondary beams at the GF, see Section 6, will enable a unique possibility to investigate photo-induced reactions on short-lived species. Furthermore, direct  $(p, \gamma)$  and  $(\alpha, \gamma)$  reactions can be as well studied by employing in-ring, pure, thin, gaseous  $\text{H}_2$ , and He targets.<sup>[213,214]</sup> In this way, direct and reverse reactions can be measured for the same pairs of nuclides, thus enabling immediate testing of Hauser–Feshbach calculations.

#### 4.4.3. Direct Measurement of Astrophysical S-Factors

Helium burning in stars, as has been realized at the dawn of nuclear astrophysics,<sup>[199]</sup> is the key process to understanding the abundances of chemical elements in the universe. This process proceeds via the triple- $\alpha \rightarrow ^{12}\text{C}$  reaction, enhanced by the Hoyle resonance,<sup>[215]</sup> and followed by the  $\alpha$  radiative capture on carbon,  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ . The rate of the former process at stellar temperatures is known to  $\approx 10\%$ . In turn, a  $\approx 100\%$  uncertainty in the rate of the latter reaction represents the main source of uncer-

tainty in stellar evolution models. A direct measurement of the rate of the  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$  reaction at astrophysical energies is considered “the holy grail” of nuclear astrophysics, but is extremely challenging. The radiative process is rare due to the weakness of the electromagnetic force, and may be suppressed by 3–6 orders of magnitude with respect to other processes (e.g., elastic scattering).

Attempts to measure the inverse process generalized to a virtual-photon-induced disintegration  $^{16}\text{O}(e, e'\alpha)^{12}\text{C}$  showed the possibility to access this process experimentally,<sup>[216]</sup> albeit no satisfactory agreement of theoretical predictions with the data was achieved. There is a revived interest in studying this process at electron-scattering facilities.<sup>[217,218]</sup> While one wins in the rates due to high intensity of electron sources, the price to pay are electromagnetic background processes and the necessity to extrapolate to the real photon point. At GSI, Coulomb dissociation of a 500 MeV per nucleon  $^{16}\text{O}$  beam colliding with a Pb target is used to address this reaction. This is an extremely challenging experiment. Apart from tiny reaction rates at low center-of-mass energies, the dissociation products have nearly identical magnetic rigidities,<sup>[219]</sup> making it hard to separate them. Moreover, recent studies<sup>[220]</sup> concluded that the most promising method to study  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$  is via the inverse reaction. The GF will allow to directly study the  $^{16}\text{O}(\gamma, \alpha)^{12}\text{C}$  photodisintegration process avoiding the aforementioned complications.

To be of direct use for understanding stellar nucleosynthesis, measurements at the GF should be done close to the energy relevant to the helium-burning conditions in stars, where the ignition plasma temperature is  $T \approx 2 \cdot 10^8$  K. The kinetic energy of the  $\alpha$  particle corresponding to the astrophysics-relevant Gamow window is  $E_\alpha \approx 300$  keV. The respective threshold for the (inverse) photodisintegration process  $^{16}\text{O}(\gamma, \alpha)^{12}\text{C}$  is  $E_\gamma^{\text{th}} \approx 7.6$  MeV. For comparison, the competing proton-knockout reaction threshold lies at  $\approx 11.6$  MeV.

#### 4.4.4. Alpha Clustering in Heavy Nuclei

Although alpha clustering in light nuclei is well known and the famous Hoyle state in  $^{12}\text{C}$  plays an important role in the evolution of the Universe, there are many open questions concerning the physics of clusterization in nuclei.<sup>[221]</sup> Even the geometrical structure of the most clusterized nuclei, such as  $^6\text{He}$  in the ground state and  $^{12}\text{C}$  in the Hoyle state (and higher similar states), is still under debate. In the case of  $^6\text{He}$ , one critical feature is the correct prediction of the  $\beta$ -decay to  $^6\text{Li}$  that is sensitive to the details of the wavefunction of  $^6\text{He}$ . The case of  $^8\text{He}$  is also important as its size is somewhat smaller than that of  $^6\text{He}$  due to the pressure of outer neutrons.

Much less is known concerning the alpha clustering in heavier nuclei. At the Budker Institute of Nuclear Physics (Novosibirsk), more than 30 years ago, an experiment with a super-thin nuclear jet target crossing the electron beam in a storage ring<sup>[222]</sup> at electron energy  $E_e = 130$  MeV demonstrated a significant cluster component in the double magic  $^{16}\text{O}$  nucleus. There were observed various cluster-decay channels, with the final states in  $^{12}\text{C}$ ,  $^8\text{Be}$ , and four alpha particles. These promising experiments were discontinued and this storage ring does not exist anymore. Also the electron-ion scattering experiment ELISe, aiming at reaction



studies on stored short-lived nuclides, is significantly delayed at FAIR.<sup>[223]</sup>

A series of experiments on alpha clustering in heavier nuclei were performed at Jyväskylä with alpha scattering from heavy nuclei.<sup>[224]</sup> This reference is the latest detailed publication on the experiment with  $^{36}\text{Ar} + \alpha$  at 150 MeV energy. There is a systematic accumulation of collective states, like cluster of cluster states with the same spin going from  $^{16}\text{O}$  all the way to  $^{40}\text{Ca}$ . In the shell-model language, such states are regular combinations of many selected states from higher shells. The only currently available picture is that of a quasicrystal structure where the analogs of crystal bands, probably overlapping, are formed built on alpha constituents. The bands are split by alpha tunneling as electron bands in normal crystals.

The study with gamma rays of high energy and therefore appropriate wavelength, a distant relative of X-ray diffraction from crystals, can shed light on this structure that has no analogs in other nuclear phenomena. The  $(\gamma, \alpha)$  and possibly also  $(\gamma, 2\alpha)$  reactions,<sup>[225]</sup> studied as a function of photon energy and polarization can provide unique information concerning specific features of alpha-clusterization, especially in even-even  $N = Z$  nuclei.<sup>[226]</sup>

The development of nuclear physics away from the stability band brought to the experimental light such exotic nuclei as those in vicinity of  $^{100}\text{Sn}$ , the heaviest double magic nucleus with  $N = Z$ . Here, there are indications of alpha structure continuing up to such heavy systems. This should be a regular part of the equilibrium nuclear structure in distinction to alpha decay of superheavy elements. There are various arguments in favor of the existence of such a substructure including the quadrupole collective states in heavier tin isotopes, in spite of the absence of valence protons in this shell according to the primitive shell-model scheme. Especially characteristic are extremely strong alpha decays of nuclei near  $^{100}\text{Sn}$ .<sup>[227]</sup> The decay of  $^{105}\text{Te}$  to  $^{101}\text{Sn}$  is one of the strongest alpha decays in the whole periodic chart, with a half-life of only 620 ns.<sup>[228]</sup> This is comparable to the 229 ns half-life of  $^{212}\text{Po}$  which is just a bound state of the alpha particle and the core of  $^{208}\text{Pb}$ . The strongest known  $\alpha$  decay of  $^{104}\text{Te}$  to  $^{100}\text{Sn}$  has an upper limit half-life of only 18 ns.<sup>[227]</sup> A detailed study of alpha structures in heavy nuclei would also be a driving force for the development of corresponding theory (some directions are outlined in ref. [226] as the nuclear analog of the transition between the Bardeen–Cooper–Schrieffer picture of superconductivity and boson condensation).

#### 4.4.5. Fano Effect in Nuclear Gamma Spectroscopy

The Fano effect,<sup>[229]</sup> well known in atomic and molecular physics, is a characteristic asymmetric spectral lineshape that arises due to the interference of the resonant and nonresonant transition amplitudes in the vicinity of a resonance. In nuclear physics, the Fano effect was studied, for example, in  $^{15}\text{N}(^7\text{Li}, ^7\text{Be})^{15}\text{C}$ <sup>[230]</sup> and  $d(^9\text{Li}, ^{10}\text{Li})p$ <sup>[231]</sup> reactions. However, to the best of our knowledge, the Fano effect has not as yet been observed in nuclear gamma transitions. A loosely related experiment<sup>[232]</sup> on X-ray interference with  $^{57}\text{Fe}$  Mössbauer nuclei observed Fano interference in the X-ray reflectivity of thin-film cavities around the nuclear resonance energy. However, in that case the nonresonant channel

was given by the electronic scattering of the cavity, while only the resonant channel was stemming from the driving of the nuclear Mössbauer transition.

A study of nuclear Fano resonances via photoexcitation was proposed in the context of three-body Efimov states.<sup>[233]</sup> Photoabsorption on the ground state of  $^{20}\text{C}$  ( $\tau_{1/2} \approx 16$  ms) should be sensitive to the presence of the  $n+^{19}\text{C}$  and  $n+n+^{18}\text{C}$  states embedded in the  $^{20}\text{C}$  continuum and display Fano resonances around the respective energies.<sup>[234]</sup>

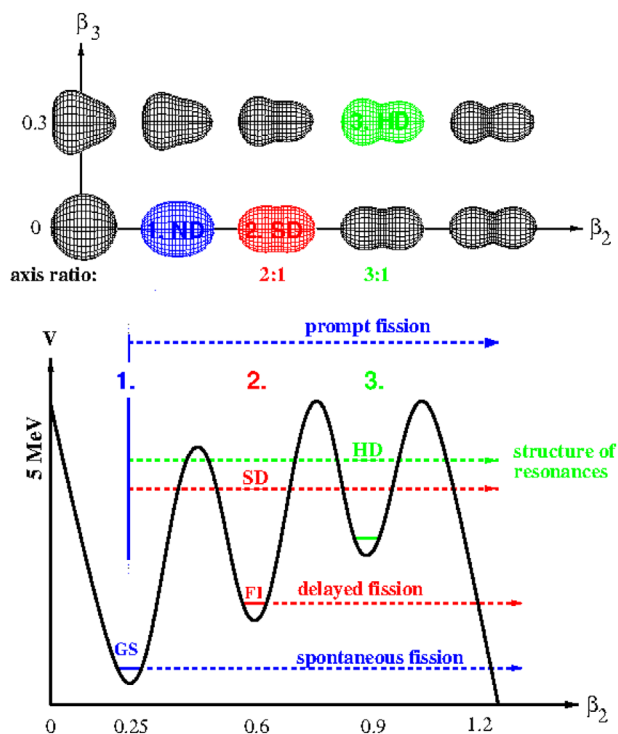
With tunable narrow-band gamma rays from the GF, one can envision a systematic study of Fano interference in the vicinity of nuclear gamma transitions, for example the ones in  $^{13}\text{C}$  discussed in Appendix B.

#### 4.5. Photofission with Monochromatic Gamma Beams

Photofission measurements enable selective studies of extremely deformed nuclear states in light actinides and can be utilized to better understand the landscape of the multiple-humped potential energy surface in these nuclei. The selectivity of these measurements originates from the low amount of angular momentum transferred during the photoabsorption process. Studies of fission isomerism in the actinide mass region provided evidence already in the 1960s for the existence of a second, minimum of the potential energy surface<sup>[235]</sup> corresponding to superdeformation (SD), with a ratio of 2:1 between the long and short principal axes of the strongly deformed nuclear shape, parameterized as a rotational ellipsoid. This corresponds to a value of  $\beta_2 \approx 0.7$  of the quadrupole-deformation parameter in the nuclear surface parameterization in terms of a spherical harmonic multipole expansion. Three decades later also the existence of a hyperdeformed (HD) third minimum of the fission barrier (axis ratio 3:1,  $\beta_2 \approx 0.9$ , octupole deformation  $\beta_3 \approx 0.3$ ) could be established (see review articles<sup>[236,237]</sup>). The lower part of **Figure 10** illustrates such a triple-humped fission barrier (expressed by the potential energy as a function of the nuclear quadrupole deformation  $\beta_2$ ).

Spectroscopic information on the properties of these extremely deformed nuclear states was obtained for the superdeformed second minimum via direct decay studies (conversion electron and  $\gamma$  spectroscopy) and isomeric (delayed) fission, while for the third minimum, transmission-resonance spectroscopy was performed, analyzing resonances in the prompt fission probability. **Figure 11** displays the fission barrier of  $^{236}\text{U}$  (left) and, in the right part, the related prompt fission cross section with transmission resonances.<sup>[238]</sup>

While direct decay spectroscopy is limited to the second minimum (due to the thin outer barrier of the third well and thus too short decay lifetimes compared to fission) and to an excitation-energy range up to about 1.5 MeV above the SD ground state, transmission resonance spectroscopy in the third minimum probes the energy region of about 1–1.5 MeV below the barrier top. Thus the intermediate range of excitation energies between 3.5 and 4.5 MeV (representing the region of the second and third vibrational phonon) remained so far inaccessible to high-resolution studies that could have provided deeper insight, for example, into the harmonicity of the nuclear potential at these extreme deformations. Instead, early photofission studies in actinides performed with bremsstrahlung photons with an



**Figure 10.** Schematic overview of the multiple-humped fission barrier in light actinide isotopes together with the corresponding nuclear shapes. Lower part: cut through the potential energy surface along the fission path, revealing - besides the normal deformed (ND) first minimum with the nuclear ground state (GS) - a superdeformed (SD) second minimum at an axis ratio of 2:1 (with a fission isomer (FI) as its ground state) and a hyperdeformed (HD) third minimum at an axis ratio of 3:1. In the upper part the corresponding nuclear shapes are displayed as a function of the quadrupole and octupole degrees of freedom. Reprinted with permission.<sup>[237]</sup> Copyright 2002, Elsevier.

effective energy bandwidth of about  $\Delta E = 200\text{--}300$  keV revealed the existence of a so-called “isomeric shelf” in the photofission cross section of  $^{238}\text{U}$  in this energy region, as visible below the sharp bend at  $\approx 4.5$  MeV in **Figure 12a**.<sup>[239]</sup> This isomeric shelf is interpreted as the result of a competition of prompt and delayed (isomeric) fission, following the  $\gamma$  decay to the isomeric ground state. Due to the high selectivity of the  $(\gamma, f)$  reaction in terms of spin and parity, only  $1^-$  and  $2^+$  states are formed following the absorption of  $E1$  and  $E2$  multipolarity, respectively. Therefore, **Figure 12a** shows an analysis of the experimental data in terms of quadrupole and dipole contributions, exhibiting a dominant  $1^-$  component for the isomeric shelf.

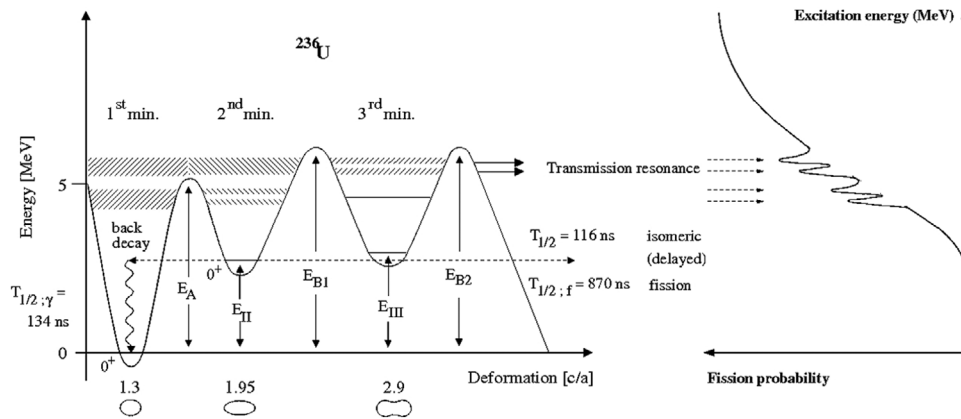
While the photon bandwidth achievable with bremsstrahlung limits the spectral resolution as shown for the existing data in **Figure 12b**, using narrow-bandwidth photons of the monochromatized beam from the GF could allow resolving a resonance structure underlying the isomeric shelf, as illustrated in **Figure 12c**. The resonance positions and strengths are based on tentative findings of an early photofission experiment with limited resolution,<sup>[240]</sup> that could conclusively be performed with the envisaged high-resolution photon beam of the GF.

Candidates for photofission studies at the GF are illustrated in **Figure 13**. For  $^{232}\text{Th}$  and  $^{238}\text{U}$  these plots show an expected triple-

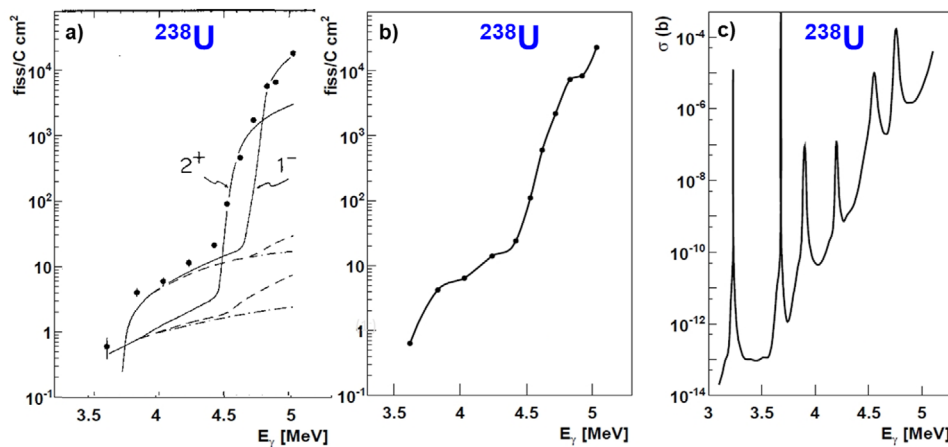
humped fission barrier structure as a function of the quadrupole deformation  $\beta_2$ . For a long time only a shallow third potential minimum was assumed to exist, until it could be demonstrated for  $^{234}\text{U}$ ,<sup>[241]</sup>  $^{236}\text{U}$ ,<sup>[238]</sup> and  $^{232}\text{U}$ ,<sup>[242]</sup> that the outer third minimum is in fact as deep as the second minimum. This also leads to a new interpretation of early photofission data, where a fine structure in the 6.0 MeV resonance of  $^{232}\text{Th}$  was measured by Zhang et al.<sup>[243,244]</sup> In view of our improved knowledge on the triple-humped barrier we have to conclude that in these measurements in fact the depth of the third well instead of the second minimum was determined. For  $^{238}\text{U}$  also the potential landscape based on a triple-humped fission barrier is drawn. For a long time, photofission in  $^{238}\text{U}$  was only studied via measurements using bremsstrahlung, where resonances could not be resolved, and with a weak tagged-photon beam of 100 keV bandwidth resulting in low-statistics resonances reported by Dickey and Axel.<sup>[245]</sup> The early  $^{236}\text{U}(t, pf)$  (pf here indicates that a proton is emitted before the residual nucleus undergoes fission) measurements by Back et al.<sup>[246]</sup> show several pronounced transmission resonances between 5 and 6 MeV, while a whole sequence of further (yet unresolved) transmission resonances at lower energies is expected to explain the isomeric shelf.<sup>[239]</sup>

Using a brilliant photon beam for photofission studies on strongly deformed actinides will provide many advantages compared to the experimental approach pursued over decades and lead to a renaissance of photonuclear physics in general and photofission in particular. So far the potential energy surface of actinides was mapped via particle induced reactions like  $(d, pf)$ ,  $(d, tf)$  or  $(^3\text{He}, df)$ , resulting in a statistical population of states<sup>[202]</sup> in the second and third potential well. In these cases, the typical population probability amounts to  $10^{-4}\text{--}10^{-5}$ , equivalent in typical experimental scenarios to about one isomeric fission event per second. Therefore only strong resonances with resonance strengths  $\sigma\Gamma \approx 10$  eVb could be studied, in the vicinity of a strong background from prompt fission. When using a monochromatic  $\gamma$  beam with a spectral density of about  $10^4\text{--}10^6 \gamma \text{ eV}^{-1} \text{ s}^{-1}$ , the spin selectivity of the photonuclear reaction together with the narrow energy bandwidth of  $< 10^{-3}$  would result in a strongly increased isomeric fission rate of  $10^2\text{--}10^6$  isomeric fission events per second. Moreover, due to the almost complete absence of background from prompt fission, clean spectra would emerge, granting access also to weak resonances with  $\sigma\Gamma \approx 0.1$  eVb and widths from about a few 100 eV to 100 keV.

Using a monochromatized  $\gamma$  beam with  $\Delta E/E \approx 10^{-6}$  would provide a  $\gamma$ -beam linewidth approaching the thermal Doppler broadening limit of about 5 eV at  $E_\gamma = 5$  MeV for heavy nuclei of  $A \approx 240$  at 300 K, thus enabling a new era of photofission studies with the GF: exploring the fission barrier landscape of actinides would enable tests of macroscopic–microscopic nuclear models with unprecedented sensitivity, allowing, for example, to improve the input to astrophysical nucleosynthesis reaction-network calculations. High-resolution  $\gamma$  spectroscopy of nuclear configurations at large deformations could be used to study Nilsson orbitals with energies decreasing as a function of nuclear deformation. In the Nilsson-orbital framework, such studies will provide information on the structure of (less deformed) superheavy elements. Dynamical aspects of the fission process could be revisited with much improved sensitivity to angular, mass and charge distributions. Finally, also



**Figure 11.** Left part: The triple-humped potential-energy surface of  $^{236}\text{U}$ . Also damped compound nuclear states in the normal deformed (ND) first, superdeformed (SD) second, and hyperdeformed (HD) third potential minima are shown as hatched areas. For strongly mixed ND and SD states, transmission resonances of HD states can occur as visible in the prompt fission probability shown in the right part. Reprinted with permission.<sup>[238]</sup> Copyright 2005, Elsevier.



**Figure 12.** a) Photofission yield for  $^{238}\text{U}$  as a function of the excitation energy: experimental data (full symbols) and  $2^+$  and  $1^-$  contributions from model calculations (labeled solid lines).<sup>[239]</sup> b) Photofission yield data from (a) (solid line to guide the eye) as accessible with bremsstrahlung photons of an effective bandwidth  $\Delta E \approx 300$  keV. c) Expected photofission yield of  $^{238}\text{U}$  when using a  $\gamma$  beam of  $\Delta E/E \approx 10^{-6}$ , based on resonances tentatively reported in an early photofission experiment with limited resolution.<sup>[240]</sup> Adapted with permission.<sup>[239]</sup> Copyright 1983, Springer.

applications of the fission process would benefit from such high-quality photofission studies, for example, from the understanding of strong  $E1$  resonances as doorway states to fission in order to better understand and optimize the mechanisms of minor actinide transmutation in nuclear waste treatment (see also Section 14.2).

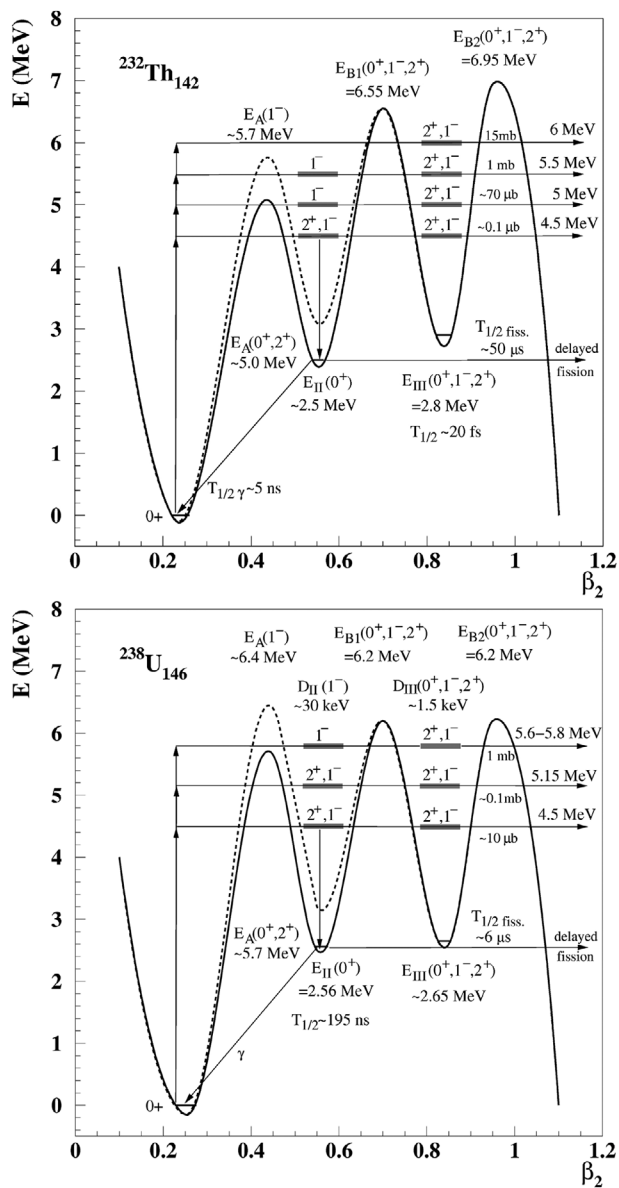
Another application of nuclear photofission, considered also for the ELI-NP facility,<sup>[248]</sup> is measurement of magnetic moments of isomeric states of neutron-rich nuclei.

#### 4.6. Odd Harmonics in Angular Distribution of Fission Fragments

Odd harmonics in angular distribution of fission fragments appear due to interference of the fission amplitudes from nuclear states of opposite parity. They may appear due to mixing of opposite-parity nuclear states by the weak interaction or, in the

case of neutron-induced fission, due to population of opposite-parity states by capture of neutrons in s- and p-waves. In the case of photofission, opposite parity states may be populated by the capture of  $E1$  and  $M1$  or  $E2$  photons. Observation of odd harmonics requires separation of light and heavy fission fragments ( $A_{\text{fragment}} < A/2$  and  $A_{\text{fragment}} > A/2$ ).

For many years it was believed that observation of odd harmonics is impossible because of the large number of final states of the fragments (fragments are formed in excited internal states) so that any interference effect should average out, see for example, the classic nuclear physics book by Bohr and Mottelson.<sup>[249]</sup> However, pioneering work by the Danilyan group and others<sup>[109,250–253]</sup> discovered that the parity violating correlation  $\vec{\sigma} \cdot \vec{p}_1$  is not suppressed in the neutron-induced fission (here  $\vec{\sigma}$  is the neutron spin and  $\vec{p}_1$  is the light-fragment momentum), it is actually about  $10^{-4}$ , that is, it is enhanced by three orders of magnitude relative to the ratio  $10^{-7}$  of the weak to strong interactions in nuclei.



**Figure 13.** Triple-humped potential energy landscape for  $^{238}\text{U}$  (top) and  $^{232}\text{Th}$  (bottom) as a function of the quadrupole deformation  $\beta_2$ . The solid lines show a parameterization in the harmonic model, where potential barriers and minima are described by joint parabolas. The dashed curves represent the spin-dependent barriers for dipole ( $1^-$ ) and quadrupole ( $2^+$ ) excitations, differing at the inner but degenerate at the middle barrier.<sup>[247]</sup> Expected transmission resonances in various potential wells are indicated with their energies, spins and cross sections. For  $^{232}\text{Th}$  extrapolated partial lifetimes for delayed fission and ( $\gamma$ ) back decay are also indicated.

The theory of this phenomenon was developed in refs. [109, 254, 255]. Interference between opposite-parity amplitudes is not suppressed since the orientation of the strongly deformed nucleus is produced before the separation of the fragments due to mixing of the doublet of the opposite-parity rotational states. The enhancement of PV happens at the initial stage due to mixing of very close opposite-parity states in the spectrum of compound resonances which are formed after neutron capture. Earlier it had

been assumed that this mixing is “forgotten” during the complicated fission process and does not appear at the final fission stage. Indeed, it is the case where temporal description of the fission process is applicable, with different stages of fission separated in time. However, there is an uncertainty relation between the energy resolution and time resolution,  $\delta E \delta t \gtrsim \hbar$ . To temporally separate different stages of fission, we need a large energy spread  $\delta E$ . For the case of nearly monochromatic thermal neutrons ( $\delta E \approx T \ll D$  where  $T$  is neutron temperature and  $D$  is the distance between the compound resonances), we have all components of the nuclear wavefunction present simultaneously, the time dependence is given by a common factor  $\exp(-iEt/\hbar)$ . As a result, the mixed-parity compound state contains also the mixed rotation doublet in the strongly deformed nucleus before the separation of the fragments. The details of the corresponding calculations may be found in refs. [109, 255].

Odd harmonics in fission may also appear due to the interference of  $s$ - and  $p$ -wave neutron capture resulting in the correlations  $\vec{p}_n \cdot \vec{p}_l$  and  $\vec{\sigma} \cdot (\vec{p}_n \times \vec{p}_l)$ , where  $\vec{p}_n$  is the neutron momentum.<sup>[109]</sup> The correlation  $\vec{\sigma} \cdot (\vec{p}_n \times \vec{p}_l)$  has been observed with the predicted magnitude.

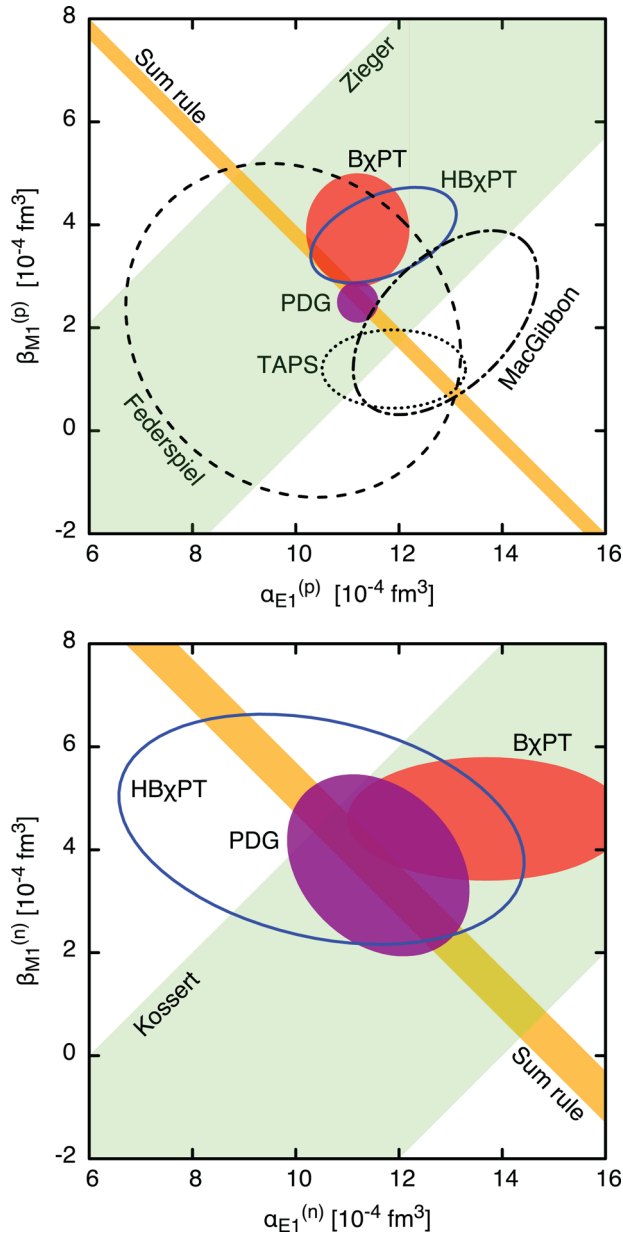
The GF allows us to investigate both parity violating and parity conserving odd harmonics in photofission. The corresponding theory is presented in ref. [256]. The variable spread of the photon energies will allow investigation of the transition from small  $\delta E$  regime, where odd harmonics are not suppressed, to the “lost-memory” regime where there is a suppression by a factor of  $\sqrt{\delta E/D}$ . The explanation of this suppression factor is simple: the number of compound states captured in the interval  $\delta E$  is  $N \approx \delta E/D$ , the amplitudes of the fission from different compound states have random signs, so the effect is suppressed by  $\sqrt{N}$ .

#### 4.7. Photoinduced Processes on the Proton and Light Nuclei

Low-energy Compton scattering off the proton  $p(\gamma, \gamma')p$  and light nuclei (namely, deuteron or helium), is traditionally used to measure the nucleon polarizabilities, see the recent reviews.<sup>[257–260]</sup> The present status of the dipole electric ( $\alpha_{E1}$ ) and magnetic ( $\beta_{M1}$ ) polarizabilities of the proton and neutron is shown in **Figure 14**. The GF could improve upon the latest measurements at the operating photon-beam facilities (HI $\gamma$ S and MAMI) given its broader energy range, high energy resolution, and photon flux. Nucleon polarizabilities enter as input to precision atomic physics, most notably, spectroscopy of muonic atoms.<sup>[261]</sup> Better precision of the polarizability measurements would reduce the current uncertainties in atomic calculations.<sup>[262–264]</sup>

Compton scattering above the pion-production threshold provides better sensitivity to polarizabilities compared to the case of lower energies. In addition, a strong correlation between the values of nucleon polarizabilities and the properties of nucleon excited states, in particular, the ratio of the electric quadrupole to magnetic dipole  $E2/M1$  strengths at the  $\Delta(1232)$  resonance has been observed.<sup>[257]</sup> The Delta resonance is discussed further in Section 4.10.

The optical theorem, in conjunction with other general principles such as micro-causality, fully determines the amplitude of forward Compton scattering in terms of integrals of



**Figure 14.** Plot of  $\alpha_{E1}$  versus  $\beta_{M1}$  for the proton (upper panel) and neutron (lower panel). The orange band represents the latest Baldin sum-rule evaluation.<sup>[265]</sup> “PDG” denotes the latest Particle Data Group summary. Other references can be found in ref. [259].

photoabsorption cross sections.<sup>[266]</sup> For example, the spin-independent forward Compton scattering amplitude,  $f(\nu)$ , as function of the photon energy  $\nu$ , is given in terms of total photoabsorption cross section,  $\sigma(\nu)$ , as

$$f(\nu) = -\frac{(Ze)^2}{M} + \frac{2\nu^2}{\pi} \int_{\nu_\pi}^{\infty} d\nu' \frac{\sigma(\nu')}{\nu'^2 - \nu^2} \quad (15)$$

where the first term is the classical Thomson amplitude characterized by the ratio of the target charge and mass, and the lower integration limit reads  $\nu_\pi = m_\pi(1 + m_\pi/2M)$ , with  $m_\pi$  the pion

mass. Expanding this expression in powers of  $\nu/m_\pi$  yields a number of useful sum rules; first of all, the Baldin sum rule for the sum of dipole polarizabilities<sup>[267]</sup>

$$\alpha_{E1} + \beta_{M1} = \frac{1}{2\pi^2} \int_0^{\infty} d\nu \frac{\sigma(\nu)}{\nu^2} \quad (16)$$

Our current knowledge of the empirical cross sections, by means of this sum rule, provides stringent constraints on the nucleon polarizabilities, as shown by the yellow band in Figure 14.

Similar considerations for spin-dependent Compton scattering lead to the Gerasimov–Drell–Hearn (GDH) sum rule<sup>[268,269]</sup> which relates the anomalous magnetic moment  $\kappa$  of a particle of spin  $S$  and mass  $M$  to an energy-weighted integral over the spin-dependent photoabsorption cross section via

$$I^{\text{GDH}} \equiv \int_0^{\infty} \frac{d\nu}{\nu} [\sigma^{\text{P}}(\nu) - \sigma^{\text{A}}(\nu)] = 4\pi^2 \kappa^2 \frac{\alpha}{M^2} S \quad (17)$$

where  $\sigma^{\text{P}}$  ( $\sigma^{\text{A}}$ ) stands for the photoabsorption cross section with circularly polarized photons and the target polarization parallel (antiparallel) to the photon momentum, respectively. The GDH sum rule was shown to hold exactly for the electron, order by order in QED.<sup>[270,271]</sup> For the nucleon, a perturbative QCD calculation is not helpful, but the comparison has been done based on the measured helicity-dependent cross section  $\sigma^{\text{P}} - \sigma^{\text{A}}$ .<sup>[272]</sup> For the proton, the result for the r.h.s. is  $I_p^{\text{GDH}} \simeq 204 \mu\text{b}$  ( $1 \text{ b} = 10^{-24} \text{ cm}^2$ ), to be compared to the l.h.s. value  $205(21) \mu\text{b}$  based on the empirical cross section.<sup>[273]</sup> Likewise, for the neutron  $I_n^{\text{GDH}} = 233 \mu\text{b}$  is comparable to the sum-rule evaluation:  $229.3(5.6)(4.0) \mu\text{b}$ .<sup>[274]</sup>

For the case of the deuteron the empirical verification of the GDH sum rule is much more delicate. The deuteron anomalous magnetic moment is small,  $\kappa_d \simeq -0.143$  (compared to proton  $\kappa_p \simeq 1.79$  and neutron  $\kappa_n \simeq -1.91$ ), leading to a tiny sum-rule value,  $I_d^{\text{GDH}} = 0.65 \mu\text{b}$ . This small sum rule value implies an almost complete cancellation of the contributions from the hadronic range  $\approx I_p^{\text{GDH}} + I_n^{\text{GDH}}$  versus the near-threshold photodisintegration  $\gamma d \rightarrow pn$ . At present, an account for all channels leads to  $I_d^{\text{h.s.}} = 27.3 \mu\text{b}$ , deviating from the sum-rule expectations. Recent experimental data at photon energies between the breakup threshold and 10 MeV from HI $\gamma$ S,<sup>[275]</sup> while compatible with the sum rule, feature a significant uncertainty.

The spin asymmetry of deuteron photodisintegration<sup>[276]</sup> as well as pion photoproduction on the deuteron is of great interest not only in view of the GDH sum rule but also in view of a sensitive test of present day theoretical models, although we are not aware of any measurements of the beam-target spin asymmetry in the  $d(\gamma, p)n$  reaction.

A polarized deuteron (spin-1) contains polarized proton and neutron. Absorption of a circularly-polarized photon is only possible in an antiparallel helicity configuration, whereas only scattering (a Compton process suppressed by one power of  $\alpha$ ) is possible in the parallel configuration. The threshold for photodisintegration of the deuteron is 2.22 MeV, the maximum is reached around 5 MeV. A 100% asymmetry is expected. Nuclear effects are not expected to play a significant role; in addition, they are calculable in chiral effective field theories.<sup>[277]</sup>

In general, polarization observables offer sensitive tests of the theoretical understanding.<sup>[278]</sup> For example, the polarization of the outgoing neutron  $P_\gamma(n)$  in  $d(\gamma,n)p$  at low energies shows a discrepancy between the theory and existing data.

#### 4.8. Pion Photoproduction

Several main directions in contemporary nuclear science are addressing problems related to astrophysics and investigating weakly bound nuclei at the limit of nuclear stability. Such nuclei usually have a neutron halo or other weakly bound external nucleons.<sup>[279–281]</sup> Loosely bound nuclei have been studied by electroinduced two-nucleon knockout.<sup>[282]</sup> Several new approaches can be envisaged for the future GF. One approach is to use photoexcitation with variable gamma energy at wavelength comparable to the size of the exotic orbitals. Ideally, one would perform a series of  $(\gamma, NN)$  experiments on a sequence of isotopes from stable to exotic that could provide a “photo image” of the evolution of valence orbitals as a function of the mass number. Another related image can be derived from pion photoproduction with the registration of the pion and emitted nucleons on a series of such isotopes. One can expect that pion production on such nuclei will have a component similar to this process on a free nucleon.

Investigation of  $(\gamma, \pi)$  reactions is one of the rare techniques to probe the wavefunction of loosely bound nucleons, for example by the difference of pion production from the halo and from normal strongly bound isotopes. The idea is to check how the  $\pi$  production depends on the isospin asymmetry of the nucleus. The  $(\gamma, \pi)$  cross section at several hundred MeV scales with the atomic weight  $A$  approximately as  $A^\alpha$  dependence with  $\alpha \approx 2/3$ ,<sup>[283]</sup> close to what one might expect for an incoherent surface effect.  $\pi$  production on the proton and deuteron is well studied, and this reaction on a free neutron is known with a minimal model dependence, providing reference for measurements on other systems. The targets of interest are the long chains of stable isotopes in Sn, Yb, Sm, and Dy, Table 4. We note that the isotopic dependence of atomic PV was recently measured in the Yb isotopic chain.<sup>[284]</sup>

##### 4.8.1. Photoproduction of Bound $\pi^-$

Secondary photons at the GF which have highly tunable energy and narrow width obtained by proper collimation provide a unique opportunity to realize resonance photoproduction of pionic atoms. It is realized through the reaction  $\gamma + n \rightarrow p + \pi^-$  inside a nucleus, that is



where  ${}^A_{Z_i}X$  and  ${}^A_{Z'}X'$  are the initial and final nucleus, respectively (both in their nuclear ground state<sup>[285]</sup>),  $Z_i$  and  $Z = Z_i + 1$  are the corresponding atomic numbers,  $A$  is the number of nucleons which is the same for the initial and final nucleus, and  $l$  is the orbital angular momentum of the bound pion.

Estimates of total widths of bound  $ns$  states in pionic atoms, the effective photoproduction cross section of the initial nucleus, dominant contributions to photon-attenuation background, maximal photoproduction rate  $p_{\max}$  of pionic atoms with atomic numbers  $Z$  up to 92, and suggested tuning of the photon-energy

spread are presented in ref. [286]. These estimates indicate that  $p_{\max}$  can reach up to  $\approx 10^{10}$  atoms  $s^{-1}$ , which offers orders-of-magnitude improvement compared with other production methods, for example, producing pionic atoms by capturing free pions as in Ref. [287], where  $\approx 10^5$  pionic helium atoms  $s^{-1}$  are produced at a 590 MeV proton facility.

For the estimates presented in ref. [286], cross sections for producing free pions with final nuclei in the ground state are needed. While there exist such experimental data for light nuclei,<sup>[288–292]</sup> we are not aware of such data for heavy nuclei. There are studies of charged-pion photoproduction from heavy nuclei<sup>[293–295]</sup> using bremsstrahlung-photon beams and radiochemical measurements, where the measured cross section corresponding to the final nucleus in the ground state actually include contributions of decays from excited states. To measure the cross section for producing free pions with final nuclei in the ground state, monochromaticity of the GF photons would be useful, especially for heavy nuclei where the energy difference between the nuclear ground state and the first excited state is typically smaller than in light nuclei. We can tune the energy of the narrow-band gamma rays at the GF precisely so that excited nuclear states cannot be produced. These cross section data would be invaluable for estimating the rates of bound-pion photoproduction discussed in this section.

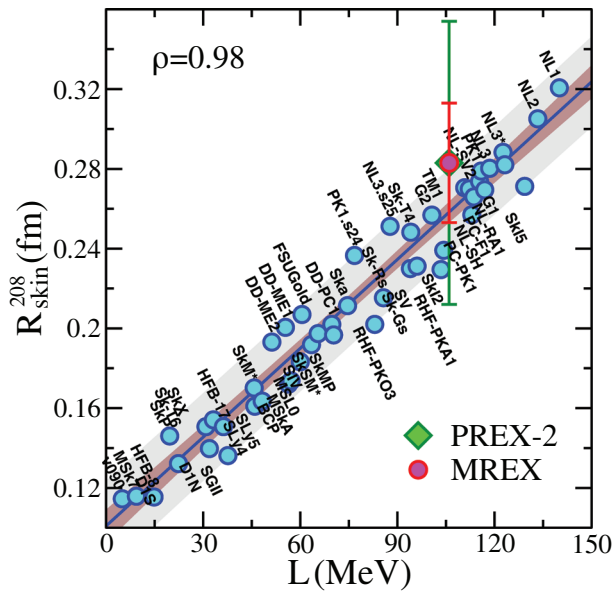
We note that gamma rays at the GF can be utilized to study coherent photoproduction of  $\pi^0$ <sup>[296,297]</sup> near threshold including the cross section dependence on  $A$ , the mass number of the nucleus. An advantage is that, with narrow-band gamma rays tuned close to the threshold, contributions other than coherent photoproduction (i.e., incoherent production and breakup reactions<sup>[297]</sup>) are energetically suppressed. Coherent pion photoproduction is further discussed in the following sections.

##### 4.8.2. Neutron-Skin Measurements in Coherent $(\gamma, \pi^0)$ Reactions

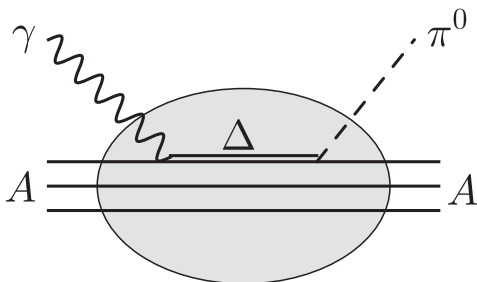
The all-important nuclear equation of state (EOS) relates objects with orders-of-magnitude different sizes, describing the structure and stability of nuclear matter as well as the properties of neutron stars.<sup>[298]</sup> In particular, the authors of ref. [299] used the EOS to likely rule out the neutron-star nature of an object with 2.6 solar masses observed via detecting gravitational waves.<sup>[300]</sup> On the other hand, astronomical observations are being used to infer information about the EOS. The recent LIGO detection of a neutron-star merger constrains the tidal neutron-star polarizability.<sup>[301]</sup> A wealth of new data are provided by the NASA Neutron Star Interior Composition Explorer (NICER) operating as payload on the International Space Station.<sup>[302]</sup> By analyzing recent pulsar data, first joint measurements of the masses and radii of neutron stars became available,<sup>[303,304]</sup> which can be used to set bounds on the EOS parameters.

Tidal polarizability crucially depends on the linear slope  $L$  of the density dependence of the symmetry energy. The neutron skin  $R_n - R_p$ , the difference of the radii of the neutron and proton distributions within a nucleus, is also a sensitive probe of isovector interactions within nuclei and is strongly correlated with  $L$ ,<sup>[305]</sup> as shown in **Figure 15**.

While proton distributions are known with high precision across the nuclear chart<sup>[309]</sup>, information on neutron



**Figure 15.** Correlation of the neutron skin of  $^{208}\text{Pb}$  with the slope  $L$  of the density dependence of symmetry energy.<sup>[298,305]</sup> Blue circles indicate predictions of various nuclear models. The existing experimental measurements of the neutron skin of  $^{208}\text{Pb}$ <sup>[306,307]</sup> are indicated by the green diamond with green error bars, and the future one by red circle and error bar.<sup>[298,308]</sup>

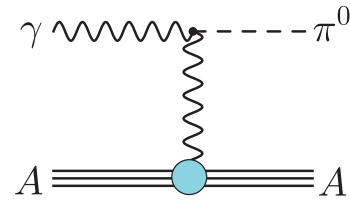


**Figure 16.** Coherent neutral pion photoproduction in the  $\Delta(1232)$  region.

distributions is scarce. The idea of accessing neutron skins with parity-violating electron scattering on nuclei relies on the fact that the neutral weak boson  $Z^0$  couples predominantly to the neutrons. Recent measurements at the Jefferson Lab<sup>[306,307]</sup> furnished precise information on the neutron skin of lead, leading to tighter constraints on the parameters of the EOS.<sup>[310]</sup> Further experiments to extract neutron skins from electron scattering are under analysis<sup>[311,312]</sup> or planned.<sup>[298,308]</sup>

Additional ways to access neutron skins include measuring PV in atoms,<sup>[313]</sup> and coherent  $\pi^0$  photoproduction that was used by the A2 collaboration at Mainz to investigate neutron skin of  $^{208}\text{Pb}$  using photons in the energy range of 180 to 240 MeV.<sup>[314]</sup>

The reaction mechanism is mainly the  $\Delta(1232)$  resonance excitation, as shown in **Figure 16**, by isospin symmetry the same on protons and neutrons, so that the cross section can be brought in correspondence with the baryon density  $Z\rho_p(r) + N\rho_n(r)$ . Using precise knowledge of nuclear charge (i.e., proton) densities,<sup>[309]</sup> one can then deduce the neutron density and the neutron



**Figure 17.** Neutral pion photoproduction via the Primakoff effect.

skin  $R_n - R_p$ , using the definition of the proton and neutron radii,

$$R_{n,p}^2 = \int d^3\vec{r} r^2 \rho_{n,p}(r) \quad (19)$$

The GF with its unique characteristics can allow one to measure coherent  $\pi^0$  photoproduction on various nuclear targets with an unprecedented precision and over a wide range of photon energies and momentum transfers. In order to reconstruct a  $\pi^0$  from the two decay photons one will need a  $4\pi$ -detector similar to the crystal ball used in the Mainz experiment.<sup>[314]</sup> Importantly, the 100% polarization of the photon beam in GF will allow to suppress  $\pi^0$ 's coming from incoherent processes which do not give access to the neutron skin. These incoherent contributions constitute a slowly-varying background that extends over a wide range of momentum transfer, limiting the applicability of the form factor fit beyond the second diffraction minimum. As a result, they contribute a significant part of the systematic uncertainty (see, for example, ref. [315] which discusses additional theory inputs that may affect the interpretation of the experimental data). A measurement of coherent  $\pi^0$  photoproduction at GF thus offers a promising avenue for extracting accurate information about neutron skins alternative to parity-violating electron scattering and atomic parity violation.

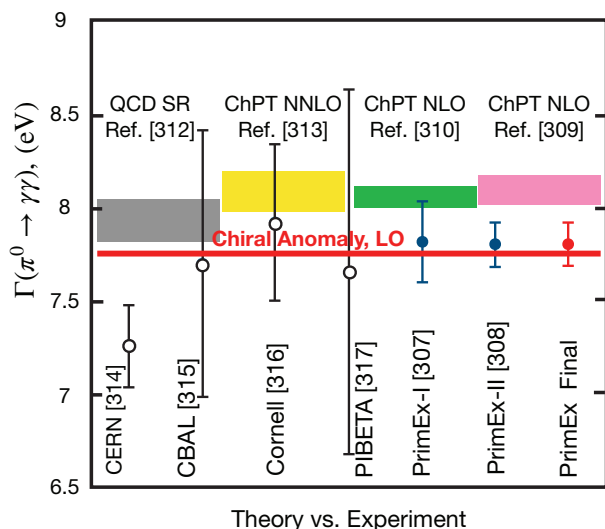
#### 4.8.3. Pion Decay Constant from the Primakoff Effect

The same process, coherent  $\pi^0$  photoproduction, but measured at very forward angles, provides a direct way to measure the radiative  $\pi^0$  width  $\Gamma_{\pi^0\gamma\gamma}$  via the Primakoff effect, see **Figure 17**.

The differential cross section for this process is given by

$$\frac{d\sigma^{\text{Prim}}}{d\Omega} = \frac{8\alpha\Gamma_{\pi^0\gamma\gamma}}{m_\pi^3} Z^2 F_{\text{Ch}}^2(t) \frac{\nu^4 \beta_\pi^2}{t^2} \sin^2 \theta_\pi \quad (20)$$

with  $m_\pi$  being the pion mass and  $Z$ ,  $F_{\text{Ch}}$  the charge and charge form factor of the nucleus, respectively. Furthermore,  $\nu$  is the photon energy,  $\beta_\pi = \sqrt{1 - m_\pi^2/\nu^2}$  the pion velocity,  $t$  the momentum transfer to the nucleus and  $\theta_\pi$  the angle the pion makes with respect to the incoming photon momentum. The most recent PrimEx-II experiment at JLab<sup>[316]</sup> combined with older experimental determinations leads to  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = 7.806(052)(105)$  eV, with the first and the second uncertainty referring to the statistical and systematic one, respectively. This 1.5% determination improved over its predecessor PrimEx-I<sup>[317]</sup> by almost a factor of 2. Historically, the chiral anomaly  $\pi^0 \rightarrow \gamma\gamma$  has served as an important milestone for establishing the chiral perturbation



**Figure 18.** Theoretical predictions for the  $\pi^0$  decay constant: ref. [320] (Chiral Anomaly, LO), QCD sum rules,<sup>[321]</sup> ChPT NNLO,<sup>[322]</sup> and ChPT NLO<sup>[318,319]</sup> in comparison with results from earlier experiments<sup>[323–326]</sup> along with the recent ones by the PrimEx collaboration.<sup>[316,317]</sup>

theory (ChPT), the low-energy effective theory of quantum chromodynamics (QCD), and has been considered the perfect place for comparing ChPT predictions to experimental results ever since. Currently, the most precise next-leading order (NLO) ChPT prediction for the  $\pi^0$  radiative width<sup>[318,319]</sup> reads  $\Gamma(\pi^0 \rightarrow \gamma\gamma) = 8.10(8)$  eV with a 1% uncertainty, showing a mild  $2\sigma$  tension with the experimental result, see **Figure 18**.

The main challenge in extracting the  $\pi^0$  radiative width from a pion-production experiment on a nucleus is due to the presence of coherent and incoherent strong-interaction background channels,

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma^{\text{Prim+Coh}}}{d\Omega} + \frac{d\sigma^{\text{Incoh}}}{d\Omega} \quad (21)$$

which need to be separated from the Primakoff signal. The latter is suppressed with respect to those background processes by  $\alpha^2$ , but has a characteristic  $1/t^2$  behavior which leads to a strong peak at forward angles. This peak resides close to the minimal possible momentum transfer  $t_{\text{min}} \approx m_\pi^4/4\nu^2$ , while strong-interaction contributions reside at larger values of  $t$ . This kinematic separation is the lever arm that is used to reliably extract the Primakoff signal from the pion-production data. As an example for this separation, in the PrimEx kinematics ( $\nu \approx 5$  GeV) for the  $^{208}\text{Pb}$  target the maximum of the Primakoff peak of  $d\sigma/d\theta_\pi$  resides at  $\theta_\pi \approx 0.03^\circ$ , while the coherent nuclear contribution is peaked at  $\approx 1^\circ$ . For comparison, for  $\nu \approx 400$  MeV accessible for secondary photons in the GF the peak positions are  $\theta_\pi \approx 4.5^\circ$  and  $\approx 11^\circ$ , respectively. The shift of the Primakoff peak to larger values of  $t$  automatically leads to its amplitude being reduced according to the  $1/t^2$  dependence in Equation (20) with respect to the background signal that has a less steep  $t$ -dependence. To remedy this situation, the GF may offer a significantly higher statistics as compared to PrimEx-II that uses a tagged Bremsstrahlung photon source. With a higher statistics and assuming that the systematic effects are well under control (which is likely the case

due to the lower energy), one can envision the possibility to independently determine all the ingredients by a fit over a wide angular range. This nicely connects the here envisioned Primakoff effect measurements with the measurements of neutron skins, the subject of the previous subsection, within the same GF experiment.

If a significant flux of tertiary photons can be produced with the GF, one can go to higher energies to conduct a Primakoff experiment in a more conventional setting.

#### 4.9. Precision Measurement of Nuclear E1 Polarizabilities

Precise knowledge of electric dipole nuclear polarizabilities (discussed in Section 4.7 for light nuclei) is important for eliminating uncertainties in determination of the neutron skins,<sup>[327–329]</sup> which, in turn, are essential to constrain the density dependence of the symmetry energy of the nuclear equation of state. Due to its inverse energy weighting, dipole polarizability is sensitive to low-lying  $E1$  strength, see Equation (16). An important quantity is the photoabsorption cross section. Great efforts were undertaken to investigate stable nuclei.<sup>[330]</sup> However, it was realized that much more sensitive probes could be the unstable neutron-rich nuclei, that feature larger skin thicknesses. Systematic measurements as a function of neutron excess would provide stringent constraints. The access to secondary, neutron-rich beams from ISOLDE (see Section 6) will open unique research opportunities at the GF.

Polarizability determinations via measuring gamma-ray transmission are part of the scientific program of the ELI-NP facility.<sup>[183]</sup> The  $^{208}\text{Pb}(\gamma, \gamma')$  reactions were studied also at the electron-bremsstrahlung source ELBE.<sup>[331]</sup> The GF will offer a possibility of carrying out such studies on a broad range of targets with much higher statistical sensitivity and spectral resolution. A measurement program of nuclear electric polarizabilities will complement coherent  $\pi^0$  photoproduction method described in Section 4.8.2.

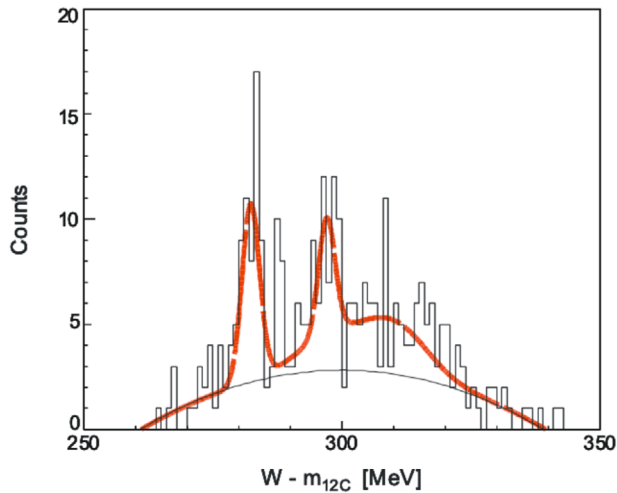
#### 4.10. Delta-Resonance Region and Continuum Effects

The Delta resonance that can be excited in all nuclei is located at around 300 MeV excitation energy and has a large width close to 100 MeV. Of special interest is the pionic decay of this resonance. First of all, pion production on loosely bound nucleons can provide unique information on the wavefunction of exotic nuclei, especially if it would be possible to follow the evolution of this process along a chain of nuclei, from stable to unstable isotopes.

There is another nontrivial interest in the detailed study of the Delta-resonance region. A Mainz experiment in the late 1990s<sup>[332]</sup> claimed the existence of narrow peaks on the background of the broad Delta resonance (see **Figure 19**). Later, this result was put into doubt, and the experimental situation remains unclear. Simple theoretical arguments<sup>[333,334]</sup> show that in the energy region of the Delta resonance there are several possible nuclear Delta + nucleon hole states with the same quantum numbers which are strongly coupled to the pion channel.

This is a typical situation of several intrinsic states interacting both through internal nuclear forces and through the virtual





**Figure 19.** Narrow resonances on top of the broad Delta resonance as claimed in ref. [332]. Adapted with permission.<sup>[334]</sup> Copyright 2004, Elsevier.

decay to the continuum channel. In such cases, a strong continuum coupling leads to the phenomenon of superradiance when a special collective combination (state) acquires a broad width (short superradiant lifetime), while other states with the same quantum numbers become long-lived narrow resonances. The theory of such many-body superradiance, an analog of the theoretically predicted and later discovered electromagnetic Dicke superradiance in optics, was developed earlier,<sup>[335–337]</sup> supported by numerical simulations for various systems with quantum signal propagation and interaction through the continuum, as reviewed in ref. [338]. The simplest explanation, according to von Brentano,<sup>[339]</sup> is in the fact that interaction of quantum states through a common decay mode, in contrast to the usual Hermitian perturbation, leads to the width (imaginary part of the complex energy) repulsion and vastly different lifetimes. Therefore, the presence of narrow pionic resonances on the background of a “superradiating” Delta peak is not excluded theoretically and should be further explored experimentally. Narrow resonances of similar nature are possible also at higher energy as a result of specific quark structures.

Detailed studies of the fine structure of the Delta resonance possible with an intense gamma beam of appropriate energy with different nuclear targets would open a new branch of nuclear physics of relatively high energy where particle physics is combined with details of the nuclear many-body problem.

#### 4.11. Parity-Violation in Photo-Nuclear Processes

PV signatures in the interaction of real photons with nucleons and nuclei arise due to the SM weak interaction among quarks. This underlying mechanism, however, needs to be matched onto hadronic observables. As a result of this matching, a number of effective PV hadron–hadron couplings are generated. Those involving the lightest mesons  $\pi$ ,  $\rho$ ,  $\omega$  are generally expected to govern low-energy processes, and a minimal set was introduced by Desplanques, Donoghue, and Holstein (DDH).<sup>[340]</sup> Among

these couplings the PV  $\pi N$  coupling  $h_\pi^1$  is expected to play a major role since it is the only non-derivative pion-nucleon coupling. Naive dimensional analysis leads to an expectation  $h_\pi^1 \approx G_F \Lambda_\chi F_\pi \approx 10^{-6}$  with  $\Lambda_\chi \approx 1$  GeV the chiral symmetry breaking scale, and  $F_\pi = 92.4$  MeV the pion decay constant. The “DDH preferred value” reads  $h_\pi^1 \approx 5 \times 10^{-7}$ .<sup>[340]</sup>

The hierarchy of DDH couplings has recently been questioned from a new perspective that combines chiral effective theory with the large- $N_c$  approach,<sup>[347]</sup> where  $N_c$  is the number of colors. Within this new paradigm, couplings associated with isovector transitions involving spin (or isoscalar transitions without spin) are large, while the opposite spin–isospin correlation is suppressed. In meson–nucleon interactions without PV, this pattern is supported by a large  $\pi N$  (spin-isovector), vector  $\omega N$  (no spin-isoscalar) and magnetic  $\rho N$  (spin-isovector) couplings. From this perspective,  $h_\pi^1$  (no spin-isovector) should be suppressed. The first non-zero determination of  $h_\pi^1$  in the  $\bar{n} + p \rightarrow d + \gamma$  reaction<sup>[107]</sup> obtained  $h_\pi^1 = (2.7 \pm 1.8) \times 10^{-7}$ , about half the DDH best value, leaving the question, whether or not the large- $N_c$  hierarchy is realized in nature, open.

In Section 3 low-energy, nonresonant Compton processes with a PV signature enhanced by low-lying parity doublets is considered, with primary laser photons backscattered off the ion beam, with the limitation  $\omega \lesssim 60$  keV in the rest frame of the ion. When using secondary photons on a fixed target, higher energies will be achieved with a possibility to tune the photon energy to resonance transitions of interest (see also Section 2). Parameters of relevant resonance transitions with a significant enhancement due to parity doublets are listed for several nuclei in **Table 5**. The resonance will deexcite by emitting photons which will need to be counted in an  $\approx 4\pi$  integrating photon detector, and the dependence of the photon flux in the detector on the circular polarization of the incident photon beam will give access to the PV asymmetry. Due to the resonance kinematics, the enhancement is much stronger than in the nonresonant case, compare to **Table 3**. On the other hand, lower rates will be achieved: the necessity to excite a narrow resonance will reduce the rate accordingly, due to the energy-angle resolution correlation of the secondary-photon GF beam. Still, much larger asymmetries will dominate over lower rates in  $\text{FOM} = \text{Rate} \times A^2$ . While there is a substantial overlap with **Table 3**, the PV asymmetries listed here are significantly enhanced due to the resonant nature of the process. In the past, PV in  $^{19}\text{F}$  and  $^{21}\text{Ne}$  (see the respective entries in **Table 5**) was studied with nuclear, rather than photon, polarization. As shown in, ref. [348] the two observables are fully analogous and, when integrated over the full solid angle of the emitted photon, are equal.

In general, a global analysis of PV observables, typically performed with nuclear systems, is complicated by the need to embed these PV meson-nucleon couplings into PV nuclear potentials and solve nonrelativistic equations which may bear significant uncertainties. As a result, different couplings are intertwined with complicated nuclear effects and may be difficult to disentangle. An alternative way is to move to higher energies where one can directly produce light mesons. Tuning the energy of the photons to the relevant domain one may hope to enhance—if not isolate—the dominant contribution.

**Table 5.** Gamma transitions with an enhanced PV component in isotopes of fluorine, neon and hafnium. Energies are given in keV. Parameters are from the ENSDF database.<sup>[32]</sup>

Isotope	Transition	$T_{1/2}$	Type	Admixture	$T_{1/2}$	Type	$\Delta E$ (keV)	$10^4 A^{\text{PVTC}}$	Ref.
$^{18}\text{F}$ ( $1^+$ )	$0^-(1081) \rightarrow g.s.$	19 ps	E1	$0^+(1042) \rightarrow g.s.$	1.8 fs	M1	39	$-10 \pm 18$	[341]
$^{19}\text{F}$ ( $1/2^+$ )	$1/2^-(110) \rightarrow g.s.$	0.6 ns	E1	$1/2^+ - 1/2^-$			110	$-0.68 \pm 0.18$	[342,343]
$^{21}\text{Ne}$ ( $3/2^+$ )	$1/2^-(2789) \rightarrow g.s.$	81 ps	E1/M2	$1/2^+(2795) \rightarrow g.s.$	5.5 fs	M1	5.7	$24 \pm 29$	[344]
								$8 \pm 14$	[345]
$^{180}\text{Hf}$ ( $0^+$ )	$8^-(1142) \rightarrow 6^+(641)$	5.53 h	M2/E3	$8^+(1085) \rightarrow 6^+(641)$	2 ps	E2	57	$-148 \pm 26$	[346]

Threshold  $\pi^+$  photoproduction on the proton with circularly polarized photons was proposed in ref. [349] as a way to access  $h_\pi^1$ . The PV asymmetry is practically isotropic and is given by

$$A_\gamma \approx \frac{\sqrt{2}F_\pi(\mu_p - \mu_n)}{|g_A|M_N} h_\pi^1 \approx 0.52h_\pi^1 \quad (22)$$

with  $g_A \approx -1.27$  being the nucleon axial coupling and  $\mu_{p,n}$  being the proton and neutron magnetic moment, respectively. The sensitivity to the value of  $h_\pi^1$  compares well to that in the nuclear  $\bar{n} + p \rightarrow d + \gamma$  process for which the asymmetry is  $A_\gamma \approx -0.11h_\pi^1$ . To estimate the rate and FOM, we note that the total cross section for  $\pi^+$  photoproduction off the proton at 180 MeV photon energy is  $\approx 100 \mu\text{b}$ . Since the asymmetry is roughly energy-independent, no particularly high energy resolution is necessary. Let us assume  $10^{-3}$  out of  $10^{17}$  photons arrive on target; hydrogen target is probably not the best option, so let us assume it is carbon—then we will be looking at  $\pi^\pm$  in the detector. The asymmetry is roughly the same but the cross section is  $Z^2 = 36$  times that on the proton, for each pion species. Assuming a  $1 \text{ cm}^3$  target, its cross section will have  $\approx 10^{23} \text{ }^{12}\text{C}$  nuclei to interact with. So, we get  $10^{14} \times (3.6 \times 10^{-27} \text{ cm}^2)/1 \text{ cm}^2 \times 10^{23} = 3.6 \times 10^{10} \pi^+ \text{ s}^{-1}$ . For asymmetries  $\approx 1.4 \times 10^{-7}$  we get  $\text{FOM} \approx 7 \times 10^{-4} \text{ s}^{-1}$ .

A similar process was proposed with a semi-inclusive  $\pi^+$  electroproduction at threshold  $p(\bar{e}, \pi^+)e'n$ . Photoproduction has an advantage over electroproduction in that there is no background from Z-exchange, and all the signal is due to  $h_\pi^1$ .

As one moves to the resonance region, a direct PV photoexcitation of a nucleon and  $\Delta$  resonances become possible. Most notably the PV  $\gamma N\Delta$  coupling  $d_\Delta^+$  ( $d_\Delta^-$ )<sup>[350]</sup> responsible for a  $E1 \gamma p \rightarrow \Delta^+$  ( $\gamma n \rightarrow \Delta^0$ ) transition, respectively, gives rise to the asymmetry

$$A_\gamma^\pm \approx -\frac{2d_\Delta^\pm M_N}{C_3^V \Lambda_\chi} \quad (23)$$

with  $C_3^V = 1.6$  being the usual parity-conserving coupling inducing the M1  $\gamma N\Delta$  transition. A measurement of  $\pi^-$  electroproduction on the  $\Delta$  resonance on a deuterium target by the G0 collaboration<sup>[351]</sup> obtained

$$A_\gamma^- = -(0.36 \pm 1.06 \pm 0.37 \pm 0.03) \text{ ppm} \quad (24)$$

with the three uncertainties being the experimental statistical, theoretical, and experimental systematic, respectively. Accordingly, a loose bound  $d_\Delta^- = (3 \pm 10) \times 10^{-7}$  was extracted. It can be

expected that the GF will be able to measure these small asymmetries  $\approx 10^{-8}$  due to high intensity and 100% photon polarization, together with relatively high resonant cross sections  $\approx 300 \mu\text{b}$ .

Another promising task for the GF is the resonant PV  $\Sigma$  hyperon production  $\bar{\gamma} + p \rightarrow \Sigma^+$  with a subsequent decay to the  $\pi N$  final state. Until now, the reverse  $\Sigma^+ \rightarrow \bar{\gamma} + p$  decay with a branching ratio  $1.23(5) \times 10^{-3}$  has been accessible, with the scope of studying the asymmetry  $a_\gamma = 0.76 \pm 0.08$ .<sup>[352]</sup> The competing process is the nonresonant  $\gamma p \rightarrow \pi N$  process which, at the  $\approx 200$  MeV incident beam energy, is well understood, and the asymmetry for the inclusive reaction is due to the PV coupling  $h_\pi^1$  leading to  $10^{-8}$  asymmetries. While the contribution of  $\Sigma$  production is suppressed with respect to nonresonant pion photoproduction, the figure of merit introduced in Section 3 favors  $\Sigma$  photoproduction: it depends on the cross section linearly, and quadratically on the asymmetry. With a precise tune of the photon energy to the  $\Sigma$  hyperon position, the large asymmetry more than compensates for low rate.

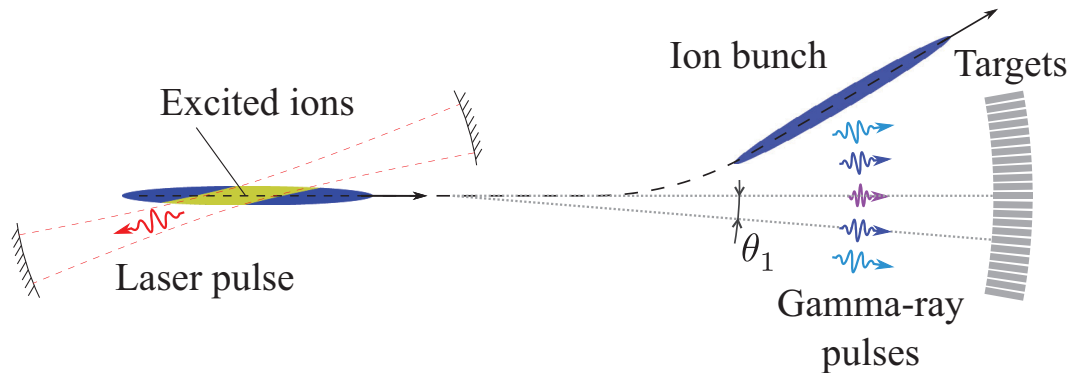
## 5. Experimental Considerations with Fixed Targets

### 5.1. Thermal-Load Issues

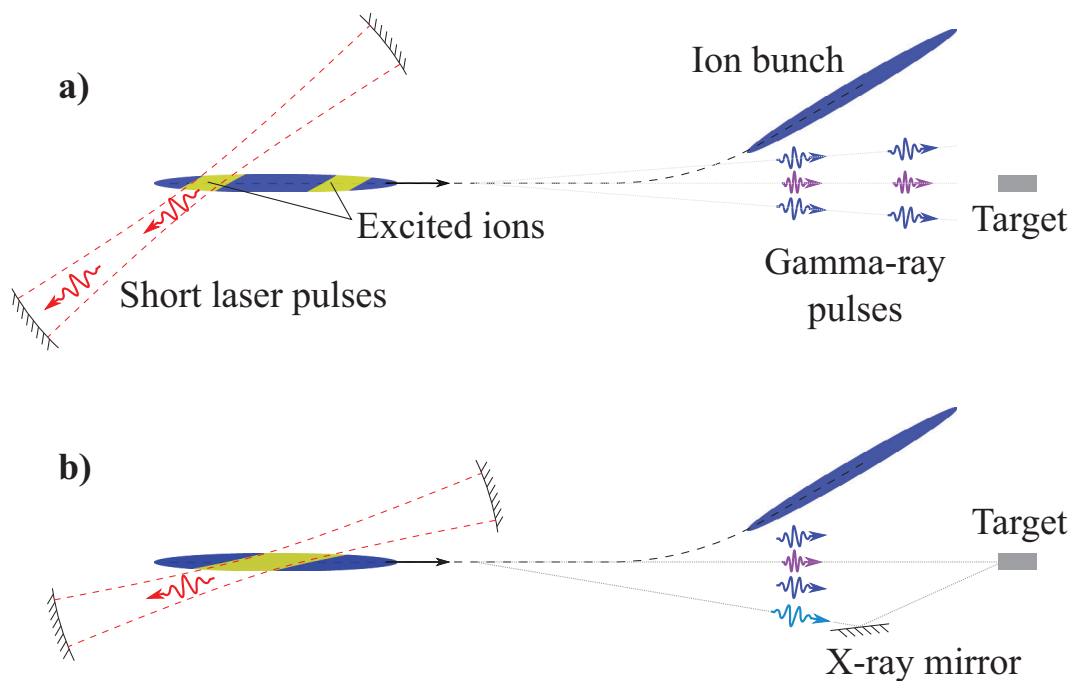
In designing fixed-target experiments at the GF, it is important to realize that the secondary photon beam carries significant power. With the maximum gamma-ray energy and a total photon flux (at all energies), the power carried by the photons is 3 MW. To make such energy load manageable for the target, it may be beneficial to position the target as far away as possible from the interaction region. With  $\gamma \approx 10^3$  and neglecting the initial PSI angular spread, positioning a 2 m diameter target at a distance of 1 km would match the target size to the diameter of the “spot” produced by the gamma rays emitted in the  $\approx 1/\gamma$  cone.

### 5.2. Parallel Spectroscopy with Spatially Resolved Detection

The strong correlation of the photon energy with its angle of propagation (see Section 1.1) suggests a possibility of conducting experiments utilizing the entire flux of the GF secondary photons. This requires a detector providing spatial resolution (**Figure 20**). With this arrangements, a photon with a given energy will hit a ring-shaped area on the target. Parallel spectroscopy offers the advantage of efficient utilization of the GF running time as opposed to scanning arrangements, where a narrow slice of the gamma-ray energies is selected via collimation and the energy is tuned, for instance, by simultaneously adjusting the PSI  $\gamma$  factor and tuning the primary-photon energy.



**Figure 20.** The parallel spectroscopy configuration.



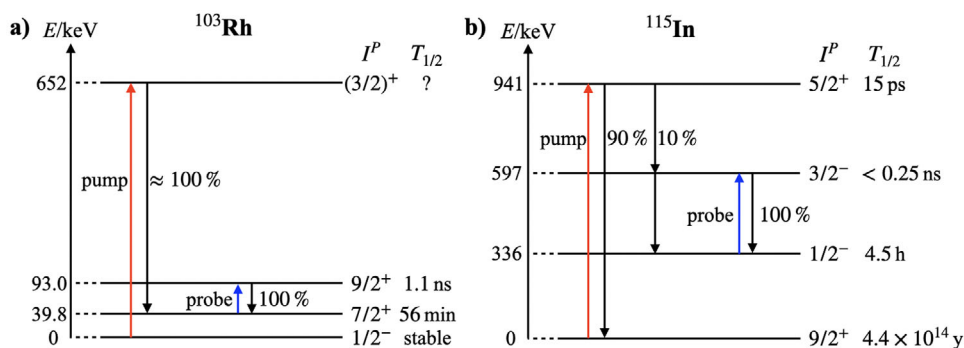
**Figure 21.** The Gamma Factory configurations suitable for the pump-probe experiments: a) sufficiently large angle of collision between the laser and the ion beam allows for the laser temporal profile to be imprinted into the gamma-ray pulses; b) X-ray probe pulse can be selected and energy-tuned using a small-angle X-ray mirror.

### 5.3. Gamma-Ray/X-Ray and Gamma-Ray/Gamma-Ray Pump-Probe Spectroscopy

Pump-probe techniques are ubiquitous in atomic, molecular, and condensed matter physics, and are used in many variants, both in time and spectral domain. Here the system under study is first subject to the “pump” photons that cause the system to undergo a transition, for example, an excitation of an atomic or molecular state or melting a crystalline lattice. The changes in the system are then monitored via its interactions with the “probe” photons.

Pump-probe spectroscopy, in novel regimes, is also possible with the GF (**Figure 21**). The pump and probe pulses of secondary GF photons can be produced using two laser pulses. This gives an option for both the pump and the probe being gamma rays.

We can, for example, have two primary laser pulses interacting with the same ion bunch. The energy of the pump and probe can be tuned within  $\approx 10^{-3}$  (the energy spread of the PSI that can be maintained in the ring) by selecting different parts of the ion energy distribution. One can also do “gross” tuning by choosing different atomic transitions in the PSI. It could be possible to imprint a temporal structure onto the gamma-ray pulse in order to perform pump-probe experiments with sub-ps resolution. The duration and timing of the gamma-ray pulses will be determined by geometric overlap between the sufficiently short laser pulse and the ion beam. With a  $\approx 10 \mu\text{m}$ -wide ion beam in a typical LHC interaction point, the minimum duration of the gamma-ray pulse could be  $\approx 30 \text{ fs}$ , which comes from the  $10 \mu\text{m}$  divided by the speed of light, assuming that the laser beam propagates per-



**Figure 22.** Pump-probe spectroscopy with a)  $^{103}\text{Rh}$  and b)  $^{115}\text{In}$  isomers. The branching ratio after exciting the nucleus to a higher energy level,  $I^P$  and  $T_{1/2}$  of energy levels are shown (according to the NuDat 2 database<sup>[55]</sup>).

pendicularly to the ion beam. This requires a correspondingly short laser pulse, but generation of such pulses is routine with modern lasers. Different-energy photons could come in overlapping pulses (down to 30 fs) or be separated by a fraction of a nanosecond if they are derived from the same ion bunch, or can come from different ion bunches and have correspondingly long separation.

Some of the options for GF based pump-probe spectroscopy include:

- The light pulses could be tuned to two different transitions of the PSI;
- Pump and probe can be of the same energy (depending on the experiment);
- The pump and probe can be produced from different PSI bunches;
- Pump and probe pulses do not necessarily need to be temporally separated;
- Pump-probe spectroscopy with nuclear isomers. If the produced nuclear states are sufficiently long-lived, one could move the production target (Figure 21a) to probe produced nuclear states using gamma rays with different energy at different spatial locations;
- Because the photons emitted at the periphery of the  $\approx 1/\gamma$  cone are of low energies, one can design a pump-probe experiment with a gamma-ray pump and an X-ray probe (Figure 21b) using the well-developed technology of grazing-incidence X-ray mirrors.<sup>[353]</sup> An attractive feature of this scheme is that the X-ray energy can be tuned by tilting the mirror; a potential downside for some experiments would be the inherent time delay (due to the difference in the optical path length) between the pump and probe pulses.

Two specific examples of a possible application of pump-probe spectroscopy are shown in **Figure 22**. These examples involve isomers from Table 7. Pump-probe spectroscopy as discussed here could be used to prove the feasibility of producing the isomers at the GF and to study reaction cross sections and production rates.

#### 5.4. Highly Monochromatic Gamma Beams

Energy bandwidth is a key parameter when aiming for exciting narrow nuclear resonances with typical intrinsic widths of a few

eV. Exciting such a resonance with a  $\gamma$  beam of a few tens to hundreds of keV, as currently available from existing facilities, will predominantly result in background generated by the large amount of off-resonant incident photons. So aiming for clean  $\gamma$ -spectroscopic conditions requires reducing the energy bandwidth of the  $\gamma$  beam ideally to the physical limit set by (thermal) Doppler broadening.

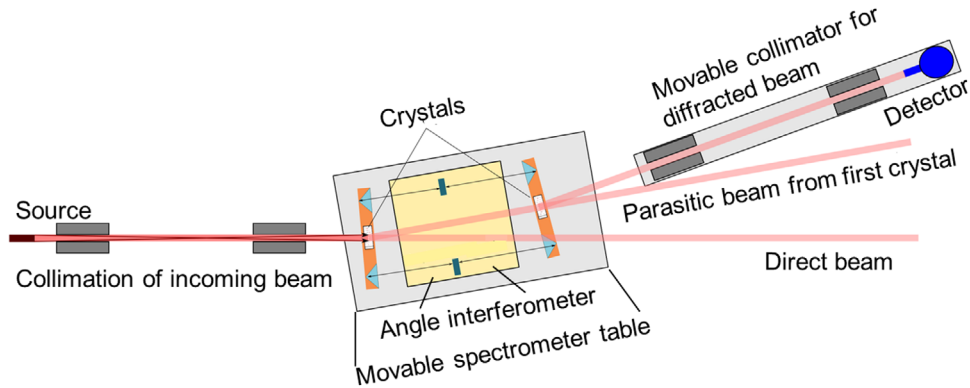
The highly brilliant  $\gamma$ -ray source of the GF will deliver a  $\gamma$  beam with a divergence in the range of milliradians, with a photon flux of up to  $10^{17}$   $\gamma$  rays  $\text{s}^{-1}$ , and a possibility of monochromatization on the order of  $\Delta E_\gamma/E_\gamma \approx 10^{-3}$  over a wide energy range. Due to pile-up problems, this intense beam would put serious constraints on detection systems if it were used without further preparation. A substantial fraction of foreseen experiments at this facility will be based on the concept of nuclear resonance fluorescence (NRF; see Section 4.1). For NRF experiments the optimal monochromatization should be equal to the width of the excited nuclear resonances, which is expected to be of the order of  $\Delta E_\gamma/E_\gamma \approx 10^{-6}$ , due to thermal motion of the target atoms. Therefore, further monochromatization of the  $\gamma$  beam would on the one hand provide an improved signal-to-noise ratio for these experiments as well as solve eventual detection problems. Therefore, when aiming for an ultimate quality of nuclear  $\gamma$  spectroscopy, the unprecedented intensity of the GF photon beam can serve as an asset to trade beam intensity for spectral resolution.  $\gamma$ -ray optics allowing to further monochromatize the  $\gamma$  beam is thus of high importance for a future high-intensity  $\gamma$ -beam facility like the GF.

The most accurate method for the absolute determination of  $\gamma$ -ray wavelengths relies on crystal diffraction from highly perfect flat crystals of silicon or germanium, allowing to obtain a resolving power which is unequalled by any other  $\gamma$ -ray spectroscopic methods. Over many years, the concept of crystal-based photon diffraction has been pioneered and optimized at the GAMS facility at the Institut Laue-Langevin (ILL) in Grenoble<sup>[354–356]</sup> as a technique to monochromatize  $\gamma$  beams.<sup>[357]</sup>

Diffraction of photons is governed by Bragg's equation

$$n \cdot \lambda = n \frac{hc}{E_\gamma} = 2d \sin\theta_B \quad (25)$$

Here  $h$  represents Planck's constant,  $c$  is the speed of light,  $n$  is the diffraction order,  $d$  the lattice spacing of the diffracting crys-



**Figure 23.** Layout of a double-crystal monochromator as realized at the GAMS facility of the ILL (Grenoble).<sup>[357]</sup> The consecutive action of the two crystals is seen. Both crystals are mounted on interferometer arms. The positions of these arms with respect to a movable spectrometer table are controlled with optical interferometers. The diffracted beam is separated with a movable collimation system away from the intense direct beam. Adapted under the terms of the CC-BY license.<sup>[357]</sup>

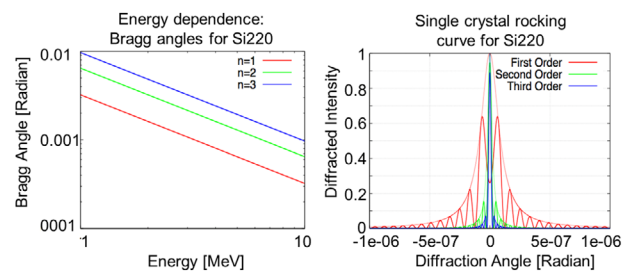
tals and  $\theta_B$  the diffraction angle. While this equation provides information on the energy dependence of  $\theta_B$ , information on resolution power is obtained from dynamical diffraction theory,<sup>[358]</sup> predicting the dependence of diffracted intensity  $I$  on the diffraction angle  $\theta$ . The result is summarized by the following simplified expression

$$I(\theta) \propto \frac{\sin^2(A\sqrt{1+\gamma^2})}{1+\gamma^2}, \quad \gamma \propto \frac{hc}{E_\gamma}(\theta - \theta_B), \quad A \propto \frac{hc}{E_\gamma} \quad (26)$$

Hence the diffracted intensity consists of an oscillating term surrounded by a Lorentzian envelope and its width, corresponding to the “acceptance width” of the monochromator can be estimated to scale with  $hc/E_\gamma$ . Comparing the scaling of the acceptance width to Equation (25) results in

$$\frac{\Delta E_\gamma}{E_\gamma} = \frac{\Delta\theta}{\theta_B} \approx \frac{C}{n} \quad (27)$$

where  $C$  is a constant. From Equations (25) and (26), it follows that the achievable energy resolution is independent of the incident photon energy  $E_\gamma$ . The acceptance width of a perfect crystal can be as small as a few nanoradians. Thus the number of  $\gamma$  rays accepted from the incident beam for diffraction is small. In fact, a perfect crystal acts for  $\gamma$  rays as an excellent collimator, accepting almost exclusively the nondivergent part of the beam and diffracting it in a different direction with respect to the incoming beam. Since the initial beam is typically several orders of magnitude more divergent, this selection results in a drastically attenuated diffracted beam. For the divergence expected for the GF, one expects a loss factor of about nine orders of magnitude. In order to fully exploit the properties of a perfect crystal for the production of monochromatic  $\gamma$  rays it would be required that the divergence of the incident photon beam were comparable to the acceptance width of the crystal. This can be achieved by combining two crystals to form a double-crystal monochromator. The first crystal will produce a multitude of monochromatic beams, where each energy is diffracted in a low-divergence beam directed at its particular Bragg angle. A particular energy may then be



**Figure 24.** Left: Energy dependence of the Bragg diffraction angle  $\theta_B$  for a (220) silicon crystal. Right: Rocking curve of a (220) Si crystal, that is, distribution of the diffracted intensity as a function of the diffraction angle.

selected with the second crystal. This scheme is realized in the GAMS facility at the ILL (Grenoble), as shown in **Figure 23**.<sup>[356]</sup>

A double-crystal spectrometer can be operated in two geometries. In the so-called non-dispersive alignment mode, the two crystals are positioned in parallel, which means that all  $\gamma$  rays diffracted by the first crystal are accepted by the second crystal. In this case, no energy selection is made and there is no monochromatization. However, this geometry delivers a measurement of the intrinsic instrument resolution as it measures the convolution of two single-crystal intensity profiles  $I(\theta)$  of Equation (26). In the dispersive geometry, the spectrometer realizes a dedicated Bragg angle  $\theta_B$  between the crystals and therefore selects specific energies. A detailed review on the two geometries can be found in ref. [359].

A typical measurement procedure involves rocking of the second crystal (and detector) such that its orientation is  $+\theta_B$  and  $-\theta_B$  relative to the first diffracted beam. Except for small ( $\approx 10^{-7}$ ) corrections due to a finite vertical divergence, the angular separation of these two diffracted beams is  $2\theta_B$ . The diffraction angles are measured by polarization sensitive Michelson interferometers which have a sensitivity of  $\approx 10^{-9}$  rad<sup>[355]</sup> and which are calibrated using an optical polygon.<sup>[356]</sup> The left panel of **Figure 24** shows the  $\gamma$ -ray energy dependence of the Bragg diffraction angle  $\theta_B$  for a Si crystal cut along the (220) direction, typically (depending on diffraction order and photon energy) ranging between 1 mrad (at 1 MeV) to about 10 mrad for  $E_\gamma = 10$  MeV. The

single-crystal rocking curve, that is, the distribution of the diffracted  $\gamma$ -beam intensity for the same type of (220) Si crystal is shown in the right panel of Figure 24, exhibiting diffraction angles of the order of 10 nrad.

Such a double-crystal monochromator can reach high resolution and instrumental diffraction widths nearly equal to those predicted by dynamical diffraction theory<sup>[358]</sup> have been obtained for energies up to about 6 MeV.

From a practical perspective, to realize an ultimate  $\gamma$ -ray energy resolution a three-stage measurement chain is needed to link the  $\gamma$ -ray wavelengths of interest to visible wavelengths.<sup>[354]</sup> In a first step, the lattice spacing of a Si crystal is measured in terms of the wavelength of an iodine-stabilized HeNe laser operating near 633 nm. This step employs simultaneous X-ray and optical interferometry and yields a calibrated Si-crystal sample. In the second step, the lattice spacings of various other crystals are compared to the calibrated Si crystal to yield a family of crystals whose lattice spacings are known relative to the optical wavelength. This method employs an X-ray crystal comparator. In the final step, which comprises the double-crystal monochromator setup,  $\gamma$  rays are diffracted by the crystals calibrated in the second step and the diffraction angles are accurately measured. By combining the measured lattice spacing and diffraction angles,  $\gamma$ -ray wavelengths are determined with high accuracy.

The difficulty in making sub-ppm wavelength measurements via this prescription may be seen by considering the accuracy required in the measurement of the lattice-spacing parameter  $d$  and the diffraction angle  $\theta$ . The crystal-lattice constant  $d$  must be determined with an accuracy of  $\approx 10^{-17}$  m. The Bragg angle ( $\approx 10^{-3}$  rad at 5 MeV) must be determined with an angular precision of  $\approx 10^{-10}$  rad. In addition, the angular scale upon which the Bragg angle is measured must have an accuracy of  $\approx 1$  in  $10^7$ .<sup>[355]</sup> Such properties have been demonstrated at the GAMS facility and can thus serve as a “role model” for a potential monochromator to be integrated into the GF experimental device suite with an envisaged relative energy resolution  $\Delta E_\gamma/E_\gamma \approx 10^{-6}$ .

## 6. Photophysics with a Storage Ring for Radioisotopes

The secondary beam of the GF can be used to irradiate solid-state targets of stable or long-lived nuclides. In general, such experiments have been performed in the past and are planned at future photon facilities, though with photons at different energies and/or lower intensities as compared to the GF. However, the ultimate interest and the highest discovery potential lie in investigations of exotic nuclei with large proton-to-neutron asymmetries. Nuclei far from the line of stability are currently at the center of interest in nuclear structure physics. They offer insight into the physics of loosely bound finite drops of Fermi liquid, and are intricately related to astrophysical processes of formation of stable nuclei with their observed abundances on Earth and in the Universe. Estimates predict the existence of more than 7000 nuclei stable with respect to particle decay;<sup>[360]</sup> the lifetime of those outside of the valley of stability is determined by weak decays in the direction of this valley. Experimental access to these species is rendered possible by several new-generation facilities under construction including FAIR in Germany, SPIRAL2 in France, HIAF in China and FRIB in the USA.

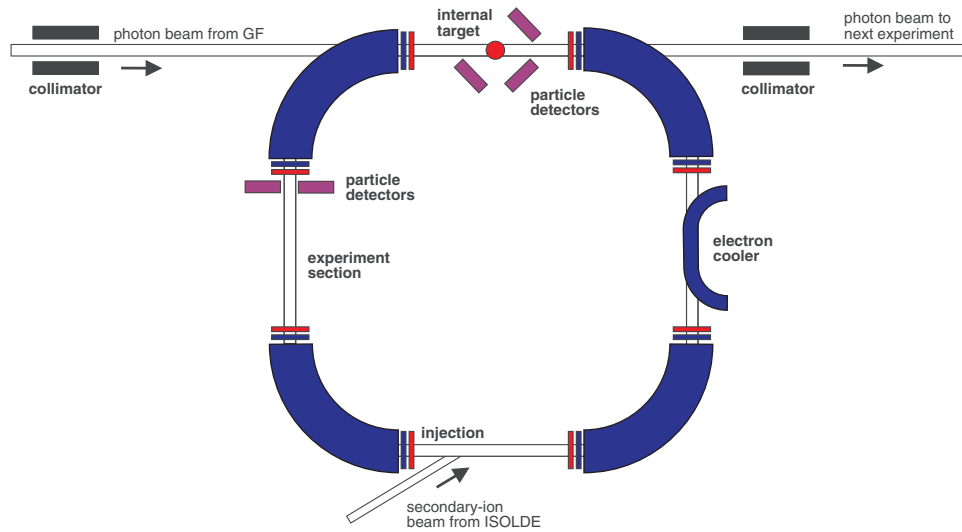
Exotic nuclei are inevitably short-lived and their production rates in nuclear reactions are small. For instance, halo phenomena, where one or a few valence nucleons are weakly bound, occur in short-lived nuclei lying close to the limits of nuclear existence, the so-called driplines, see Section 4.8. The “classic” halo nucleus  $^{11}\text{Li}$  has a half-life of merely 8.75(14) ms,<sup>[55]</sup> and no target can be produced out of it. As known from first detailed studies,<sup>[361]</sup> the size of external weakly bound neutron orbitals in  $^{11}\text{Li}$  is essentially the same as the size of the strongly bound doubly magic isotope  $^{208}\text{Pb}$ . There is still no general agreement on the mechanism leading to the binding at such large distances. The wavefunction of halo nucleons looks like that of one or a few Cooper pairs bound to a normal core by some special forces.<sup>[362,363]</sup> There are also competing mechanisms: the collective modes of the core coupled through the continuum may create loosely bound states, as for example in the heaviest oxygen isotopes.<sup>[364]</sup>

The location of the GF at CERN has a unique advantage of having in its close proximity a state-of-the-art radioactive-ion-beam facility, the ISOLDE.<sup>[365]</sup> The ISOLDE facility offers a large variety of secondary beams. As of today, an intense 1.4 GeV proton beam impinges on a thick, several  $10\text{ g cm}^{-2}$ , production target, such that the reaction products stop in the target material. Target spallation and fission are the major nuclear reactions giving access to exotic nuclei of interest. A variety of schemes have been developed to achieve clean secondary beams delivered to various experimental stations. In the present context, the major option is HIE-ISOLDE<sup>[366]</sup> (HIE stands for high intensity and energy), which provides post-accelerated beams at energies of up to 10 MeV per nucleon in high atomic charge states after charge breeding in a dedicated REXTRAP/REXEBS system.<sup>[367,368]</sup>

To bring exotic nuclei in collisions with photons, their storage is indispensable. About a decade ago, a proposal was put forward at ISOLDE to install a dedicated storage ring.<sup>[369]</sup> Such storage ring is a part of the upgrade program of the ISOLDE, the EPIC project (Exploiting the Potential of ISOLDE at CERN).<sup>[59]</sup> On the one hand, its installation will enable a broad range of unique physics experiments at HIE-ISOLDE, see ref. [369]; on the other hand, the research scope can be dramatically extended if merging with the photons from the GF is achieved. Since the photons cannot be transported to ISOLDE, the storage ring needs to be constructed next to the GF. A beamline from the ISOLDE to the GF site is required to transport secondary ion beams at energies of a few MeV per nucleon from the ISOLDE hall to the GF. Dependent on the exact location of the GF, such beamline can be 100–300 m long.

The interactions of the GF photons with antiprotons can also be envisioned. Various technical solutions can be considered. A straightforward approach is to construct a beamline connecting the antiproton decelerator (AD) facility and the proposed storage ring at the GF. The PUMA project (antiProton Unstable Matter Annihilation<sup>[370]</sup>), aims at transporting trapped antiprotons from AD to ISOLDE to study antiproton collisions with exotic nuclei. A similar methodology may as well be applied.

The design of the storage ring will be based on the experience gained in operation of the low-energy storage rings TSR in Heidelberg<sup>[369]</sup> and CRYRING@ESR in Darmstadt.<sup>[371]</sup> It will have a circumference of about 40 m. Secondary ions stored at energies of a few MeV per nucleon will have typical revolution frequencies of a few hundred kHz. The ring will have four straight

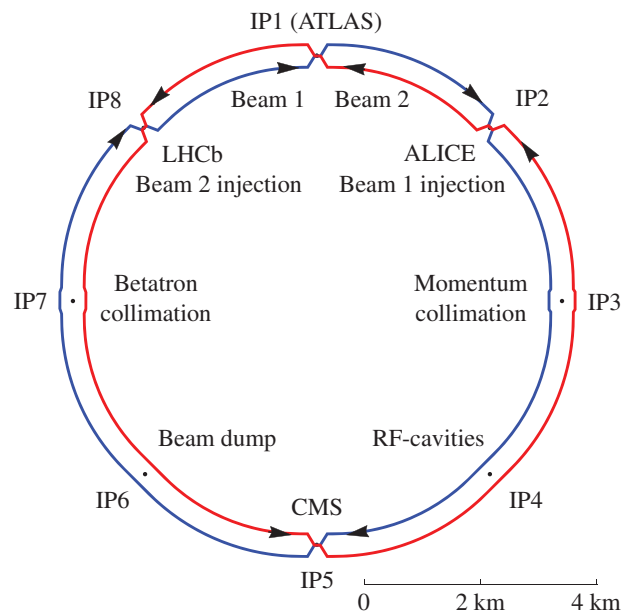


**Figure 25.** A sketch of a possible arrangement of the low-energy storage ring at the GF. The photon beam from the GF comes from the left and interacts with the stored secondary ion beam. The photon beam leaves the ring on the right and can be employed in a next experimental station. An internal gas target can be implemented as an option.

sections, where two of them will be used for injection/extraction and an electron cooler. The experimental straight section will be aligned with the photon beam, see **Figure 25**. In order to reduce heat load and stress on vacuum windows, an evacuated pipe can be used to connect SPS/LHC and the storage ring.

Dependent on the specific physics case, coasting as well as bunched beams will be employed. If nuclear and storage lifetimes allow, accumulation of beam currents up to about 1 mA is possible.<sup>[369]</sup> The electron cooled ion beam has a momentum spread on the order of  $10^{-4}$  or better and the transverse size is about 1 mm. These parameters constrain the interaction region and thus offer excellent conditions for high energy and angular resolution in experiments. The beam is stored at a few MeV per nucleon energy which facilitates the detection of the beam-like recoils and reaction products. Any product of a charge-changing (atomic or nuclear) reaction will be deflected differently by the dipole magnets as the primary beam and can thus be intercepted by a particle detector. It should be emphasized that all tools developed at various storage rings<sup>[372,373]</sup> can be available here as well, which allow, for example, to prepare the beam in a specific, well-defined atomic or nuclear state by employing internal targets or dedicated laser beams.

One of many experiments that would be enabled by the GF, is the measurement of the dipole polarizability of short-lived neutron-rich nuclei. Such measurements have been performed on external targets. For instance, radioactive  $^{68}\text{Ni}$  was studied at the R<sup>3</sup>B setup at GSI by colliding a secondary  $^{68}\text{Ni}$  with a heavy lead target.<sup>[181]</sup> One- and two-neutron decay channels were studied. A straightforward advantage of the GF is the access to the most exotic nuclear species. A secondary beam of interest stored in the ring will react with real photons from the GF. Beam-like recoils from various decay channels, analyzed by the dipole magnets of the ring, can unambiguously be identified with near-unity efficiency. In coincidence, the emitted particles can be detected with dedicated detector setups surrounding the interaction region.

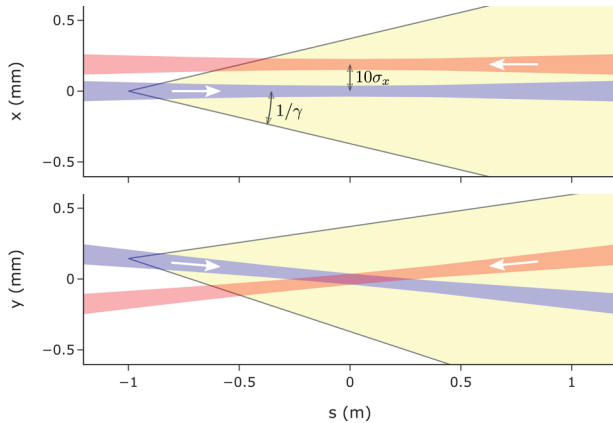


**Figure 26.** The LHC layout. Adapted with permission.<sup>[374]</sup> The separation between the beams is exaggerated here (in reality it is 20 cm). IP: interaction points.

The photon beam from the GF will pass through the interaction region of the storage ring and can be used in different experiments downstream.

## 7. Colliding-Beam Opportunities

The LHC collider (see **Figure 26**) has two counter-rotating beams which are normally separated by 20 cm horizontally and brought to collision at several interaction points around the ring. Superconducting magnets guiding both beams share the same



**Figure 27.** The typical LHC interaction point (IP) configuration compared to a  $1/\gamma$  cone of gamma-radiation. The diameter of the beams in this picture is  $4\sigma_{x,y}$  (at the IP  $\sigma_{x,y} \approx 19 \mu\text{m}$ ). The beams are separated by  $10\sigma_x \approx 0.2 \text{ mm}$  horizontally in order to avoid stripping of the PSI due to collisions with counter-propagating ion or proton beam.

cryostat. Due to the magnet design, the strength of the magnetic field guiding each beam is the same (rigidity of both beams is the same). The LHC can operate in proton-proton, ion-ion, or ion-proton collision mode.

The secondary photons produced at the GF can themselves be directed onto a relativistic beam, for instance the counter-circulating beam of the LHC (see **Figure 27**), thus benefiting from another Lorentz boost of photon energy (for secondary photons in the frame of the counter-circulating ions/protons) or two Lorentz boosts (for tertiary photons in the lab frame). This possibility, that may be realized at a later stage of the GF program, may open additional physics opportunities. We briefly discuss some of them here.

### 7.1. Photoabsorption Structure Functions

Via scattering secondary photons from the GF head-to-head off a proton or ion beam, one can study polarized and unpolarized inclusive structure functions at high energies.

For secondary photons with energy  $\omega$  in the laboratory frame and a proton beam with a relativistic factor  $\gamma_p$  up to  $\approx 7000$  from the LHC, the highest invariant mass amounts to

$$\sqrt{s} = \sqrt{4M_p\gamma_p\omega} \leq 108 \text{ GeV} \sqrt{\frac{\gamma_p}{7000} \cdot \frac{\omega}{400 \text{ MeV}}} \quad (28)$$

The total photoabsorption cross section can be written in terms of inclusive structure functions familiar in the context of inelastic electron scattering.<sup>[352]</sup> Those surviving for real photons are  $F_{1,3}$  and  $g_{1,5}$ , and denoting the photon circular polarization  $\xi = \pm 1$  and the proton helicity  $h = \pm 1/2$ , we write

$$\sigma(\xi, h) = \frac{8\pi^2\alpha}{s - M^2} \left[ F_1 - 2h\xi g_1 + \frac{\xi}{2} F_3 + 2hg_5 \right] \quad (29)$$

The structure functions  $F_i$ ,  $g_i$  are functions of  $s$ . The first two terms in Equation (29) conserve parity, while the last two terms are parity-violating.

High-energy behavior of scattering amplitudes is governed by Regge theory and is economically described by  $t$ -channel exchanges. The leading contribution to the spin-averaged structure functions  $F_1$  at asymptotically high energies is identified in QCD with exchanges of gluons which combine into colorless compounds, while quark-antiquark (meson) exchanges are suppressed.<sup>[375]</sup> The well-known pomeron that has quantum numbers of the vacuum and couples equally to particles and antiparticles ( $C$ -parity even), is identified with the colorless two-gluon exchange. An exchange of a colorless three-gluon state leads to a  $C$ -odd odderon which couples to particles and antiparticles with an opposite sign. Predicted nearly 5 decades ago,<sup>[376]</sup> this elusive kind of interaction of hadrons has just recently been observed in Tevatron/LHC data.<sup>[377]</sup> While not accessible with the inclusive photoabsorption cross section by Furry's theorem (structure functions are the imaginary part of the forward Compton amplitude), the odderon can contribute to exclusive channels, for example, photoproduction of axial vector mesons, or in parity-violating asymmetries, as outlined below. This would be the first observation of the odderon in electromagnetically induced scattering processes.

Data on  $F_1$  with real photons exist up to  $\approx 200 \text{ GeV}$ ,<sup>[352]</sup> nonetheless the new data at GF are expected to significantly improve the precision. Using ion beams one can study nuclear shadowing: it is observed that a high energy probe does not see all nucleons within a nucleus, but only part of them.<sup>[378]</sup> GF can allow to study nuclear shadowing at highest attainable energies where only the leading pomeron exchange gives a sizable contribution (asymptotic regime), or below where other contributions are non-negligible (sub-asymptotic regime).

Measuring the structure function  $F_3$  entails shining a beam of circularly polarized photons onto an unpolarized proton/ion beam. No data on the purely electromagnetic  $F_3$  exist. Data on this structure function in electron scattering are almost exclusively sensitive to interference of the  $Z^0/\gamma$  exchange between the electron and the proton. A superconvergence relation  $\int_0^\infty \frac{d\omega}{\omega^2} F_3(\omega) = 0$  was derived in ref. [379], but has never been verified experimentally. GF can provide the input to this sum rule from the inelastic threshold up to highest achievable energies. The structure function  $F_3$  violates parity but conserves  $CP$ , therefore it is also  $C$ -parity odd. This feature removes the restriction of Furry's theorem and allows for the odderon direct contribution to  $F_3$  at asymptotic energies: the odderon leads to slowly (e.g., logarithmically<sup>[376]</sup>) growing cross section, while Regge meson exchanges lead to a  $\approx 1/\sqrt{s}$  behavior.

The spin structure function  $g_1$  with polarized proton/ion beams is relevant for the GDH sum rule<sup>[268,269]</sup> that equates the squared anomalous magnetic moment of the proton to an energy-weighted integral over  $g_1$ . Data on  $g_1$  with real photons exist up to  $\sqrt{s} \approx 2 \text{ GeV}$ , allowing to experimentally verify this important sum rule.<sup>[380]</sup> However, the higher-energy part of the integral is estimated using a model-based parametrization of existing deep-inelastic data at low  $Q^2$ <sup>[381-384]</sup> and their extrapolation to the real photon point.<sup>[385,386]</sup> A direct measurement at the GF would serve as an explicit check of that model.

The parity-violating spin structure function  $g_5$  requires a polarized proton/ion beam, and can be obtained from a single-spin asymmetry upon averaging over photon polarization. This



structure function has generally been elusive even in deep-inelastic electron scattering. No data with real photons exist. Together with  $F_3$ , a measurement of  $g_3$  at asymptotic and sub-asymptotic energies will be completely new in terms of addressing PV in the Regge domain: Regge theory operates with  $t$ -channel exchanges which have well-defined parity. In this context, it is worth mentioning the current  $3\sigma$  tension in the unitarity of the Cabibbo–Kobayashi–Maskawa matrix in its top row.<sup>[352]</sup> This tension came about due to a recent re-evaluation of the electroweak radiative  $\gamma W$ -box correction to the neutron and nuclear  $\beta$  decay rate in refs. [387, 388]. The mechanism found in those references is the Regge exchange contribution to the parity-violating structure function  $F_3$ .

## 7.2. Production of Ultrahigh-Energy Gamma Rays

### 7.2.1. Scattering of Secondary Photons Off Stored Relativistic Ions

Consider a secondary photon beam generated by the GF that is back-scattered (if possible, resonantly) from relativistic ions. Nuclear levels have energies of several MeV. We take 15 MeV as reference, as it is done in Section 2.4.3. This places the energy of the secondary photons to  $\approx 15 \text{ MeV}/2\gamma$ , between about 2.6 and 40 keV using the  $\gamma$ -factor range for the LHC and assuming head-on collisions.

An example of a configuration that yields parameters not too far from these is the following. Assume the LHC at injection energy with Li-like Xe beam ( $\gamma \approx 190$ ) using the  $120 \text{ eV } 2s-2p_{1/2}$  transition (similar to the transition proposed for the GF proof-of-principle experiment at the SPS<sup>[7]</sup>). The maximum energy of emitted secondary X-rays in this case will be 46 keV. In the frame of reference of the counter-rotating ion beam these photons will appear to be of 17 MeV energy suitable for excitation of some nuclear levels. The re-emitted gamma radiation from the nuclear level will be Lorentz boosted to 7 GeV in the lab frame. The lifetime of the upper state of the  $2s-2p_{1/2}$  transition in Li-like Xe is 186 ps.<sup>[389]</sup> This extends the 46 keV X-ray emission region to 10 m which is about ten times longer than the focused ion beam region in the IP (see Figure 27). Longer  $2s$  lifetimes of lighter ions limits their efficiency for such a scheme.

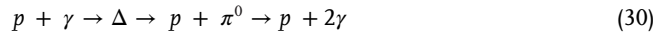
A more efficient although much more expensive approach would be to use a dedicated X-ray FEL facility generating the required X-ray pulses.

If a 15 MeV nuclear resonance decays via photons, with highest accessible relativistic factors, one would produce gamma rays with energies of up to  $\approx 90 \text{ GeV}$  in the lab frame. For most efficient gamma production, one would choose a resonance that decays in the photon channel with a high branching ratio. How many such photons can be produced this way strongly depends on the specific system and the details of experimental arrangements; preliminary estimates show that on the order of  $10^6$  high-energy photons per second could be achievable in favorable scenarios.

### 7.2.2. Scattering of Secondary Photons Off a Proton Beam

To achieve the highest possible photon energies, one may shine secondary GF photons head-on onto the proton beam at the

LHC.<sup>[390,391]</sup> With the inverse Compton scattering process, the energy of the resulting photons will be close to the LHC proton-beam energy 6.5 TeV. However, the cross section of this process is low and we can expect only several such scattering events per hour with the GF beam intensity.<sup>[392]</sup> Another promising scenario with a much higher cross section would be to excite the  $\Delta(1232)$  resonance at  $\approx 300 \text{ MeV}$  in the rest frame of the proton. It will be producing  $\pi^0$ 's and  $\pi^+$ 's which decay in flight:



The incident photon energy must be tuned to  $\omega \approx 300 \text{ MeV}/2\gamma_p \approx 22 \text{ keV}$  for the relativistic factor of the LHC proton beam  $\gamma_p = 7000$ . Such low-energy secondary photons might originate from a lower-energy PSI beam (for example, at the SPS) or by directing the secondary photons on the proton beam at a large relative angle. Either way, the secondary photon beam should be produced not too far from the point at which the collision with the proton beam occurs to have as many secondary photons interacting with the proton beam as possible. Note that since the width of the  $\Delta(1232)$  is 120 MeV one can use a fairly broad secondary photon spectrum, say  $\omega = 260 \pm 60 \text{ MeV}$ . The  $\pi^0$  will be emitted with the energy  $\omega_\pi \approx 2\gamma_p (230 \pm 60) \text{ MeV} \approx (3.2 \pm 0.8) \text{ TeV}$ . These pions will decay within  $\gamma_p \tau_{\pi^0} \approx 6 \times 10^{-13} \text{ s}$  and all this energy will be shared between two photons going within a small angle  $\approx m_\pi/\omega_\pi$ . The cross section for  $\pi^0$  production on top of the resonance is  $\sigma \approx 300 \mu\text{b}$ . The background processes are associated with charged particles, such as pair production (with a cross section of  $\approx 10 \text{ mb}$  for 300 MeV photons) and  $\pi^+$  production, where almost equal amount of  $\pi^0$ 's and  $\pi^+$ 's are produced (the latter live much longer and do not produce photons).

Pion production rate can be estimated as follows. Assuming  $10^{15} \text{ photons s}^{-1}$  (to account for the divergence of the photon beam) colliding with the proton bunch of  $3 \times 10^{10} \text{ protons}^{[13]}$  in a bunch of  $(16 \mu\text{m})^2$  cross section, we have

$$10^{15} \times 3 \times 10^{10} \times \frac{3 \times 10^{-28} \text{ cm}^2}{(16 \times 10^{-4} \text{ cm})^2} \approx 4 \times 10^3 \text{ s}^{-1} \quad (31)$$

The number of photons is double that number. The photon energy distribution in the lab frame is expected to be broad and monochromatization via collimation may not be possible in this case (this will be studied in more detail in future work). The large width of the  $\Delta$  resonance of  $\approx 120 \text{ MeV}$  is of advantage for the number of pions and photons produced: we do not need to tune the secondary photons too precisely and will be integrating over the whole  $\Delta$  peak. The highest attainable energy photon beam of 4 TeV is unprecedented (the fixed-target program COMPASS is limited to below  $\approx 100 \text{ GeV}$  photons). Neutral pions are routinely produced, for example, in pp collisions at the LHC. However, because of the symmetric kinematics, pions and photons are spread over  $4\pi$  solid angle. With the asymmetric kinematics considered here, we will obtain a high-energy photon beam with small divergence.

The very high energy gamma rays (VHEGR) are of interest in astrophysics, so having an intense source of VHEGR with energy up to 4 TeV will help calibrating the detectors for the VHEGR detection and to study VHEGR interactions with matter.

## 8. Production of Isotopes and Isomers for Medicine, Dark Matter Search and Gamma Lasers

Isotope and isomer production via photonuclear reactions is among the important applications of gamma sources; see, for example, refs. [393, 394] for a detailed discussion. The advantages of the GF are, first of all, high photon flux, but also high monochromaticity allowing one, in some cases, to take advantage of resonant cross section enhancement.<sup>[393]</sup>

We consider the production of useful nuclear isotopes and isomers via  $(\gamma, n)$  or  $(\gamma, \gamma')$  reactions from fixed targets containing long-lived nuclei (half-life longer than 1 year).

### 8.1. Production of Medical Isotopes via $(\gamma, n)$ Reactions

Production of medical isotopes via  $(\gamma, n)$  can be realized by either resonantly exciting specific nuclear energy levels beyond the neutron separation threshold or exciting the giant dipole resonance (see Section 4.3) using photons in a broad band. The former approach could be cleaner by taking advantage of photon monochromaticity achievable at the GF and involve less power deposited on the target. The photon bandwidth can be adjusted to match the total width of the excited state predominantly arising from neutron emission. But the resonant cross section is suppressed due to the small gamma emission branching ratio of the excited state. The latter approach could be more effective due to a larger peak cross section and a broader width of the GDR (together resulting in a larger integral cross section), allowing for more photons to be absorbed. This was studied in, for example, ref. [395] employing gamma photons produced by laser photons Compton back-scattered off relativistic electrons at the Canadian light source (CLS); see also Table A2. With orders of magnitude higher photon fluxes at the GF, we can expect a significant improvement of production rates, thus making  $(\gamma, n)$  reaction practical for producing medical isotopes. Radioisotopes which may have better application in nuclear medicine but are not available due to low production rates accompanied with high cost (see, for example, ref. [393]) might become accessible with the advent of the GF. A number of isotopes useful for medicine<sup>[395]</sup> can be produced via  $(\gamma, n)$  reactions; see the examples given in Table 6.

We present an example of producing the  $^{99}\text{Mo}$  medical isotope at the GF via the GDR. The GDR in heavy nuclei have resonance energies  $E_0 \approx 77 \times A^{-1/3} \approx 14$  MeV with widths  $\Gamma_{\text{tot}} \approx 23 \times A^{-1/3} \approx 5$  MeV. Here we can tune the maximal energy of secondary photons at GF to  $E_\gamma = E_0 + \Gamma_{\text{tot}} \approx 19$  MeV and use photons emitted within the  $1/\gamma$  cone, that is, photons with energy between 9.5 and 19 MeV (see Section 1.1), by suitable collimation. The average background photon-attenuation cross section in this energy range is  $\sigma_{\text{bg}} \approx 6$  b, dominated by electron-positron pair production ( $\approx 4.4$  b) and Compton scattering off electrons ( $\approx 1.7$  b).<sup>[352,396]</sup> The peak cross section of the  $^{100}\text{Mo}(\gamma, n)^{99}\text{Mo}$  reaction is  $\sigma_0 \approx 0.15$  b.<sup>[395]</sup> Therefore, the maximal production rates of the  $^{99}\text{Mo}$  isotope can be estimated as

$$p \approx j \frac{\Gamma_{\text{tot}}}{E_0 + \Gamma_{\text{tot}}} \frac{\sigma_0}{\sigma_0 + \sigma_{\text{bg}}} \approx 6 \times 10^{14} \text{ s}^{-1} \quad (32)$$

**Table 6.** Examples of medical isotope production via the  $^{A+1}_Z\text{X}(\gamma, n)^A_Z\text{X}$  reaction.<sup>[393,395]</sup> For produced medical isotopes  $^A_Z\text{X}$ , their ground-state nuclear spins  $I^P$ , half-lives  $T_{1/2}$  and decay modes are provided. Here  $\% \epsilon$  and  $\% \beta^+$  represent probabilities of nuclear decay via electron capture ( $\epsilon$ ) and  $\beta^+$  decay, respectively.  $S_n$  is the neutron-separation energy of the initial nucleus  $^{A+1}_Z\text{X}$ . The data are from ref. [55].

Z	$^{A+1}\text{X}$	$^A\text{X}$	$I^P$	$T_{1/2}$	Decay mode	$S_n$ [keV]
29	$^{65}\text{Cu}$	$^{64}\text{Cu}$	1+	12.7 h	$\% \epsilon + \% \beta^+ = 61.50$ $\% \beta^- = 38.50$	9910.4
42	$^{100}\text{Mo}$	$^{99}\text{Mo}$	1/2+	66.0 h	$\% \beta^- = 100.00$	8294.2
46	$^{104}\text{Pd}$	$^{103}\text{Pd}$	5/2+	17.0 d	$\% \epsilon = 100.00$	10009.2
68	$^{170}\text{Er}$	$^{169}\text{Er}$	1/2-	9.4 d	$\% \beta^- = 100.00$	7256.9
75	$^{187}\text{Re}$	$^{186}\text{Re}$	1-	3.7 d	$\% \beta^- = 92.53$ $\% \epsilon = 7.47$	7360.7
77	$^{193}\text{Ir}$	$^{192}\text{Ir}$	4+	73.8 d	$\% \beta^- = 95.24$ $\% \epsilon = 4.76$	7772.0
79	$^{197}\text{Au}$	$^{196}\text{Au}$	2-	6.2 d	$\% \epsilon + \% \beta^+ = 93.00$ $\% \beta^- = 7.00$	8072

where  $j \approx 10^{17} \text{ s}^{-1}$  is the expected flux of secondary photons produced at the GF. This production rate is reached when almost all photons (after collimation) are absorbed in the target. Therefore, the thickness of an enriched  $^{100}\text{Mo}$  target or multiple thin targets should be greater than the absorption length  $l \approx 1/(\sigma_{\text{bg}} n) \approx 2.8$  cm, where  $n$  is the number density of  $^{100}\text{Mo}$  in the target with a density of  $\approx 10 \text{ g cm}^{-3}$ . After a week of irradiation,  $^{99}\text{Mo}$  isotopes with activities of  $\approx 500$  TBq can be produced. Such activities are a significant improvement compared to those obtained at other facilities including some nuclear reactors.<sup>[397,398]</sup> The worldwide demand of  $^{99}\text{Mo}$  isotopes is  $\approx 9000$  6-day Ci  $^{99}\text{Mo}$  per week,<sup>[399]</sup> where 6-day Ci refers to activities measured 6 days after the end of target processing. Assuming 1 day for the target processing after the 1-week irradiation,  $\approx 2300$  6-day Ci  $^{99}\text{Mo}$  per week, nearly one quarter of the global supply, can be obtained at the GF.

The  $^{99}\text{Mo}$  isotope having a half-life of  $T_{1/2} \approx 65.9$  h decays via  $\beta^-$  to  $^{99m}\text{Tc}$  ( $T_{1/2} \approx 6.0$  h). Therefore,  $^{99}\text{Mo}$  isotopes are mainly used for the production of the  $^{99m}\text{Tc}$ , the most frequently used isomer in nuclear medicine. More examples of producing shorter-lived isomers or isotopes from decay of longer-lived mother isotopes, so-called generators, are listed in ref. [393]. The worldwide demand for  $^{99}\text{Mo}$  is nowadays mainly satisfied by a small number of nuclear reactors via the  $^{235}\text{U}(n, f)^{99}\text{Mo}$  reaction.<sup>[398]</sup> Some nuclear reactors have suffered shutdown for maintenance or breakdowns, leading to shortages or interruptions in the supply of  $^{99m}\text{Tc}$ . Therefore, looking for alternative methods of producing  $^{99}\text{Mo}$  isotopes has become important.

Production rates for other medical isotopes such as  $^{192}\text{Ir}$  and  $^{196}\text{Au}$  of  $\approx 10^{15} \text{ s}^{-1}$  can analogously be derived. Similar numbers of neutrons are also produced from the  $(\gamma, n)$  reaction, thus offering tertiary neutron beams; see also Section 12.4. One convenience of exploiting the GDR is that we may use the same experimental setup for producing many different medical isotopes, since the dependence of resonance energy and width on  $A$  is weak, both proportional to  $A^{-1/3}$ . Multiple thin targets consisting

**Table 7.** Examples of medical isomer production in  ${}^A X(\gamma, \gamma') {}^A m X$  reactions that proceed via an intermediate excited state of energy  $E_e$ .<sup>[393]</sup> The indices “g,” “e,” “m” denote the ground, intermediate excited and final isomeric states, respectively, for which the nuclear spin and parity  $I^P$  are provided. The isomeric state is characterized by the energy  $E_m$  and half-life  $T_{1/2}^m$ , with direct radiative decay via a gamma-ray of energy  $E_d$  and multipolarity  $\lambda L$ . The last column presents decay modes of the isomeric states, which are for the listed cases either isomeric transition (IT), that is, the transition to a lower-lying level of the same nucleus, or  $\beta^-$  decay. The data are from refs. [55, 402].

Z	${}^A X$	${}^A m X$	$I_g^P$	$E_e$ [keV]	$I_e^P$	$E_m$ [keV]	$I_m^P$	$T_{1/2}^m$	$E_d$ [keV]	$\lambda L$	Decay mode
43	${}^{99}\text{Tc}$	${}^{99m}\text{Tc}$	$9/2^+$	1207.26	$(7/2^-)$	142.683	$1/2^-$	6.0 h	2.173	$E3$	%IT = 99.996
									142.63	$M4$	% $\beta^-$ = 0.004
45	${}^{103}\text{Rh}$	${}^{103m}\text{Rh}$	$1/2^-$	357.396	$5/2^-$	39.753	$7/2^+$	56.1 min	39.755	$E3$	%IT = 100
				651.716	$(3/2)^+$						
49	${}^{113}\text{In}$	${}^{113m}\text{In}$	$9/2^+$	1024.28	$5/2^+$	391.699	$1/2^-$	99.5 min	391.698	$M4$	%IT = 100
				1131.48	$5/2^+$						
49	${}^{115}\text{In}$	${}^{115m}\text{In}$	$9/2^+$	933.780	$7/2^+$	336.244	$1/2^-$	4.5 h	336.241	$M4$	%IT = 95.0
				941.424	$5/2^+$						% $\beta^-$ = 5.0
				1078.16	$5/2^+$						
68	${}^{167}\text{Er}$	${}^{167m}\text{Er}$	$7/2^+$	264.874	$3/2^-$	207.801	$1/2^-$	2.3 s	207.801	$E3$	%IT = 100
				531.54	$3/2^+$						
				667.900	$(5/2)^-$						
				745.32	$7/2^-$						
				810.52	$(5/2)^+$						
77	${}^{191}\text{Ir}$	${}^{191m}\text{Ir}$	$3/2^+$	658.90	$(3/2^-)$	171.29	$11/2^-$	4.9 s	41.89	$E3$	%IT = 100

of different atoms can also be used to produce various isotopes simultaneously.

It is noted that specific activity is an important quality criteria of medical isotopes. To reach high specific activity via photoproduction, photons with high flux density  $\Phi$  (not just high fluxes) are required, which can be estimated from  $\sigma\Phi \approx \ln 2/T_{1/2}$ ,<sup>[393]</sup> where  $\sigma$  is the reaction cross section of transmuted the target isotope into the product isotope and  $T_{1/2}$  is half-life of the product isotope. Since the secondary GF photons with high fluxes are mainly emitted within a small cone (see Figure 1), high flux density can be obtained by putting a target close to the gamma source. When high specific activities are required, one may need to use thin targets to avoid significant photon attenuation. Besides using photon beams with high flux density, high specific activity can also be acquired via effectively separating and concentrating the product isotope, for example, through the magnetically activated and guided isotope separation method,<sup>[400]</sup> which can also be applied to preparation of targets containing enriched isotopes.

Not only isotopes, but also nuclear isomers would be copiously produced at the GF via  $(\gamma, n)$  reactions, since nuclei will partially decay to isomeric states after neutron emission. The isomer ratio, that is, ratio of produced nuclei in the isomeric state to those in the ground state, has been studied with many nuclear reactions including  $(\gamma, n)$  via GDR (see, for example, ref. [401]) using bremsstrahlung photons. The knowledge of isomer ratios of different isotopes and their energy dependences could help to reveal the nuclear structure and mechanism of nuclear reactions. But currently available data are scarce and have significant discrepancies.<sup>[401]</sup> Secondary photons at the GF would offer significant improvement in measuring such data compared with bremsstrahlung photons, as a result of better energy resolution and higher photon fluxes.

## 8.2. Production of Nuclear Isomers via $(\gamma, \gamma')$ Reactions

Radioactive isomers relevant to medicine can be produced via  $(\gamma, \gamma')$  reactions. Using the highly monochromatic GF photons, one can selectively excite transitions from the stable or long-lived nuclear ground state to certain higher-energy levels serving as gateway states which will partially decay to the isomeric state directly or by cascade, which is similar to the isomer-depletion process discussed in Section 2.1; see Figure 3. Table 7 lists some isomers relevant for medicine, together with candidate low-lying gateway levels.

To give an example, production of the  ${}^{115m}\text{In}$  can be realized by selectively exciting the 1078 keV transition with a total radiative width  $\Gamma_{\text{rad}} \approx 4.6 \times 10^{-4}$  eV and a branching ratio  $f \approx 0.16$  of decay to the isomeric state.<sup>[55]</sup> Doppler broadening of this transition leads to  $\Gamma_{\text{tot}} \approx 1.2$  eV at room temperature. The photon-attenuation background is dominated by Compton scattering as  $\sigma_{\text{bg}} \approx 10$  b is much larger than the effective cross section  $\sigma_{\text{eff}} \approx \sigma_0 \Gamma_{\text{rad}}/\Gamma_{\text{tot}} \approx 0.42$  b with  $\sigma_0 \approx 1.1 \times 10^3$  b being the resonant photon-absorption cross section neglecting Doppler broadening. The production rate of  ${}^{115m}\text{In}$  can be approximated as

$$p \approx j \frac{\Gamma_{\text{tot}}}{E_\gamma} \frac{\sigma_{\text{eff}}}{\sigma_{\text{eff}} + \sigma_{\text{bg}}} f \approx j \frac{\Gamma_{\text{rad}}}{E_\gamma} \frac{\sigma_0}{\sigma_{\text{bg}}} f \approx 10^9 \text{ s}^{-1} \quad (33)$$

Here, as before,  $E_\gamma$  is the maximal energy of secondary photons at the GF; it is tuned to  $E_\gamma \approx 1078$  keV in this case.

We note that for exciting narrow resonances in cases where Doppler width is larger than the radiative width but the effective cross section  $\sigma_{\text{eff}}$  is still larger than  $\sigma_{\text{bg}}$ , Doppler broadening could allow a larger fraction of photons ( $\Gamma_{\text{tot}}/E_\gamma \approx 10^{-6}$  at room temperature) to be resonantly absorbed leading to higher nuclear isomer production rates as  $p \approx j f \Gamma_{\text{tot}}/E_\gamma$  [see Equation (33)].

**Table 8.** Further examples of isomers for medical applications.<sup>[403]</sup> In these cases, specific gateway levels for production of these isomers have not yet been identified. However, they may potentially be produced via the excitation of PDR or GDR. See Table 7 for explanations of the notations. As additional decay modes, some of these isomers undergo electron capture ( $\epsilon$ ) or  $\beta^+$  decay.

Z	$^A\text{X}$	$^{Am}\text{X}$	$E_m$ [keV]	$J_m^P$	$T_{1/2}^m$	$E_d$ [keV]	$\lambda L$	Decay mode
17	$^{34}\text{Cl}$	$^{34m}\text{Cl}$	146.36(3)	$3^+$	32.0 min	146.36(3)	M3	%IT = 44.6 % $\epsilon$ + % $\beta^+$ = 55.4
25	$^{52}\text{Mn}$	$^{52m}\text{Mn}$	377.749(5)	$2^+$	21.1 min	377.748(5)	E4	%IT = 1.78 % $\epsilon$ + % $\beta^+$ = 98.22
35	$^{80}\text{Br}$	$^{80m}\text{Br}$	85.843(4)	$5^-$	4.42 h	48.786(5)	M3	%IT = 100
36	$^{81}\text{Kr}$	$^{81m}\text{Kr}$	190.64(4)	$1/2^-$	13.1 s	190.46(16)	E3	%IT = 99.9975 % $\epsilon$ = $2.5 \times 10^{-3}$
43	$^{94}\text{Tc}$	$^{94m}\text{Tc}$	76(3)	$(2)^+$	52.0 min	76(3)		% $\epsilon$ + % $\beta^+$ = 100 %IT < 0.1
50	$^{117}\text{Sn}$	$^{117m}\text{Sn}$	314.58(4)	$11/2^-$	14.0 d	156.02(3) 314.3(3)	M4	%IT = 100
72	$^{178}\text{Hf}$	$^{178m}\text{Hf}$	1147.416(6)	$8^-$	4.0 s	88.8667(10)	E1	%IT = 100
78	$^{193}\text{Pt}$	$^{193m}\text{Pt}$	149.78(4)	$13/2^+$	4.3 d	135.50(3)	M4	%IT = 100
78	$^{195}\text{Pt}$	$^{195m}\text{Pt}$	259.077(23)	$13/2^+$	4.0 d	19.8 129.5(2)	M4	%IT = 100

Alternatively, a broad excitation via the PDR or GDR with decay to the isomeric state can be pursued; see examples in **Table 8**. Isomer production via the GDR using ( $\gamma, n$ ) reactions is briefly discussed at the end of Section 8.1. Photoproduction of isomers via ( $\gamma, \gamma'$ ) reactions was investigated employing photons Compton back-scattered off relativistic electrons, and the obtained cross sections are larger for photons in the PDR energy range compared to GDR.<sup>[394]</sup>

There exists a maximum cross section between 5 and 10 MeV on the order of mb with a broad width on the order of MeV, which lies in the PDR energy range; see Section 4.2. It is demonstrated in ref. [394] that production of  $^{99m}\text{Tc}$ ,  $^{103m}\text{Rh}$ ,  $^{113m}\text{In}$ , and  $^{115m}\text{In}$  isomers with activities of more than 10 mCi can be realized by use of gamma rays from laser-electron Compton scattering with photon fluxes of  $10^{13} \text{ s}^{-1}$  and 6-h irradiation. The achieved activity is generally sufficient for medical imaging but is still inadequate for therapeutic applications. With nearly four orders of magnitude improvement in photon fluxes at the GF, isomers with considerably higher activities can be produced thus meeting the requirement for therapeutic applications. We can tune the maximal energy of secondary photons at the GF to a few hundred keV above the neutron-separation threshold to cover the PDR. Using photons emitted within  $\approx 1/\gamma$  cone (so roughly 1/2 of all secondary photons, see Section 1.1), production rates of these isomers could reach  $\approx 10^{13} \text{ s}^{-1}$ .

Returning to the example of  $^{115m}\text{In}$  production discussed above, it can also be realized by use of photons in the PDR energy range, about 5 to 10 MeV. In this energy range, the average background photon-attenuation cross section is  $\sigma_{\text{bg}} \approx 6 \text{ b}$  and the integrated cross section of the  $^{115}\text{In}(\gamma, \gamma')^{115m}\text{In}$  reaction is around  $5 \times 10^{-3} \text{ b MeV}$ .<sup>[394]</sup> Following an estimate similar to that for isotope-production rates in Section 8.1, we find that production of  $\approx 10^{13} \text{ s}^{-1}$  of  $^{115m}\text{In}$  can be achieved at the GF, when almost all photons (after collimation) are absorbed in a  $^{115}\text{In}$  target

or multiple thin targets with total thickness greater than the absorption length  $l \approx 4.4 \text{ cm}$ .

In this case, the production rate of the isomer of interest is higher when using broadband excitation rather than the narrow resonance, by roughly four orders of magnitude. The isomer-production rate corresponds to activities of produced nuclear isomers after irradiating for a long time comparable to  $T_{1/2}$  of the isomeric state.

Besides medical applications, nuclear isomers were recently proposed as detectors for certain kinds of dark matter which could induce collisional deexcitation of the isomers; see **Table 9**.<sup>[404]</sup> We note that isomers listed in Table 9 are not the only candidates for dark matter search. The GF can produce a range of nuclear isomers with larger quantities accessible, including heavier isomers whose larger nuclear radii allow deexcitation to be induced by smaller momentum exchange during collision with dark matter particles.<sup>[404]</sup> Nuclear isomers have also been suggested for building gamma-ray lasers (see Section 9).

Heating due to the high flux of gamma rays is expected to be a tractable problem with above reactions, since there are several applicable heat-dissipation techniques, for example, using a stack of multiple thin targets.<sup>[393]</sup>

## 9. Induced Gamma Emission and Gamma Lasers

Realization of stimulated photon emission in the gamma range has been an outstanding challenge to the community for many years. Many different proposals have been contemplated<sup>[405]</sup>; however, only a handful of schemes can be considered realistic (and none have been realized up till now). The advent of the GF motivates an examination of whether this facility may bring a gamma laser closer to reality.

There are two main groups of gamma-ray laser (graser) proposals. One suggests building a recoilless gamma-ray laser<sup>[405,406]</sup>

**Table 9.** Isomers for dark matter detection.<sup>[402,404]</sup> See Table 7 for explanations of the notations.

Z	<sup>A</sup> X	$E_m$ [keV]	$I_m^p$	$T_{1/2}^m$	$E_d$	$\lambda L$	Decay mode
56	<sup>137</sup> Ba	661.659(3)	11/2 <sup>-</sup>	2.55 min	378.0(4) 661.657(3)	E5 M4	%IT = 100
71	<sup>177</sup> Lu	970.175(3)	23/2 <sup>-</sup>	160.4 d	115.868(3)	E3	% $\beta^-$ = 78.6(8) %IT = 21.4(8)
72	<sup>178</sup> Hf	2446.09(8)	16 <sup>+</sup>	31 y	12.7(2) 309.50(15) 587.0(1)	M4(+E5) E5	%IT = 100
73	<sup>180</sup> Ta	77.1(8)	9 <sup>-</sup>	$> 1.2 \times 10^{15}$ y			

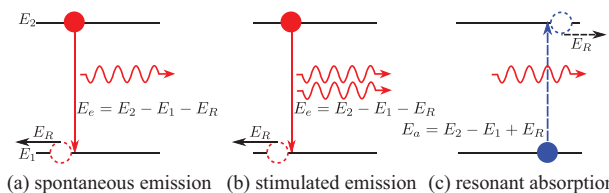
using nuclei incorporated in a crystal. The reason to use a crystal is that the Mössbauer effect may mitigate the issue of the Doppler broadening of the transition which could significantly suppress the stimulated emission cross section. But this meets the so-called graser dilemma, where high intensity of pumping required for creating population inversion, that is, more nuclei in the upper lasing state than in the lower lasing state, could be destructive to other conditions for stimulated emission gain, including the Mössbauer and Bormann effects. In order to relax the population inversion requirements, an approach was proposed<sup>[407,408]</sup> to suppress resonant absorption for the Mössbauer nuclear transitions of the ions placed in a lattice. This can be done via coherent optical driving of electronic transitions of these ions and exploiting the hyperfine coupling between the nuclear and electronic degrees of freedom. These concepts are reminiscent of the physics discussed in Section 2.3.

We note that Mössbauer effect works for transitions with energy below  $\approx 180$  keV. Candidate low-energy gamma transitions may be selected from a list in ref. [409].

We highlight here two examples of graser proposals benefiting from the Mössbauer effect. It has been proposed to build a graser based on collective excitations of <sup>57</sup>Fe Mössbauer nuclei, also known as nuclear excitons, in a nuclear forward scattering setup.<sup>[410]</sup> There is also a proposal for a VUV laser based on the 8 eV nuclear transition between the ground and isomeric states of <sup>229</sup>Th ions doped in a VUV transparent crystal.<sup>[411]</sup> While pumping of the isomer can be done with a conventional VUV laser, Zeeman splitting induced by an external magnetic field or electric quadrupole splitting in the crystal result in population inversion for the lasing transition between specific hyperfine sublevels.

The other group of proposals suggest building a graser with the assistance of recoil,<sup>[412,413]</sup> which can eliminate the requirement of population inversion due to reduced overlap between the photon-absorption lineshape and photon-emission lineshape. The idea is that if the recoil energy  $E_R$  is larger than the Doppler width of the transition, emitted photons would not be absorbed by the nucleus in the ground (initial) state, but they would still stimulate deexcitation of an excited nucleus; see **Figure 28**. However, implementation of this scheme requires cooling to suppress Doppler broadening in order to get acceptable stimulated emission gain.

In the two-level pumping scheme with hidden population inversion,<sup>[413]</sup> the photon intensity required for pumping is es-



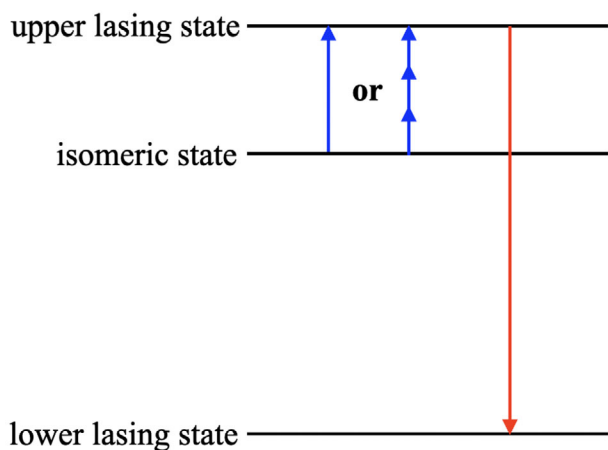
**Figure 28.** The influence of recoil on stimulated emission and resonant absorption.  $E_1$  and  $E_2$  are the level energies. The resonant gamma-ray energy for spontaneous and stimulated emission  $E_e$  is lower than  $E_2 - E_1$  by the recoil energy  $E_R$ , while the gamma-ray energy required for resonant absorption  $E_a$  is higher than the internal energy difference, again, by the recoil energy. Thus, the emitted photons are detuned from resonance and are not readily absorbed.

timated to be  $\geq 10^{30}$  ph cm<sup>-2</sup> s<sup>-1</sup> keV<sup>-1</sup>) using samples cooled down to 10  $\mu$ K.<sup>[414]</sup>

Many graser proposals involve using nuclear isomers; see, for example, **Table 10**. A detailed compilation of nuclear isomers with half-lives  $\geq 10$  ns is provided in ref. [402], though possible usages of these isomers are not underlined. Nuclei potentially valuable for realizing a gamma-ray laser based on the concept of hidden population inversion are tabulated in ref. [415]. High photon fluxes from the GF will help produce copious amount of candidate isomers. High tunability and high resolution of the gamma beams could help characterize the samples during the isomer-separation process before incorporating concentrated isomers into a crystal. The GF may also assist in finding optimal candidate nuclei such as nuclei with small energy difference between the isomeric state and an upper lasing state, where an X-ray or even optical laser can be used for pumping, see the energy level structure suggested in **Figure 29**. Here, an isomeric state with a lifetime long enough to enable accumulation of isomers and their incorporation into a host crystal is used. The isomer is then excited via a single-photon or a multiphoton laser-driven transition to an upper lasing state. A likely difficulty with the latter is that multiphoton transitions are strongly suppressed; see Section 4.3. Two examples, <sup>144</sup>Pr and <sup>152</sup>Eu, exhibiting such energy level structures are shown in **Figure 30**. Here, the required excitation energy is relatively low (about 40 keV for <sup>144</sup>Pr and 20 keV for <sup>152</sup>Eu); photons at this energy may soon become available at XFEL facilities. However, the main drawback remains that such transitions have narrow radiative widths of the upper lasing state. This holds particularly true for <sup>152</sup>Eu. Therefore, it may be

**Table 10.** Isomers potentially useful for gamma-ray lasers.<sup>[416,417]</sup> See Table 7 for explanations of the notations.

Z	<sup>A</sup> X	E <sub>m</sub> [keV]	I <sub>m</sub> <sup>P</sup>	T <sub>1/2</sub> <sup>m</sup>	E <sub>d</sub>	λL	Decay mode
27	<sup>60</sup> Co	58.59(1)	2 <sup>+</sup>	10.5 min	58.603(7)	M3 + (E4)	%IT = 99.75(3) %β <sup>-</sup> = 0.25(3)
70	<sup>169</sup> Yb	24.1999(16)	1/2 <sup>-</sup>	46 s	24.20(2)	E3	%IT = 100
72	<sup>178</sup> Hf	2446.09(8)	16 <sup>+</sup>	31 y	12.7(2)	M4(+E5)	%IT = 100
					309.50(15)	E5	
					587.0(1)	E3	
72	<sup>177</sup> Hf	2740.02(15)	37/2 <sup>-</sup>	51.4 min	214	E3	%IT = 100
72	<sup>179</sup> Hf	1105.74(16)	25/2 <sup>-</sup>	25.0 d	21.01(12)	M2	%IT = 100
					257.37(15)	E3	
73	<sup>180</sup> Ta	77.1(8)	9 <sup>-</sup>	> 1.2 × 10 <sup>15</sup> y			
77	<sup>192</sup> Ir	56.720(5)	1 <sup>-</sup>	1.45 min	56.71(3)	E3	%IT = 99.9825 %β <sup>-</sup> = 0.0175

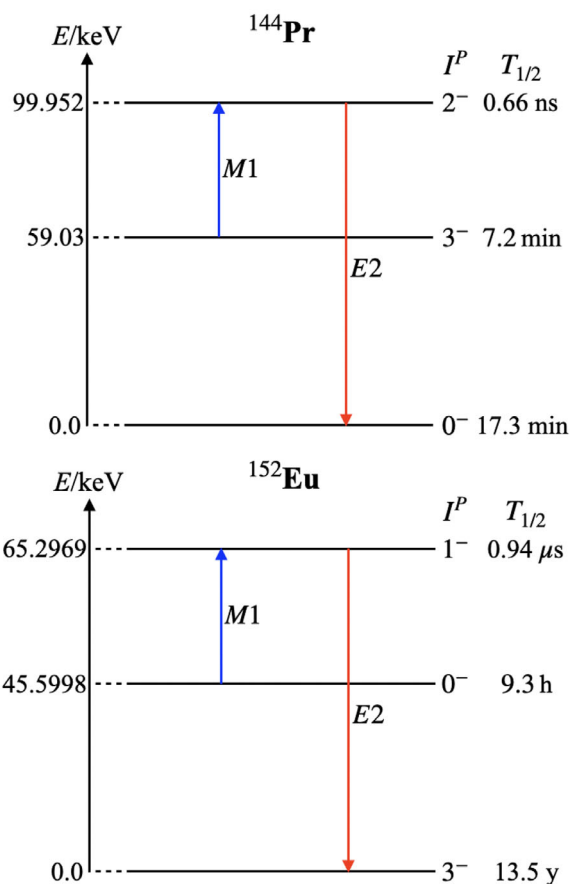


**Figure 29.** A gamma-ray laser scheme.<sup>[406]</sup> After a large number of isomers are produced, the isomeric state is excited to an upper lasing state via a single-photon or multiphoton process indicated by the blue arrows. Deexcitation from the upper lasing state to the lower lasing state is shown as the red arrow.

difficult to realize effective pumping from the isomeric state to the upper lasing state.

For graser schemes where the required transition energy cannot be reached by X-ray lasers, the GF may be utilized for pumping, such as transferring isomers to an upper lasing state. We note that secondary photons with total fluxes of  $\approx 10^{17}$  photons  $s^{-1}$ , uniformly distributed over the entire energy spectrum, at the GF consist of pulses having fluxes of  $10^{10}$  photons per pulse at a repetition rate of  $\approx 10$  MHz. The pulse duration is typically  $\approx 100$  ps and can be reduced to 30 fs limited by the transverse size of the ion beam. The strong energy-angle correlation of GF photons, see Section 1.1, may allow application of the Borrmann effect,<sup>[406]</sup> that is, minimized photon absorption when photons are incident at special angles satisfying the Bragg law, to alleviate heating problems.

To summarize, the GF can help facilitate research on induced emission and lasing with nuclear transitions, although, a clear path to a graser does not seem to be in sight as yet.



**Figure 30.** Examples of nuclear isomers for a prospective gamma-ray laser; see also Figure 29.

## 10. Gamma Polarimetry

### 10.1. Polarimetry with Narrow Resonances

Narrow-band GF photons in combination with polarized nuclear-target technology open a possibility to perform

polarimetry using the target as a polarization filter. To this end, the energy of the GF photons should be tuned in resonance with a gamma transition in the target nucleus.

Suitable transition can be found in the  $^{13}\text{C}$  ( $I^P = 1/2^-$  for the stable ground state; see also Figure 8), which can be made into a polarized target.<sup>[418]</sup> For example, there is an  $E1$  transition to an  $I^P = 1/2^+$  state at 3.09 MeV that has a radiative width of 0.43 eV and radiatively decays back to the ground state. There is also an  $M1$  transition to an excited  $I^P = 1/2^-$  state at 8.86 MeV that has a width of 150 keV. The upper state of this transition lies above the neutron-separation energy for  $^{13}\text{C}$  (4.9 MeV) and predominantly decays by neutron emission to the ground state of  $^{12}\text{C}$  (the ground state is the only possible state of the resultant  $^{12}\text{C}$  because the excited states of this nucleus lie sufficiently high).

The resonant cross section for a closed transition is [cf., Equation (B1)]

$$\sigma \simeq \frac{\lambda'^2}{2\pi} \quad (34)$$

where  $\lambda'$  is the wavelength in the ion frame. For the 3.09 MeV  $E1$  transition,  $\sigma \approx 260$  b ( $1 \text{ b} = 10^{-24} \text{ cm}^2$ ) is large enough that it is feasible to construct a target comprising multiple absorption lengths for resonant photons. The expected asymmetry for absorption of circularly polarized photons on a  $1/2 \rightarrow 1/2$  transition is 100%, and thus such a system can be an efficient circular analyzer, perhaps only limited in precision by the counting statistics of the gamma rays. One should note in this respect that the resonance will be narrower than the spectral width of the gamma beam, so only a fraction of the photons will, in fact, be resonant, see Appendix B.

This should not be a problem for the broader 8.86 MeV  $M1$  resonance; however, the resonant cross section is some five orders of magnitude smaller because the width is dominated by decay via neutron emission rather than gamma transition and because of the smaller photon wavelength.

Due to these factors, polarimetry may need to rely, instead of photon-transmission measurements, on the detection of reaction products (neutrons or noncollinear photons).

## 10.2. Other Polarimetric Techniques

Polarization measurements of gamma and X-rays have a long tradition in many branches of modern physics. For example, a number of polarization-sensitive studies were performed in astrophysics,<sup>[419,420]</sup> atomic, nuclear and plasma physics.<sup>[421–423]</sup> Depending on the energy of the photons, the photoelectric effect, Compton effect, and electron-positron pair production are typically employed in these experiments. In addition, in the recent years, Bragg scattering was successfully used for high-precision polarization measurements in the keV energy range.<sup>[424–426]</sup>

During the last two decades, a number of experiments were performed also to study linear polarization of photons, emitted in relativistic collisions at ion storage rings.<sup>[422,427,428]</sup> These measurements usually employ the polarization sensitivity of Compton scattering of light by (quasi-free) electrons. Namely, the angular distribution of Compton-scattered photons is defined by the direction of the linear polarization of incident radiation, as predicted by the well-known Klein–Nishina formula.<sup>[427]</sup> In order

to measure this angular distribution and, hence, to determine the linear polarization one usually employs solid-state position sensitive detectors. These Compton detectors allow (linear) polarization measurements in the energy range of about 10 keV to 10 MeV.<sup>[429]</sup> Above 10 MeV, pair-production polarimetry can be used.<sup>[430,431]</sup>

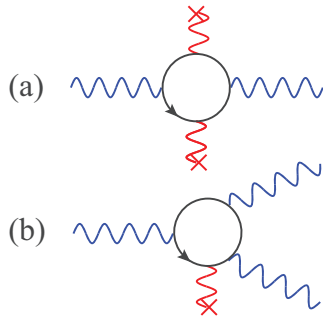
In contrast to linear polarization measurements, less progress has been made in the development of detectors for the measurement of circular polarization of X- and gamma rays. Due to the absence of a polarimetry technique which could be combined with gamma-ray imaging, for example, no circular polarization measurements have been reported in gamma-ray astronomy. In atomic and nuclear physics, however, the experimental approach based on Compton scattering off magnetized solid targets has been applied during the last decades. Moreover, a combined measurement of Compton scattered photons and subsequent bremsstrahlung of the recoiled electron has been recently proposed as a novel approach to circular polarimetry.<sup>[432]</sup> It is expected that this novel approach will allow accurate studies of circular polarization of X- and gamma rays with energies up to several tens of MeV.

The  $\Delta(1232)$  resonance is a dominant feature of the nucleon-excitation spectrum for photon energies  $\omega \approx 300$  MeV (in the photon-proton center of momentum frame). It can be used to analyze the circular photon polarization. It is common to describe the photoexcitation of  $\Delta(1232)$  by the value of the resonance photoabsorption amplitudes with the parallel and the antiparallel helicity configuration,  $A_{3/2,1/2}$ . For these, Ref. [352] gives the values  $A_{3/2} = -0.255(7) \text{ GeV}^{-1/2}$  and  $A_{1/2} = -0.135(7) \text{ GeV}^{-1/2}$ .<sup>[352]</sup> Note that the uncertainties are relatively large due to averaging over different theoretical analyses which individually have much smaller uncertainties, comfortably within 2–3% for  $A_{1/2}$  and about half that value for  $A_{3/2}$ . The model dependence stems from the separation of the experimental data into the resonant and the non-resonant parts, a procedure that is model-dependent. Their ratio amounts to  $|A_{3/2}|/|A_{1/2}| \approx 1.89$ , resulting in the asymmetry  $\frac{|A_{3/2}|^2 - |A_{1/2}|^2}{|A_{3/2}|^2 + |A_{1/2}|^2} \approx 0.56$ . The helicity-dependent total cross section integrated over the full spectrum is relevant for the GDH sum rule, see Section 4.7.

Development of precision polarimetry and spectropolarimetry (a combination of polarimetry and spectroscopy) at the GF, would open novel possibilities for fundamental-physics experiments such as studying PV in the vicinity of nuclear gamma transitions (Section 4.11) and measurement of vacuum-birefringence effects (Section 11.1).

## 11. Quantum Vacuum Effects

The quantum vacuum amounts to a highly nontrivial state, characterized by the omnipresence of fluctuations of virtual particles. While the microscopic theory of QED does not provide for a direct tree-level interaction among photons, quantum vacuum fluctuations induce effective nonlinear couplings among electromagnetic fields.<sup>[433–436]</sup> At zero field, the quantum vacuum is characterized by translational invariance and the absence of any preferred direction. Conversely, an external electromagnetic field generically introduces a preferred direction for charged particles, and, if inhomogeneous, also breaks translational invariance. Via



**Figure 31.** Lowest-order Feynman diagrams of typical quantum vacuum effects, giving rise to a) vacuum birefringence and b) photon splitting. The blue wiggly lines are probe photons and the red wiggly lines ending at crosses denote couplings to the prescribed electromagnetic field.

the charged particle-antiparticle fluctuations coupling to the external electromagnetic field, this preferred direction can also impact probe photon propagation and give rise to nonlinear QED effects such as vacuum birefringence and photon splitting; see **Figure 31** for the corresponding Feynman diagrams at one-loop order. See also the recent reviews<sup>[437,438]</sup> and references therein.

Here, we briefly discuss the perspectives of studying quantum vacuum effects at the GF, using the prominent signatures of vacuum birefringence (in magnetic and laser fields) and photon splitting (in atomic fields) as illustrative examples. Both effects arise from an effective four-photon interaction mediated by an electron-positron fluctuation<sup>[439–442]</sup>; confer **Figure 31**. The former scales quadratically and the latter linearly with the background field. Besides, we comment on quasi-elastic photon scattering.

### 11.1. Vacuum Birefringence

Linearly polarized probe photons (energy  $\omega$ ) traversing a strong pump field ( $\vec{\mathcal{E}}, \vec{\mathcal{B}}$ ) can pick up an ellipticity if their polarization vector has a nonvanishing overlap with the two distinct polarization eigenmodes imprinted on the quantum vacuum by the pump field.<sup>[443]</sup> See **Figure 31a** for the corresponding Feynman diagram.

So far, this fundamental effect induced by quantum vacuum fluctuations has never been directly verified in laboratory experiments using macroscopic fields; see the review<sup>[444]</sup> and references therein. Typical proposals for measuring vacuum birefringence in a laboratory experiment envision the effect to be induced either by A) quasi-constant static magnetic field, or B) a counter-propagating high-intensity laser pulse.

Given that the following conditions hold<sup>[445]</sup>

$$\left\{ \left( \frac{e\mathcal{E}}{m_e^2} \right)^2, \left( \frac{\Omega}{m_e} \right)^2, \frac{\omega\Omega}{m_e^2}, \left( \frac{e\mathcal{E}\omega}{m_e^3} \right)^2 \right\} \ll 1 \quad (35)$$

where  $\hbar = c = 1$ , the vacuum-birefringence phenomenon can be studied on the basis of the leading contribution to the renowned Heisenberg–Euler effective Lagrangian.<sup>[434,435]</sup> Here,  $\mathcal{E} = \max\{|\vec{\mathcal{E}}|, |\vec{\mathcal{B}}|\}$ ,  $\Omega$  denotes the typical frequency scale of variation of the pump field,  $e$  is the elementary charge and  $m_e$  is the electron mass.

In the same parameter regime, the polarization-sensitive absorption coefficients associated with the principle possibility of electron-positron pair production in the presence of the background field are exponentially suppressed with  $m_e^2/(e\mathcal{E}) \gg 1$  for  $\omega \ll m_e$  and  $m_e^3/(e\mathcal{E}\omega) \gg 1$  for  $\omega \gg m_e$ ; confer, for example, refs. [446, 447].

#### 11.1.1. Quasi-Constant Magnetic Field

First, we consider the effect of vacuum birefringence induced by a quasi-constant static magnetic field  $\vec{\mathcal{B}}$ . In this case, probe photons polarized parallel  $\parallel$  (perpendicularly  $\perp$ ) to the plane spanned by their wave vector and the direction of  $\vec{\mathcal{B}}$  experience different refractive indices. Given that the conditions (35) are met, for probe photons propagating perpendicularly to  $\vec{\mathcal{B}}$  these refractive indices are given by<sup>[448]</sup>

$$\begin{cases} n_{\parallel} \\ n_{\perp} \end{cases} \simeq 1 + \frac{\alpha}{\pi} \left( \frac{e\mathcal{B}}{m_e^2} \right)^2 \frac{1}{90} \begin{cases} 7 \\ 4 \end{cases} \quad (36)$$

with fine-structure constant  $\alpha \simeq 1/137$ .

Letting initially linearly polarized photons having an equal overlap with both polarization eigenmodes ( $\parallel, \perp$ ) traverse a constant magnetic field extending over a length  $l$ , an ellipticity characterized by the phase difference  $\Phi = \omega l(n_{\parallel} - n_{\perp})$  between the two polarization components is induced. The explicit expression for the accumulated phase difference is<sup>[449]</sup>

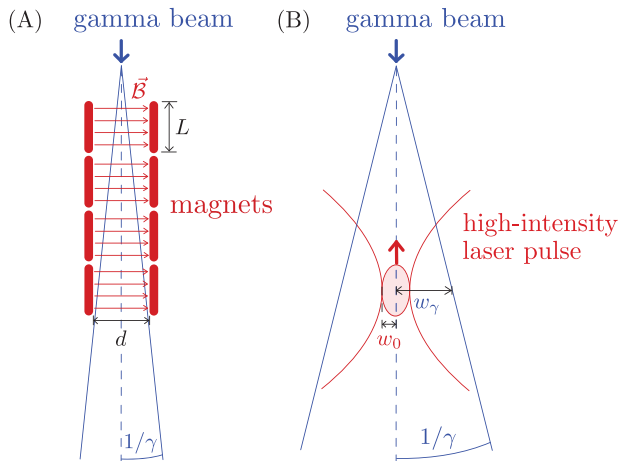
$$\Phi \simeq \omega l \frac{\alpha}{30\pi} \left( \frac{e\mathcal{B}}{m_e^2} \right)^2 \quad (37)$$

Equation (37) shows that the effect scales quadratically with the magnetic field strength and linearly with the energy of the probe photons and their propagation distance in the magnetic field. At the same time, the birefringence property of the polarized quantum vacuum results in signal photons scattered into a mode polarized perpendicularly to the incident probe light: for the case of a static quasi-constant magnetic field as considered in this subsection, the number of polarization flipped signal photons is given by  $N_{\perp} \simeq (\Phi/2)^2 N$ , where  $N$  denotes the number of gamma photons available for probing the effect.

The GF will enable such a vacuum-birefringence experiment with a probe-photon energy as high as  $\omega \simeq 400$  MeV. The driving magnetic field could be provided by a sequence of LHC dipole magnets, delivering a magnetic field of  $B \simeq 8.3$  T over a length of  $L \simeq 14.3$  m each;<sup>[450]</sup> the effective diameter  $d$  of the bore for traversing light is about  $d \simeq 45$  mm. In this case, we have  $(\Omega/m_e)^2 \simeq \omega\Omega/m_e^2 \simeq 0$ ,  $(e\mathcal{B}/m_e^2)^2 \simeq 3.54 \times 10^{-18}$ , and  $(e\mathcal{B}\omega/m_e^3)^2 \simeq 2.17 \times 10^{-12}$  fully compatible with Equation (35).

To achieve gamma-photon energies up to  $\omega \simeq 400$  MeV, the Lorentz factor  $\gamma$  which effectively governs the generation of the high-energy gamma beam in the GF needs to be as large as  $\gamma \simeq 3000$ ; confer Section 1.1 above. As the opening angle of the gamma beam is given by  $\approx 1/\gamma$ , the bore diameter of the magnet implies a maximum length  $l_{\max} \approx (d/2)\gamma \simeq 67.5$  m of the magnetic field provided by LHC magnets through which the full gamma beam could travel. In turn, we can envision the use of up to four LHC dipole magnets resulting in  $\omega l \simeq 1.16 \times 10^{17}$ ,





**Figure 32.** Graphical depiction of the two scenarios envisioned for the detection of QED vacuum birefringence at the Gamma Factory as discussed in the text. In scenario (A) the birefringence phenomenon is induced by the quasi-constant static magnetic field provided by LHC dipole magnets. In scenario (B) the effect is driven by a counter-propagating focused high-intensity laser pulse.

see **Figure 32A** for an illustration. For these parameters we obtain a small (but potentially measurable, see Section 10) value of  $\Phi \simeq 3.18 \times 10^{-5}$ .

We note that this value is about an order of magnitude larger than the one predicted to be accessible in the head-on collision of a state-of-the-art petawatt-class high-intensity-laser and free-electron-laser (FEL) pulses of  $\omega \simeq \mathcal{O}(10)$  keV.<sup>[451–455]</sup> For X-rays of  $\omega \simeq \mathcal{O}(10)$  keV the possibility of measuring such tiny ellipticities has been demonstrated experimentally.<sup>[424–426]</sup> While these X-ray techniques cannot be used at 400 MeV, in the latter parameter regime pair-production polarimetry may be used.<sup>[430,431]</sup> See refs. [456, 457] for proposals to measure magnetic-field-induced vacuum birefringence with gamma photons adopting somewhat different experimental parameters.

The advantage of using a static magnetic field to drive the vacuum birefringence phenomenon is that essentially all gamma photons traverse the magnetic field. In turn, the associated number of polarization-flipped signal photons  $N_{\perp}$  scales directly with the total number of photons constituting the gamma beam, and thus is ultimately limited (among other factors) by the repetition rate of the gamma pulses. Conversely, in the scenario utilizing a laser pulse to induce the birefringence phenomenon the repetition rate of the high-intensity laser is the limiting factor; see below.

### 11.1.2. High-Intensity Laser Pulse

Alternatively, the birefringence signal could be driven by a high-intensity laser field;<sup>[458,459]</sup> see **Figure 32B**. In such a scenario, the birefringence signal is predominantly induced in the interaction region where the gamma probe collides with the focused high-intensity laser pulse reaching its peak field strength. Outside the focus, the field strength of the high-intensity pump drops rapidly.

State-of-the-art high-intensity lasers of the petawatt-class typically deliver pulses of energy  $W = \mathcal{O}(10)$  J and duration  $\tau =$

$\mathcal{O}(10)$  fs at a wavelength of  $\lambda = \mathcal{O}(1)$   $\mu\text{m}$  and a repetition rate of  $\mathcal{O}(1)$  Hz. These pulses can be focused to a waist radius of  $w_0 \gtrsim \lambda$ . In turn, the maximum frequency scale of variation of the pump field is given by  $\Omega = 2\pi/\lambda$ . For our explicit example, we choose the parameters characterizing a commercial 300 TW Titanium Sapphire laser system, such as the one installed at the Helmholtz International Beamline for Extreme Fields at the European XFEL:  $W = 10$  J,  $\tau = 30$  fs,  $\lambda = 800$   $\mu\text{m}$  and a repetition rate of 1 Hz focused to  $w_0 = 1$   $\mu\text{m}$ . The associated Rayleigh range is  $z_R = \pi w_0^2/\lambda$ . Assuming the high-intensity laser field to be well-described as pulsed paraxial fundamental Gaussian beam, the electric peak field strength  $\mathcal{E}_0$  in its focus can be expressed in terms of the pulse energy, pulse duration and waist radius as<sup>[460]</sup>

$$\mathcal{E}_0^2 \simeq 8\sqrt{\frac{2}{\pi}} \frac{W}{\pi w_0^2 \tau} \quad (38)$$

For the laser parameters given above and  $\omega \simeq 400$  MeV, the dimensionless quantities in Equation (35) are  $(\Omega/m_e)^2 \simeq 9.2 \times 10^{-12}$ ,  $(e\mathcal{E}_0/m_e^2)^2 \simeq 1.46 \times 10^{-7}$ ,  $\omega\Omega/m_e^2 \simeq 2.4 \times 10^{-3}$  and  $(e\mathcal{E}_0\omega/m_e^3)^2 \simeq 0.09$ . These values suggest that in this parameter regime the size of the attainable vacuum birefringence signal can still be reliably estimated from the leading contribution to the Heisenberg–Euler effective Lagrangian.

At the GF, the collision point of the gamma beam with the high-intensity laser beam should be sufficiently separated from the source of the gamma photons such that the radius  $w_{\gamma}$  of the gamma beam in the interaction region with the high-intensity laser pulse generically fulfills  $w_{\gamma} \gg w_0$ ; confer also **Figure 32B** and ref. [461]. Even though this implies that only a fraction of the gamma photons will actually see the high-intensity laser focus, focusing the latter less tightly to  $w_0 \approx w_{\gamma}$  is not an option: as the ellipticity is proportional to  $\mathcal{E}_0^2 \approx 1/w_0^2$  [see **Figure 32a** and Equation (39) below], an increase of  $w_0$  would immediately reduce the effect. Moreover, the GF is expected to provide gamma pulses of duration  $T \gtrsim 160$  fs.

Given that  $w_{\gamma} \gg w_0$  and the pulse duration of the gamma beam meets the criterion  $T \gg \{\tau, z_R\}$ , which is true for the parameters of the GF, the phase difference accumulated by the gamma beam can be expressed in a form similar to Equation (37), yielding<sup>[445]</sup>

$$\Phi \simeq \omega z_R \frac{2^{1/4} \alpha}{30} \left( \frac{e\mathcal{E}_0}{m_e^2} \right)^2 e^{\frac{1}{2} \left( \frac{8z_R}{\tau} \right)^2} \text{erfc}^{1/2} \left( \frac{8z_R}{\tau} \right) \quad (39)$$

with complementary error function  $\text{erfc}(x) = 1 - \text{erf}(x)$ . We emphasize that this parameter regime even seems to be particularly beneficial for high-intensity laser driven vacuum-birefringence experiments: given that the conditions  $T \gg \tau$  and  $w_{\gamma} \gg w_0$  are met, the experiment is essentially insensitive to the shot-to-shot fluctuations inherent to high-intensity laser systems resulting in spatio-temporal offsets of  $\mathcal{O}(w_0)$  of the position of the high-intensity laser focus. Variations of this order just change the location of the high-intensity laser focus within the forward cone of the gamma probe and thus do not impact the signal; confer also **Figure 32B**.

Similarly to the result (37) for a constant magnetic field, the phase difference (39) scales quadratically with the field strength of the pump field, and linearly with both  $\omega$  and the typical extent of the pump field along the propagation direction of the probe.

This extent is typically set by the Rayleigh range  $z_R$  of the high-intensity laser.

Plugging the above parameters into Equation (39), we obtain  $\Phi \simeq 0.13$ , which is much larger than the analogous value obtained for the case of a static magnetic field discussed in Section 11.1.1. Assuming in addition that the pulse duration and beam radius of the gamma beam in the interaction region are given by  $T \simeq 160$  fs and  $w_\gamma \simeq 20$   $\mu\text{m}$ , we find  $N_\perp/N \simeq 2.07 \times 10^{-6}$  for the ratio of the polarization-flipped signal photons and the number of gamma photons  $N$  available for probing the effect; note that in the present scenario  $N_\perp/N = (\tau/T)(w_0/w_\gamma)^2(\Phi/2)^2$ .<sup>[445]</sup>

However, we emphasize once again that in contrast to the case of a static magnetic field, for the scenario involving a high-intensity laser pulse, only a fraction of the total number of gamma photons provided by the GF is available for probing the vacuum birefringence phenomenon: in this case the repetition rate of the experiment is limited by the repetition rate of  $\mathcal{O}(1)$  Hz of the high-intensity laser.

Higher laser intensities and/or larger gamma photon energies would even allow for experimental probes of vacuum birefringence in the parameter regime characterized by  $(e\mathcal{E}\omega/m^3)^2 \gtrsim 1$ , violating the condition (35). The theoretical study of quantum vacuum signatures in this parameter regime requires insights beyond the Heisenberg–Euler effective Lagrangian. Vacuum birefringence in this parameter regime<sup>[462–465]</sup> can be reliably studied resorting to the photon-polarization tensor evaluated in the background of the pump field.

Finally, we note that aside from the prospect of directly verifying a fundamental QED prediction for the first time, a precision measurement of the ellipticity constituting the signal of vacuum birefringence in Equations (37) and (39) at the GF would also constitute a sensitive probe for New Physics beyond the standard model of particle physics. The latter may leave an imprint on the refractive index of the vacuum resulting in deviations from the standard model prediction; see, for example, the recent review<sup>[466]</sup> and references therein. For a survey of the potential of the GF for searches of axion like particles, see ref. [467].

## 11.2. Photon Splitting

In contrast to vacuum birefringence, the effect of photon splitting in atomic fields mediated by an electron-positron fluctuation<sup>[468–471]</sup> has already been successfully observed in a dedicated laboratory experiment employing probe photons in the energy region of 120–450 MeV.<sup>[472]</sup> See Figure 31b for the corresponding Feynman diagram. At present, the experiment and the theory are consistent within the achieved experimental accuracy.<sup>[471]</sup>

The high flux of gamma photons at the GF as well as the possibility of a precise tuning of their energy will allow for detailed experimental studies of this nonlinear QED process at high statistics and accuracy. This will provide a sensitive test of theory at unprecedented precision.

For completeness, we note that the photon splitting process can in principle also be triggered by constant electromagnetic fields and laser fields,<sup>[473–482]</sup> but is typically suppressed in these cases.

## 11.3. Photon Scattering

In the scenario detailed in Section 11.1.2, also quasi-elastic scattering of gamma photons off the optical high-intensity laser pulse would constitute a signature of quantum vacuum nonlinearity. For the specific scenario considered there, the maximum value for the total number of quasi-elastically scattered gamma photons is given by  $N_{\text{tot}} = (196/9)N_\perp \simeq 21.8N_\perp$ .<sup>[483]</sup> However, for kinematic reasons, these signal photons are scattered into the forward opening angle of the gamma beam,<sup>[445]</sup> and thus generically cannot be discerned from the large background of the gamma photons constituting the probe and traversing the interaction region essentially unmodified. In turn, aiming at measuring the quasi-elastic scattering signal, collimators would be needed to reduce the divergence of the gamma photons before the interaction with the high-intensity laser pulse.<sup>[484–486]</sup> The same is true for scenarios envisioning the collision of gamma photons with the photons constituting the initial laser beam.

Experimental bounds on elastic photon–photon scattering from direct searches with optical and X-ray beams are discussed in refs. [487, 488], while refs. [489–492] present recent experimental evidence of light-by-light scattering with almost real photons in the ATLAS and CMS experiments at CERN.

Finally, we note that for gamma-photon versus laser-photon collisions, the GF will enable center-of-mass energies in the range of  $\sqrt{s} \simeq 1 \dots 120$  keV at a luminosity of up to  $L \simeq 10^{40} \text{ cm}^{-2}\text{s}^{-1}$ .<sup>[467]</sup> For center-of-mass energies below the electron-positron pair-production threshold, that is,  $\sqrt{s} < 2m_e \simeq 1$  MeV, no real electron–positron pairs are produced in such collisions. On the other hand, for prospective gamma-photon versus gamma-photon collisions, one could in principle probe center of mass energies in the range  $\sqrt{s} \simeq 1 \dots 800$  MeV at a luminosity of up to  $L \simeq 10^{27} \text{ cm}^{-2}\text{s}^{-1}$ . Note however, that in this parameter regime the signature of light-by-light scattering is likely obscured by electron–positron pair production via the Breit–Wheeler process<sup>[493]</sup> and the corresponding secondary scattering processes; confer also ref. [494].

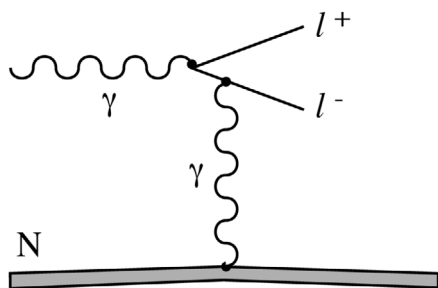
## 12. Nuclear Physics with Tertiary Beams

### 12.1. Tertiary Beams at the GF

The GF beam of gamma rays can be used to produce tertiary beams in collisions with an external stationary target. The photon-based scheme represents a change of the present, canonical paradigm for the production of such derivative beams in which the particles are produced in strong-interaction-mediated collisions. The GF tertiary-beam production scheme is based on the peripheral, small-momentum-transfer electromagnetic interactions of the photons with atoms of the target material.

An example of a Feynman diagram for peripheral production of Lepton pairs is shown in Figure 33.

In the case of peripheral electromagnetic processes, a large fraction of the wall-plug power delivered to the stored PSI beam can be transmitted to a chosen type of the tertiary beam as opposed to the proton-beam-driver schemes. A photoproduction scheme may considerably reduce the target heat-load at a fixed intensity of the produced beam, facilitating the target design and



**Figure 33.** Feynman diagram for lepton-pair production in peripheral photon–nucleus collisions. Below the muon-pair production threshold, only electron–positron pairs can be produced in this process. The cross section for production of muon pairs rises rapidly with the energy of the gamma rays. For example, for a copper target it rises from 0.2 to 10  $\mu\text{b}$  for the photon energy rising from  $\approx 400$  MeV—which is presently accessible at the LHC—to 1600 MeV, achievable by the high-energy (HE-LHC) upgrade.<sup>[495]</sup> The cross section also rises rapidly with the atomic number on the target nucleus: from 0.016  $\mu\text{b}$  for hydrogen to 30.2  $\mu\text{b}$  for lead, for 1 GeV photons. Muon photoproduction is discussed in detail in ref. [496].

circumventing the principal technological challenges which limit the intensities of the proton-beam-driven beams.

As an example, a 1 MW 300 MeV photon beam, producing a beam of  $4 \times 10^{15}$  collected positrons per second deposits 140 kW of heat power in a one-radiation-length (1X0) graphite target—only 14% of the wall-plug power dissipated in such a case.<sup>[497]</sup>

## 12.2. Polarized Electron, Positron, and Muon Sources

The high-intensity beam of gamma rays from the GF can be converted into a high-intensity beam of positrons and electrons. If the photon-beam energy is tuned above the muon-pair-production threshold, such a beam also contains a small admixture of  $\mu^+$  and  $\mu^-$ .<sup>[498]</sup>

Beams of different lepton flavors can easily be separated using both their respective and distinct kinematic characteristics and the time-of-flight method, since the produced electrons and positrons move with nearly the speed of light while the GF muons are nonrelativistic.

The target intensity of the GF source of electrons/positrons is  $10^{17}$  leptons  $\text{s}^{-1}$ , assuming the present CERN accelerator infrastructure and presently available laser technology. Such intensity, if achieved, would be three orders of magnitude higher than that of the KEK positron source,<sup>[499]</sup> and would largely satisfy the positron/electron source requirements for the proposed future high-luminosity and high-energy  $ep$  ( $eA$ ) collider project.<sup>[500]</sup>

If the secondary GF photons are circularly polarized—for example, by using circularly polarized laser photons colliding with spin-0, helium-like partially stripped ions—the first generation electrons, positrons, or muons, are polarized parallel to the photon-beam direction.

The intensity of the polarized muons which is reachable at the LHC, using the GF photon-conversion scheme, is  $10^{10}$  muons  $\text{s}^{-1}$ .<sup>[501]</sup> If achieved, it would be two orders of magnitude higher than that of the  $\pi E4$  beam at the Paul Scherrer Institute.<sup>[502]</sup> With the HE-LHC upgrade, the intensity of the polarized muon source is expected to increase to  $10^{12}$  muons  $\text{s}^{-1}$ .

The intensity of the photon-conversion-based GF polarized-muon source does not satisfy the muon-beam intensity requirements for the neutrino factory and muon collider project<sup>[503]</sup>—( $10^{13}$  muons of each sign per second). Therefore, another production scheme, suitable for generating the requisite muon fluxes, is being developed.<sup>[497]</sup> Preliminary calculations show that the requisite production rate of polarized muons can be reached for 1 MW photon beams. The principal advantage of the GF scheme, with respect to proton-beam-driver schemes, is that the product of the muon-source longitudinal and transverse emittances can be improved by more than three orders of magnitude.

There are many applications of intense muon beams, including studies of the basic symmetries of nature via searches for standard-model-forbidden muon-decay modes with unprecedented precision,<sup>[504]</sup> studies of the nuclear properties via spectroscopy of muonic atoms,<sup>[505]</sup> and revisiting the feasibility of the muon catalyzed nuclear fusion.<sup>[506,507]</sup> For the latter two applications, requiring high flux of negatively charged muons, the GF muon source has an important advantage with respect to proton driven sources producing predominantly positively charged muons. The GF tertiary, high-brilliance beams of polarized positrons and muons can open the paths to new type of fixed-target deep inelastic scattering (DIS) experiments requiring high-intensity lepton beams.

A detailed comparison of production rates of  $e^+e^-$  and  $\mu^+\mu^-$  pairs is of interest for tests of lepton flavor universality, for example, in the context of the “proton radius puzzle.”<sup>[508]</sup> A first observation of di-muonium (i.e., a bound state of  $\mu^+\mu^-$ ) production could also be of interest.<sup>[509]</sup>

## 12.3. High-Purity Neutrino Beams

Low-emittance muon beams provided by the GF source can be accelerated and stored in specially designed storage rings—which preserve polarization of stored muons—to produce muon–neutrino, electron–antineutrino, muon–antineutrino, and electron–neutrino beams of precisely controlled fluxes.

The relative fluxes of neutrinos and antineutrinos of each flavor can be precisely controlled by a frequent change of the sign of the stored muons.

Thanks to the muon polarization and ( $V-A$ )-type of the weak currents, the relative flux of muon–neutrinos (muon–antineutrinos) coming from negative-muon (positive-muon) decays, and the flux of electron–antineutrino (electron–neutrino) can be precisely controlled on the basis of their respective angular distributions. For more details see, for example, ref. [510].

The fluxes of both the neutrino and antineutrino beams should be equal and they can be predicted to a tenth of a percent accuracy, limited predominantly by the measurement of the muon-beam current in the muon storage ring.

## 12.4. Neutron and Radioactive Ion Sources

The energy of the GF photons can be tuned to excite the GDR (see Section 4.3) or fission resonances (Section 4.5) of large- $A$  nuclei, providing abundant sources of: 1) neutrons with the target intensity reaching  $10^{15}$  neutrons  $\text{s}^{-1}$  (first-generation neutrons), 2)

radioactive, neutron-rich ions (coming from fission of heavy nuclei) with the target intensity reaching  $10^{14}$  isotopes  $s^{-1}$ <sup>[511]</sup> (see also Section 8).

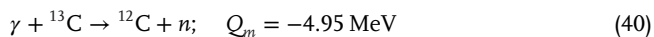
The above fluxes would approach those of other European projects under construction, such as the European Spallation Source (ESS), FAIR and the future EURISOL facilities. The advantage of the GF sources is their high efficiency—almost 10% of the LHC RF power can be converted into the power of the neutron and radioactive-ion beams. The high-flux neutron source could provide new opportunities for investigation of the basic symmetries of nature, for example, via searches for the permanent electric dipole moment (EDM) of the neutron (see ref. [512] and references therein) or neutron-antineutron oscillations.<sup>[513]</sup>

Finally, the tertiary beams of neutrons and radioactive neutron-rich isotopes could open a wide spectrum of industrial and medical applications in the domains of: 1) muon catalyzed cold fusion;<sup>[506,507]</sup> 2) energy-amplifier (EA) research<sup>[514]</sup>; and 3) production of ions for positron emission tomography (PET) and for the selective cancer therapy with alpha emitters.<sup>[515]</sup>

## 12.5. Production of Monoenergetic Fast Neutrons

Monoenergetic neutrons can be produced in  $(\gamma, n)$  reactions near narrow resonances like the ones in  $^{13}\text{C}$  (see Appendix B). If the gamma beam is polarized, the polarization will be transferred to the neutrons.

As an example, consider neutron production using the 8.86 MeV resonance of  $^{13}\text{C}$  (see Appendix B.1). Neutrons will be produced in the reaction<sup>[516]</sup>



Here the energy release of the reaction is  $Q_n \approx T_n - E_\gamma$ , neglecting the recoil energy of  $^{12}\text{C}$ . With this, we find that the kinetic energy of the neutron  $T_n \approx 3.9$  MeV is lower than the energy of the first excited state of  $^{12}\text{C}$  (4.44 MeV). Therefore, only ground-state  $^{12}\text{C}$  will be produced and the neutrons will be nearly monoenergetic.

The neutron-production rate is essentially the same as the gamma-absorption rate (Appendix B.1). For a  $1 \times 1 \times 1 \text{ cm}^3$  target containing 1 g of  $^{13}\text{C}$ , we estimate the neutron-production rate as  $5.4 \times 10^{10} \text{ s}^{-1}$ .

A potential problem for a source is reabsorption of neutrons: the produced neutrons may further react with the target according to



Given  $T_n \approx 3.9$  MeV, we get  $E_\gamma \approx 12.1$  MeV. The cross section for this neutron-capture process can be estimated as<sup>[517]</sup>

$$\sigma_{\text{tot}} = 2\pi(R + \lambda)^2 \quad (42)$$

where  $\lambda$  is the reduced wavelength of the neutron,  $R = 2.5$  fm,  $\lambda = \hbar/p = \hbar c/\sqrt{2mc^2 T_n} = 2.30$  fm ( $p$  is the neutron momentum), yielding  $\sigma_{\text{tot}} \approx 1.4$  b. With a  $1 \times 1 \times 1 \text{ cm}^3$  target containing

1 g of  $^{13}\text{C}$ , fewer than 10% of the neutrons will be reabsorbed, so the issue appears tractable.

As for the 7.55 MeV resonance (Appendix B.2), the production rate of neutrons with  $T_n \approx 2.6$  MeV is  $9.0 \times 10^9 \text{ s}^{-1}$ . The cross section for the neutron-capture process is 2.1 b. Again, fewer than 10% of the neutrons will be reabsorbed.

Narrow gamma resonances in conjunction with the GF, will thus allow producing monoenergetic neutrons at a set of well defined energies (e.g., 2.6, 3.9 MeV,... for the case of a  $^{13}\text{C}$  target). Such neutrons may be useful for measuring cross sections of processes (e.g., neutron capture) relevant to astrophysics.

It is important to note that the angular distribution of the neutrons will be nearly isotropic, suggesting a geometry for the target to study the interaction of the produced neutrons: it could be a “ball” surrounding the neutron-production target.

## 12.6. Metrology with keV Neutrons

Tertiary neutrons produced in  $(\gamma, n)$  reactions can be used to improve the operation quality of the GF. The gamma-beam energy above the neutron threshold (typically, around 7 MeV) can be measured with high accuracy by measuring the time-of-flight (TOF) of the neutrons. By subtracting the large fixed neutron binding energy, resulting in rather slow neutrons with keV energies together with a sharp start signal for the TOF measurement, a high resolution at the  $10^{-7}$  level can be achieved.<sup>[518]</sup> This enables a fast measurement of the average gamma-beam energy and the width of the gamma beam without perturbing the GF. This could provide feedback for adjusting the ion-beam energy, thus facilitating experiments requiring precise control of the ion-beam or gamma-ray energy.

## 13. Nuclear Physics Opportunities at the SPS

The proof-of-principle (PoP) GF experiment is proposed at the SPS.<sup>[7]</sup> Here, we have a much lower relativistic factor,  $\gamma \lesssim 220$ .

Since it is nontrivial to get low-energy gamma rays with  $\gamma \geq 200$  at the LHC, the operation at the SPS extends the available energy range of the secondary photons. Note that for X-rays, there exist intense coherent sources, for example, the European XFEL<sup>[101]</sup> producing X-rays with energies  $\lesssim 30$  keV.

At the SPS, with  $\lesssim 10$  eV primary laser photons, secondary photon energies of up to 1.6 MeV will be available. The use of an FEL primary-photon source (primary photon energies of up to a few hundred eV) can extend the energy range, partially overlapping with the range that should be available at the LHC with conventional lasers.

Already with the secondary-photon energies available with the currently planned PoP experiment,<sup>[7]</sup>  $\lesssim 44$  keV, interesting new results could be obtained. Table 2 contains information on nuclear transitions in the range 0.008–60 keV. We have also discussed nuclear Raman transitions accessible with the secondary photon beams (or even with primary beams if an FEL is used) at the SPS in Section 2.2.

The SPS experiments could also serve as a platform for development of laser cooling of the PSI and ion sources, for example,  $^{201}\text{Hg}$  and investigation of its 1.5 keV gamma resonance (see Table 2).

**Table 11.** Survey of the existing (first three lines) and future relativistic heavy-ion facilities. The maximum photon energy is given assuming hydrogen-like ions interacting with a primary laser beam in the optical range (down to 100 nm). With a dedicated FEL used as a primary source of higher energy photons (+ heavier ion) the maximum secondary photon energy can be increased further.

Facility	Lab.	p <sup>+</sup> energy	Max. photon energy
LHC	CERN	6.5 TeV	Pb <sup>81+</sup> + 12.6 eV → 373 MeV
SPS	CERN	450 GeV	Ti <sup>21+</sup> + 11.7 eV → 2.1 MeV
RHIC	BNL	255 GeV	Cl <sup>16+</sup> + 11.8 eV → 0.74 MeV
NICA	JINR	12.6 GeV	Li <sup>2+</sup> + 10.2 eV → 0.83 keV
SIS 100	GSI	29 GeV	B <sup>4+</sup> + 10.2 eV → 6.4 keV
SIS 300	GSI	87 GeV	Ne <sup>9+</sup> + 12.1 eV → 86 keV
SC-SPS	CERN	1.3 TeV	Kr <sup>35+</sup> + 11.4 eV → 15 MeV
HE-LHC	CERN	13.5 TeV	U <sup>91+</sup> + 7.8 eV → 0.96 GeV
FCC-hh	CERN	50 TeV	U <sup>91+</sup> + 2.1 eV → 3.5 GeV

## 14. Speculative Ideas and Open Questions

### 14.1. Applying the Gamma Factory Ideas at Other Facilities

The ideas of the GF can also be implemented at other facilities. In fact, back-scattering of laser photons from hydrogen-like ions and laser cooling of PSI were considered for RHIC.<sup>[10]</sup> A survey of the existing and future accelerator facilities where GF concepts may be implemented and the projected parameters of the corresponding gamma sources are surveyed in **Table 11**.

### 14.2. Nuclear Waste Transmutation

Nuclear waste characterization and transmutation is an important topic on the world-wide scale. Nuclear waste usually contains both stable and unstable isotopes including long-lived fission products (LLFPs) that are particularly troublesome as they usually require secure storage for thousands of years. A possible route toward a solution is transmutation of the dangerous isotopes.<sup>[519]</sup> To effectively transmute LLFPs into stable isotopes or short-lived radioactive products, one needs to avoid newly producing dangerous isotopes in the process. A selective isotope-transmutation method for LLFPs with neutron-separation thresholds lower than those of other isotopes using quasi-monochromatic gamma-ray beams was proposed in ref. [520]. To realize this, narrow-band gamma rays with tunable energy and high photon fluxes beyond the capabilities of existing facilities are needed.<sup>[521]</sup> While the secondary photons at the GF with expected total photon fluxes  $j \approx 10^{17}$  ph s<sup>-1</sup> will not bring this proposal into practice and transmute nuclear waste efficiently, the role of the GF could be to enable proof-of-principle experiments and to measure ( $\gamma, n$ ) cross sections of unstable isotopes, most of which have not been measured.

### 14.3. Laser Polarization of PSI

The interaction of polarized primary photons with the PSI generally leads to polarization of both electron and nuclear spins of the

PSI (assuming the ground-state electronic angular momentum and nuclear spin are nonzero). It is currently unclear if there is a viable scheme to preserve the electron polarization on a round trip in the storage ring. As for the nuclear spins, the task should presumably be easier on the account of much smaller values of the nuclear magnetic moments. Techniques for preserving proton polarization using so-called “Siberian snakes”<sup>[522]</sup> have been implemented, for instance, at RHIC, and could, presumably, be adopted to the PSI at the GF. There is an additional question of whether nuclear polarization will survive a round trip in a non-bare ion.<sup>[523]</sup>

As mentioned in ref. [3], regardless of whether the polarization survives a round trip, there are interesting physics opportunities with polarized PSI beams, for example, parity-violating structure-function studies (Section 7.1) or fixed-target experiments with polarized PSI.

### 14.4. Quark–Gluon Plasma with Polarized PSI

The availability of nuclear spin-polarized PSI produced at the GF opens a possibility, briefly discussed in ref. [3], to study collisions of such polarized ions and the resulting quark–gluon plasma.

Indeed, collisions of polarized nuclei, particularly deformed ones, is an active area of research in heavy-ion collisions. Here, optical polarization control may offer an alternative to the currently employed inference of the polarization of initial deformed nuclei based on the final particle distribution using two observables—multiplicity and ellipticity—as proposed<sup>[524]</sup> and experimentally realized at RHIC.<sup>[525]</sup>

### 14.5. Ground-State Hyperfine-Structure Transitions in PSI

The ground-state hyperfine intervals of heavy PSI with nonzero-spin nuclei can be in the eV range. Knowledge of these interval is important, for example, for the study of QED effects and hyperfine anomalies in strong magnetic fields as well as for determination of nuclear moments.<sup>[526]</sup> A few of such hyperfine intervals were measured in electron-beam ion traps via emission spectroscopy (see, for example, refs. [527–529]). Measurements were also performed via laser-spectroscopy in low-energy storage rings, where one can benefit from laser cooling of the PSI, see, for example, refs. [15, 530, 531].

The GF may enable a somewhat different approach to precision spectroscopy of hyperfine intervals of heavy PSI. Optical pumping (Section 14.3) easily creates hyperfine polarization. (Hyperfine polarization will also naturally result from the radiative decay of the upper state.) Conversely, the rate of production of secondary photons by polarized primary photons depends on the hyperfine state, and so monitoring this rate can be used for “optical probing” of the hyperfine state. The experiment would consist in measuring the flux of secondary photons produced by optically pumped PSI as a function of the frequency of an applied magnetic field that, when resonant with the hyperfine interval, will drive the M1 transition between the hyperfine states and redistribute their population. The matrix element of the M1 transition between the hyperfine states is on the order of a Bohr magneton, and the transition can thus be driven with a relatively modest

magnetic field. To produce such a magnetic field in the frame of the PSI, one can pass the ions through an undulator (e.g., a Halbach array made up of permanent magnets similar to the common “refrigerator magnets”) or a microwave source. Transverse magnetic fields as seen by the PSI are scaled up in magnitude by the relativistic factor compared to their value in the laboratory frame. Scanning of the frequency can be done by adjusting the relativistic factor of the PSI.

To get a feeling for some of the parameters, let us consider the 1.2 eV hyperfine interval in the ground state of hydrogen-like  $^{207}\text{Pb}^{81+}$  ions. The required microwave frequency is around 100 GHz, and the required undulator period is about 3 mm. We note also that spontaneous emission on the hyperfine transition results in forward-directed radiation with maximum photon energy of  $\approx 7$  keV in the laboratory frame. However, due to a relatively long lifetime of the upper ground-state hyperfine level, which is about 50 ms in the ion rest frame, the radiation will not be localized to the interaction point.

#### 14.6. Detection of Gravitational Waves

Laser cooling of the PSI beam in general and extreme laser cooling with nuclear transitions (Section 2.4.2) in particular can help turn the LHC into a gravitational wave detector.<sup>[532]</sup> This possibility was discussed for many years, including a dedicated workshop.<sup>[533]</sup> The general idea is that gravitational waves can resonantly couple to specific modes of the ion motion in the storage ring and the low emittance that may be achievable with laser cooling combined with precise beam-position monitors may result in a competitive scheme for gravitational-wave detection, complementing other Earth-based and space-borne facilities. The practicality and ultimate sensitivity of this method will need to be evaluated in future work.

### 15. Conclusions and Optimistic Outlook

In compiling this review of nuclear physics opportunities associated with the GF, the interdisciplinary team of authors, including both theorists and experimentalists, had an opportunity to take a fresh look at this vast field as well as at a range of related fields. We are firmly convinced that the new technologies associated with the GF will lead to significant progress on many “fronts,” and will likely lead to disruptive breakthroughs, although exactly where these will occur is difficult to predict.<sup>[534]</sup>

One of the interesting aspects of the GF science program is its complementarity to other experimental approaches, for instance, the physics done with electron-beam facilities. Many of the opportunities discussed in this review are unique to the GF, the advent of which will lift the limitations of the hitherto available photon sources. But even in the cases where the same underlying physics can be accessed with multiple approaches (for instance, measurement of neutron distributions within nuclei), consistency of the results obtained with these different probes would serve as robust check for the different experiments and supporting theory.

As with the earlier review of atomic-physics opportunities with the GF,<sup>[3]</sup> it is likely that, due to the rapid progress of ideas, the

paper will be outdated even before it is published. For example, the ongoing optimization of the LHC operation parameters dedicated to the GF operation may lead to more optimistic performance estimates across the board, especially with laser cooling. Nevertheless, it is our hope that these overviews will serve as suitable departure points for generating further ideas, conducting more in-depth studies, and, importantly, will become the bases for planning for specific experiments.

### Appendix A: Survey of Existing and Forthcoming Gamma Facilities

Here we briefly discuss the currently available sources of photons (partially) overlapping in energy with the reach of the GF. Tagged-photon facilities (summarized in **Table A1**) can be exemplified by The Electron Stretcher Accelerator (ELSA) facility in Bonn.<sup>[542]</sup> Here, a pulsed electron beam from a linac system is stretched in a storage ring before it hits an aluminum foil in which bremsstrahlung is produced. A magnetic spectrometer is used to determine the energy of the post-bremsstrahlung electrons. The “tagged photons” range in energy from 10 to 180 MeV. The energy resolution of about 300 keV; the photon rates of up to  $4 \times 10^6$  photons  $\text{s}^{-1}$   $\text{MeV}^{-1}$  have been achieved.

Compton-backscattering facilities using relativistic electron beams are summarized in **Table A2**.

**Table A1.** Bremsstrahlung tagged-photon facilities around the world.

Facility name	MAMI A2	JLab Hall D	ELSA	MAX IV
Location	Mainz	Newport News	Bonn	Lund
Electron energy [GeV]	1.6	12	4.68	220
Max $\gamma$ energy [MeV]	1600	9200	2400	180
Energy resolution [MeV]	2–4 MeV	30	12.5	0.3
Photon polarization	$\leq 0.8$	$\leq 0.4$		–
Max on-target flux [ $\gamma$ $\text{s}^{-1}$ ]	$10^8$	$10^8$	$5 \times 10^6$	$4 \times 10^6$
Reference	[535]	[536]	[537]	[538]

### Appendix B: Gamma Resonances in $^{13}\text{C}$

The relevant nuclear levels of  $^{13}\text{C}$  are depicted in Figure 8. Here we discuss several specific resonances.

#### B.1. The 8.86 MeV M1 Resonance

On-resonance cross section for the gamma transition is<sup>[517]</sup>

$$\sigma_0 = 2\pi \left( \frac{\hbar c}{E_\gamma} \right)^2 \frac{2I_e + 1}{2I_g + 1} \frac{\Gamma_\gamma}{\Gamma_{\text{tot}}} \quad (\text{B1})$$

where the quantity in parentheses is the reduced wavelength of gamma rays and  $I_g$  and  $I_e$  are the spin quantum numbers of the nuclear ground and excited states, respectively.  $\Gamma_{\text{tot}}$  is the total width of the excited state and  $\Gamma_\gamma$  is the partial width corresponding to the direct gamma transition from the excited state to the ground state. In this case,  $I_g^P = 1/2^-, I_e^P = 1/2^-, \Gamma_\gamma = 3.36$  eV,  $\Gamma_{\text{tot}} = 150$  keV,<sup>[516]</sup> yielding  $\sigma_0 = 7.0 \times 10^{-4}$  b.

By proper collimation, we can tune the energy-spread width of GF photons  $\Gamma_{\text{ph}}$  to be  $\Gamma_{\text{ph}} = \Gamma_{\text{tot}} = 150$  keV. The effective photon flux is approximately  $J_{\text{eff}} = j\Gamma_{\text{ph}}/E_\gamma = 1.7 \times 10^{15} \text{ s}^{-1}$ , where  $j = 10^{17} \text{ s}^{-1}$  is the total photon flux expected at the GF before collimation.

**Table A2.** Parameters of existing and forthcoming Compton back-scattering  $\gamma$ -ray sources around the world, from. refs. [539–541] These sources are based on photon scattering from beams of relativistic electrons circulating in storage rings.

Facility name	ROKK-1M	GRAAL	LEPS	HI $\gamma$ S	ELI-NP	SLEGS	CLS <sup>a)</sup>	GF
Location	Novosibirsk	Grenoble	Harima	Duke	Bucharest	Shanghai	Saskatoon	CERN
Storage ring	VEPP-4M	ESRF	SPring-8	Duke-SR	linac	SSRF	2.9 GeV	LHC
Laser–photon energy [eV]	1.17–4.68	2.41–3.53	2.41–4.68	1.17–6.53	1.50–1.52	0.117 (CO <sub>2</sub> )	0.117 (CO <sub>2</sub> )	multiple
$\gamma$ -beam energy [MeV]	100–1600	550–1500	1500–2400	1–100 (158)	0.2–20	<22	$\leq 15$	$\leq 400^b)$
$\Delta E/E$	0.01–0.03	0.011	0.0125	0.008–0.1	0.005		$\sim 0.0011^c)$	$\sim 10^{-4} - 10^{-6}$
Max on-target flux [ $\gamma$ s <sup>-1</sup> ]	10 <sup>6</sup>	3 $\times 10^6$	5 $\times 10^6$	10 <sup>4</sup> –5 $\times 10^8$	8 $\times 10^8$	10 <sup>9</sup> –10 <sup>10</sup>	10 <sup>10d)</sup>	10 <sup>17d)</sup>

<sup>a)</sup> Parameters of this facility are from ref. [395]; <sup>b)</sup> for possibility of achieving higher energy, see Sections 2.4.3 and 7; <sup>c)</sup> energy spread of 2.9 GeV electrons; <sup>d)</sup> the total photon flux.

For a <sup>13</sup>C target with a volume of  $1 \times 1 \times 1$  cm<sup>3</sup> and <sup>13</sup>C density of 1 g cm<sup>-3</sup>, the number of gamma-absorption events is

$$N = j_{\text{eff}} \frac{N(^{13}\text{C})\sigma_0}{1\text{cm}^2} = 5.4 \times 10^{10} \text{ s}^{-1} \quad (\text{B2})$$

### B.2. The 7.55 MeV E2 Resonance

For the 7.55 MeV energy level, we have  $J_g^P = 1/2^-$ ,  $J_e^P = 5/2^-$ ,  $\Gamma_\gamma = 0.115$  eV,  $\Gamma_{\text{tot}} = 1.2$  keV.<sup>[516]</sup> Then, from Equation (B1) we get  $\sigma_0 = 1.2 \times 10^{-2}$  b ( $\sigma_{7.55} = 17.7 \times \sigma_{8.86}$ ).

Following a similar procedure as in the case of the 8.86 MeV transition above, we get the effective photon flux  $j_{\text{eff}} = 1.6 \times 10^{13}$  s<sup>-1</sup> and using a <sup>13</sup>C target with the same volume and density, the number of gamma-absorption events is  $N = 9.0 \times 10^9$  s<sup>-1</sup>.

### B.3. The 3.09 MeV E1 Resonance

The first excited state of <sup>13</sup>C has an energy of 3.09 MeV with a linewidth of  $\Gamma_{\text{tot}} = \Gamma_\gamma = 0.43$  eV<sup>[55]</sup> and  $J^P = 1/2^+$ . The on-resonance cross section [Equation (B1)] is  $\sigma_0 = 260$  b. We note that Doppler broadening at room temperature  $T \approx 300$  K leads to a Doppler width  $\Gamma_D = 2\sqrt{\ln 2} E_\gamma \sqrt{2k_B T / (Mc^2)} \approx 10.6$  eV  $\gg \Gamma_{\text{tot}}$ , yielding the effective resonance photon-absorption cross section  $\sigma_{\text{eff}} \approx \sigma_0 \Gamma_\gamma / \Gamma_{\text{tot}} = 10$  b. For the interaction of  $\approx 3$  MeV photons with a <sup>13</sup>C target, the photon-attenuation background is dominated by Compton scattering off electrons,<sup>[352]</sup> which has a cross section  $\sigma_{\text{Compton}} \approx 0.7$  b  $\ll \sigma_{\text{eff}}$ . The maximal resonant photon-absorption rate is  $p_{\text{max}} \approx j\Gamma_D / E_\gamma \approx 3.4 \times 10^{11}$  s<sup>-1</sup>, giving  $1/\sqrt{p_{\text{max}}} \times 100 \text{ s} \approx 1.7 \times 10^{-7}$ .

Here we chose a 100 s measurement time for the purpose of an example. In order to reach such an absorption rate, the thickness of the <sup>13</sup>C target should be greater than the absorption length  $l \approx 2$  cm.

## Appendix C: Other Reviews and Nuclear Databases

An early review of photonuclear experiments with Compton-backscattered gamma beams is given in ref. [543]. Throughout the present paper, we frequently refer to a comprehensive review of nuclear photophysics<sup>[183]</sup> conducted in the context of the Extreme Light Infrastructure.

A comprehensive database of giant dipole resonances for many nuclei is maintained by the Russia Lomonosov Moscow State University Skobel'syn Institute of Nuclear Physics Center for Photonuclear Experiments Data. The database, “Chart of Giant Dipole Resonance Main Parameters,” can be accessed at <http://cdfe.sinp.msu.ru/saladin/gdrmain.html>.

The US National Nuclear Data Center maintained by the Brookhaven National Laboratory provides databases for gamma transitions in nuclei,

for instance NuDat 2.8 or the Evaluated Nuclear Structure Data Files <https://www.nndc.bnl.gov/ensdf>.

A database called BrIcc<sup>[31]</sup> provides theoretical values of internal conversion coefficients: <http://bricc.anu.edu.au/index.php>.

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## Conflict of Interest

The authors declare no conflict of interest.

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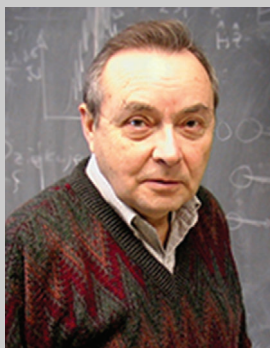
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